

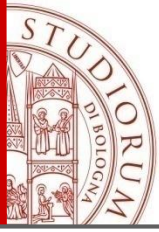
## **Seminar**

*Institut Universitaire de Technologie (IUT) de Cergy-Pontoise  
Paris, 12 September 2023*

# **A SIMPLIFIED PROCEDURE FOR THE SEISMIC DESIGN OF STRUCTURES EQUIPPED WITH FLUID-VISCOUS DAMPERS**

*Prof. Stefano Silvestri  
University of Bologna  
(Italy)*





# Presentation outline

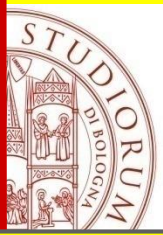
- Background
- Theoretical basis
- The “five-step procedure” (2010)
- The “direct five-step procedure” (2016-2018)
- Applicative example
- Conclusions and future developments

**MPD vs SPD systems**

## OBJECTIVES

To develop an easy method for preliminary quick design of structures equipped with fluid-viscous dampers (for the wide diffusion of their use)

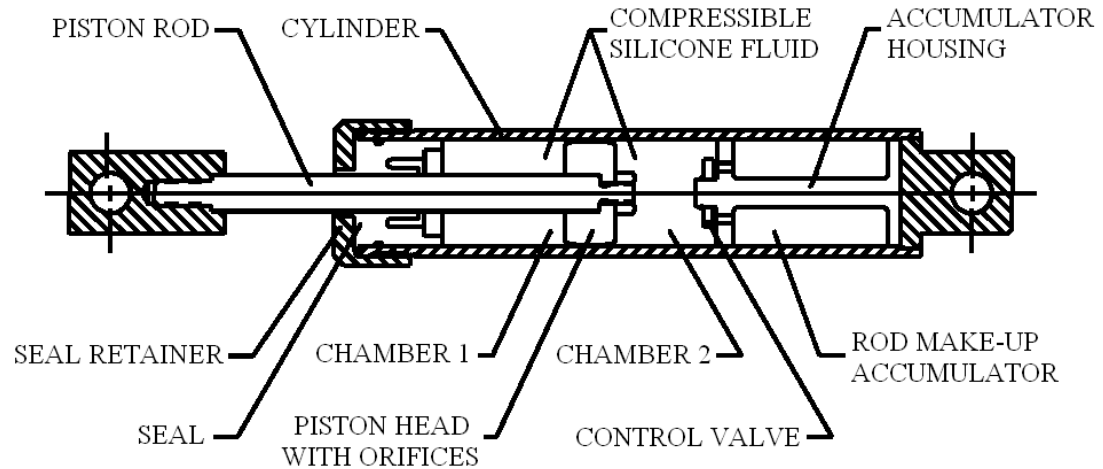
To give fully-analytical tools to the professional engineers for the control of the results of non-linear TH analyses



# Background

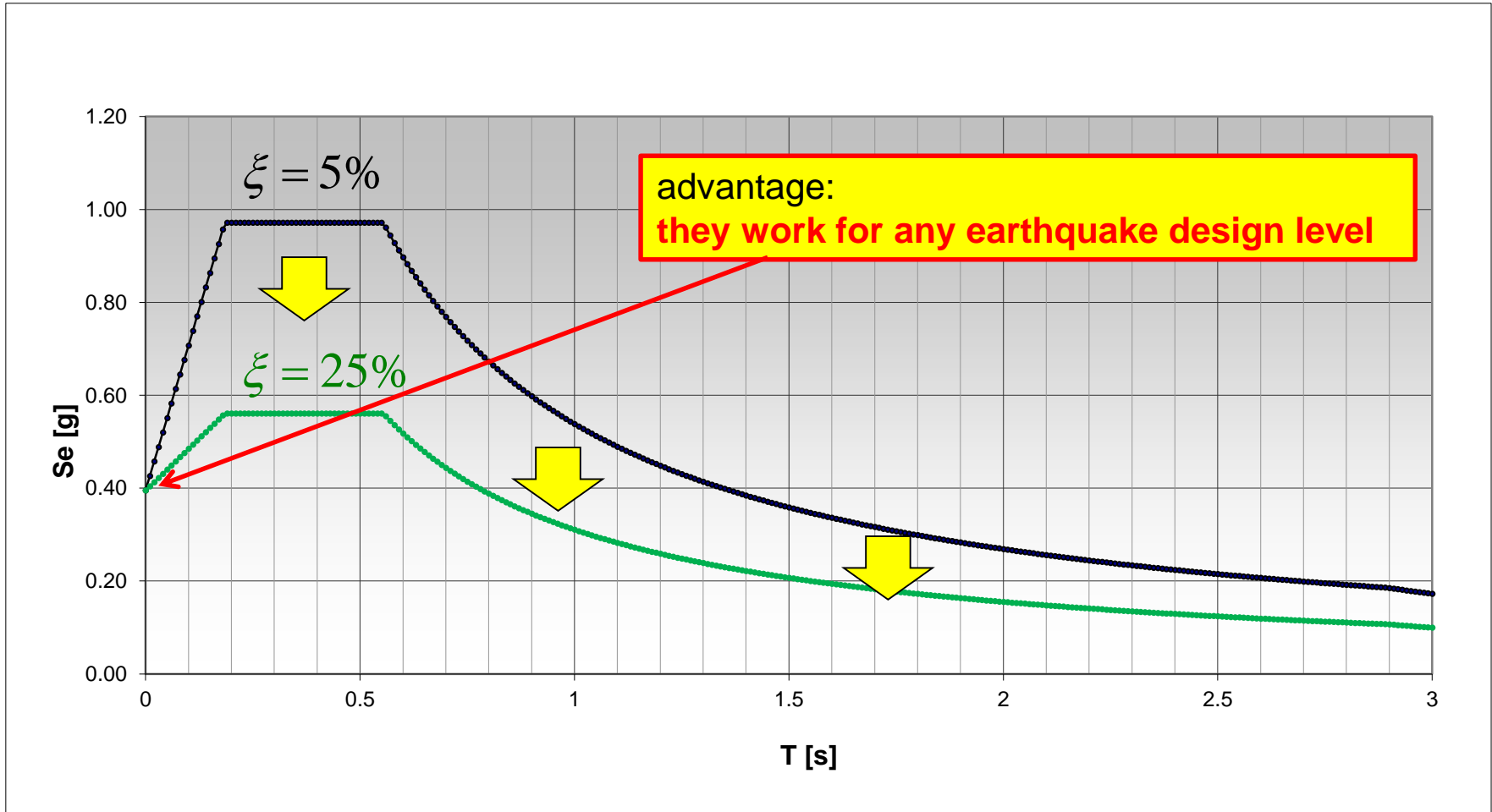
# Fluid-Viscous Dampers

**energy** is dissipated in the guise of **heat** through the passage of a **viscous silicone fluid** (stable w.r.t. temperature) across the piston head with orifices



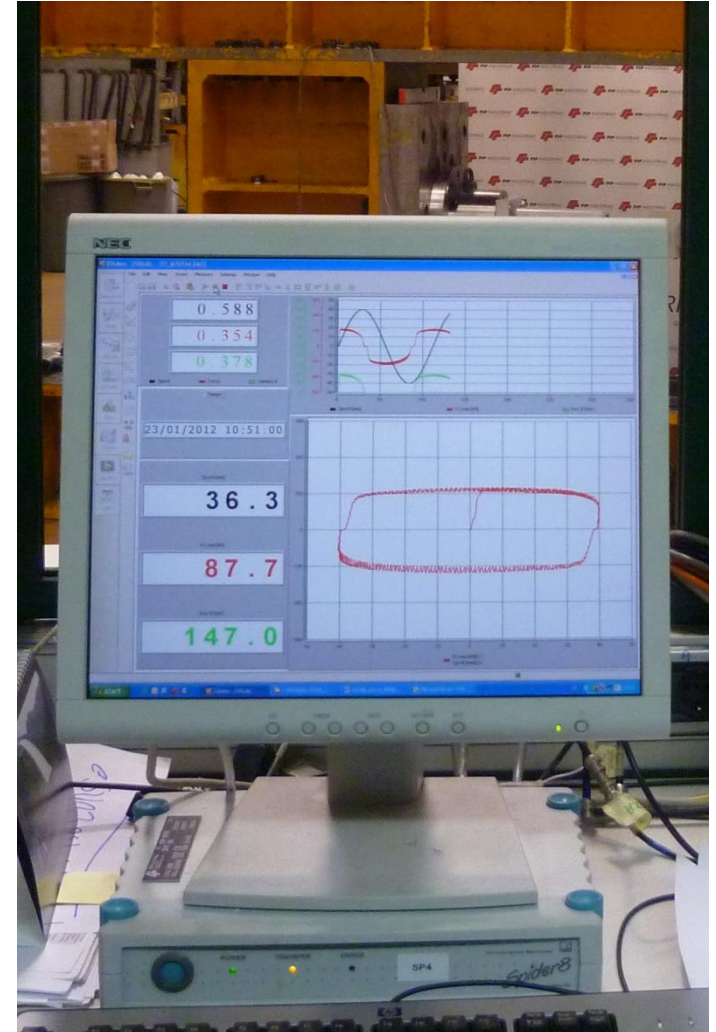


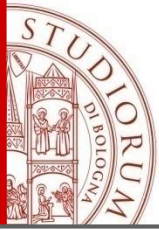
# Benefits provided by viscous dampers



# Viscous dampers

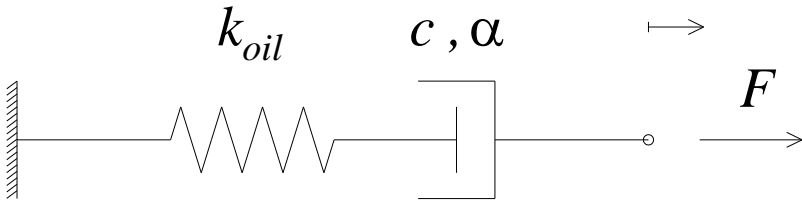
constant velocity tests



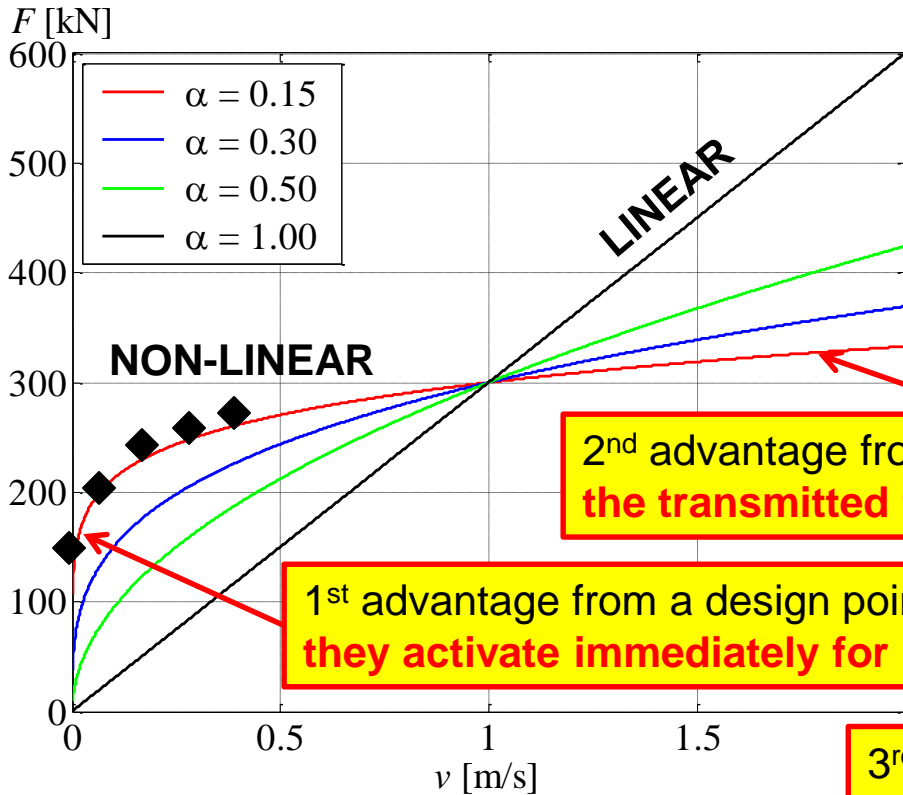


# Viscous dampers

Maxwell model:



$$F = k_{oil} \cdot x = c \cdot v^\alpha$$



$$\alpha \cong 0.15$$

$$k_{oil} = \frac{F_{max}}{5\% x_{max}}$$

half piston stroke

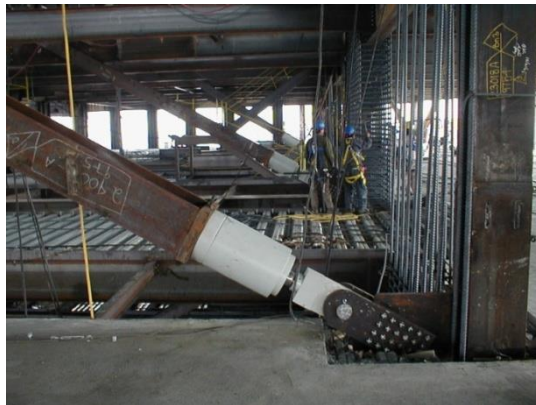
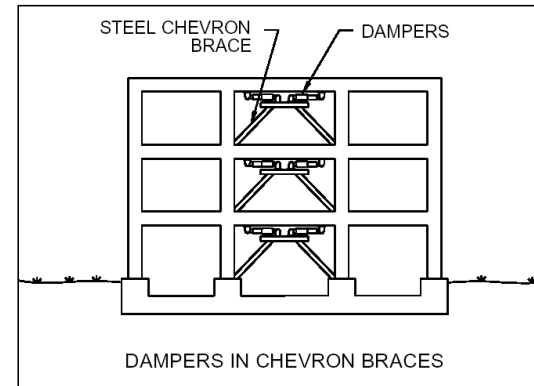
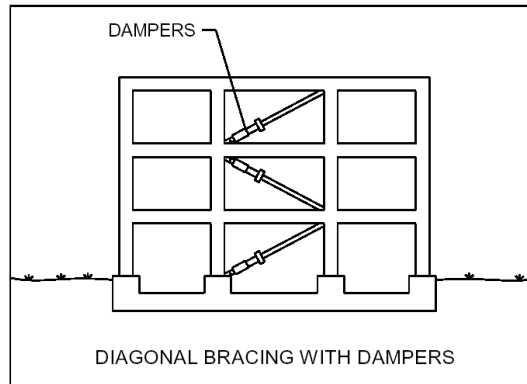
2<sup>nd</sup> advantage from a design point-of-view:  
**the transmitted force is limited!**

1<sup>st</sup> advantage from a design point-of-view:  
**they activate immediately for low velocities**

3<sup>rd</sup> advantage from a design point-of-view:  
**they don't reduce the period of vibration**

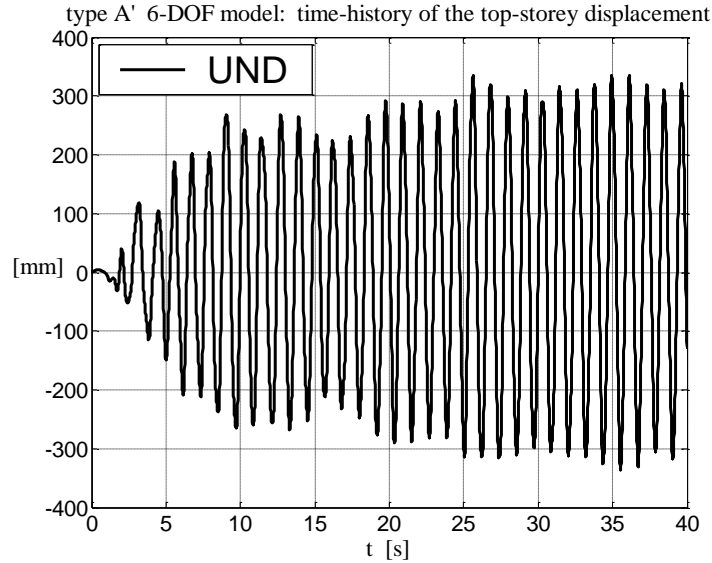
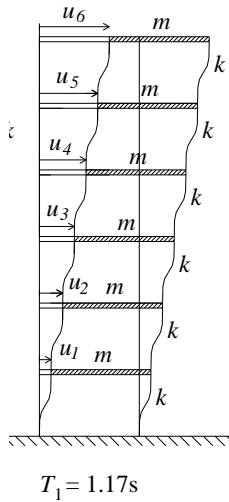
# Effectiveness

- The **effectiveness** of fluid viscous dissipative devices in reducing the seismic demand on the structural elements has been demonstrated by a number of research works and real applications since the 1980s.

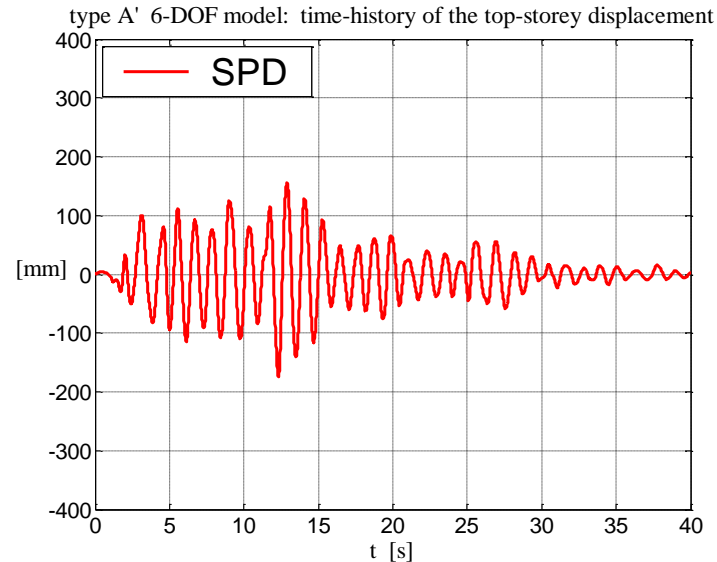
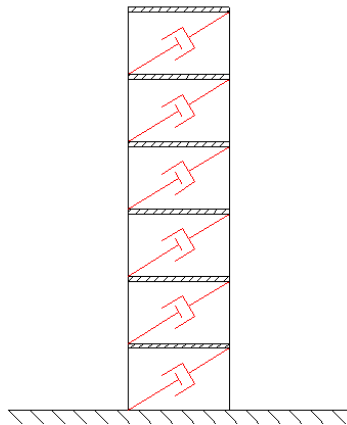


Seismic Dampers installed at the Hotel Woodland, in Woodland, California  
Force = 100,000 lbs., Stroke = +/- 2 inches  
Production = 16 pieces

# Effectiveness



**top-storey  
displacement  
response**



El Centro 1940  
scaled to  
PGA = 0.3g



# Real application



*HERA building,  
Imola (BO)*

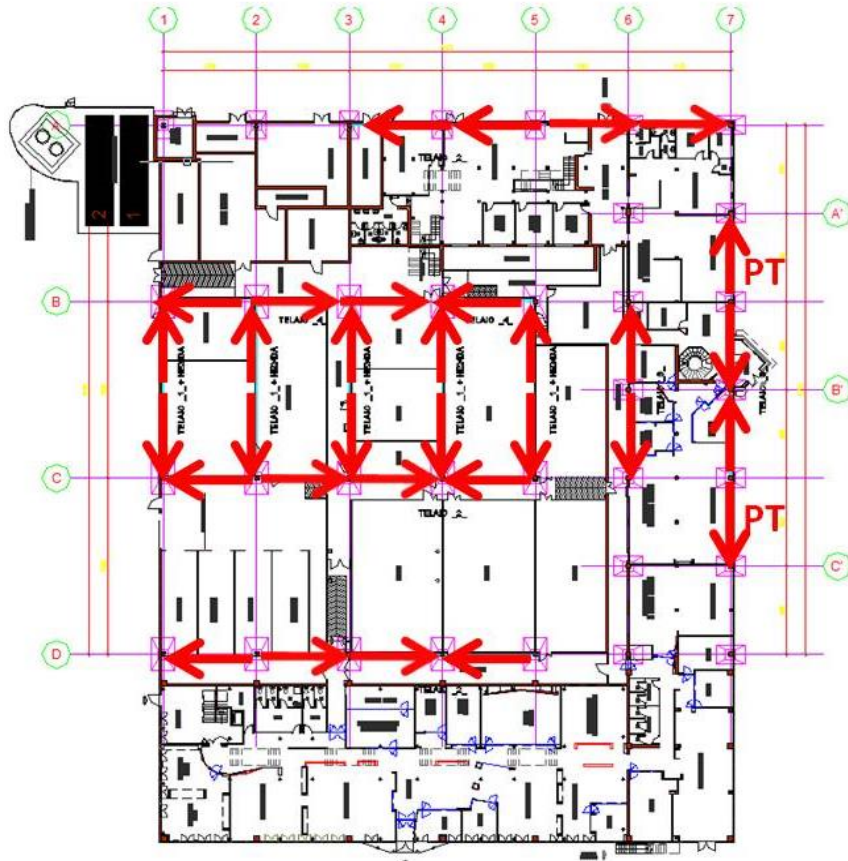
*dampers  
manufactured by  
FIP, Padova,  
Italy*

*2010-2011*

*pictures courtesy of  
Ing. Franco Baroni,  
Studio Ceccoli &  
Associati,  
Bologna*

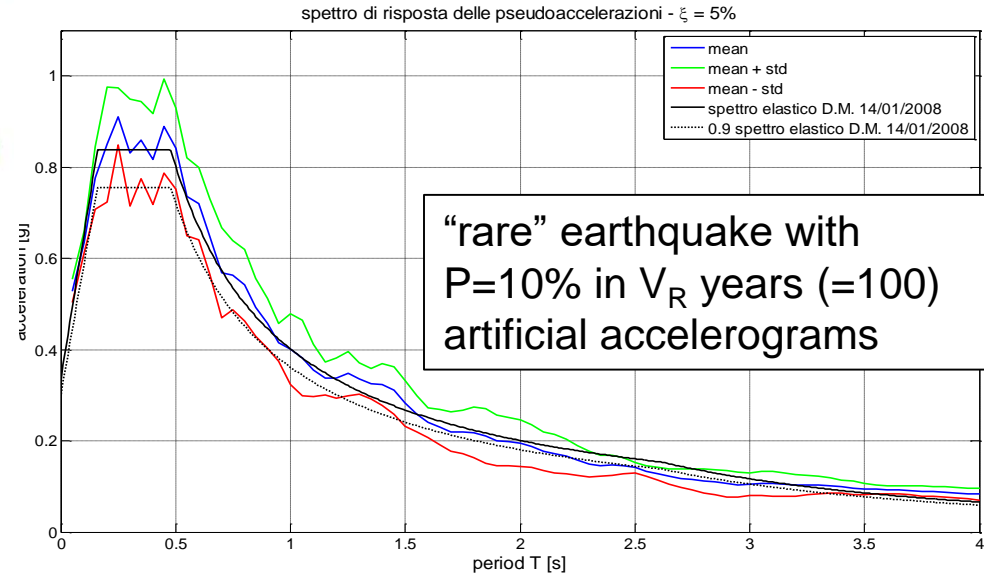


# Real application



*HERA building,  
Imola (BO)*

*n. 32 dampers  
manufactured by  
FIP, Padova,  
Italy*



# Real application



*HERA building,  
Imola (BO)*

*dampers  
manufactured by  
FIP, Padova,  
Italy*

*2010-2011*

*pictures courtesy of  
Ing. Franco Baroni,  
Studio Ceccoli &  
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# Real application



*HERA building,  
Imola (BO)*

*dampers  
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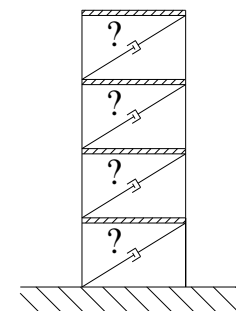
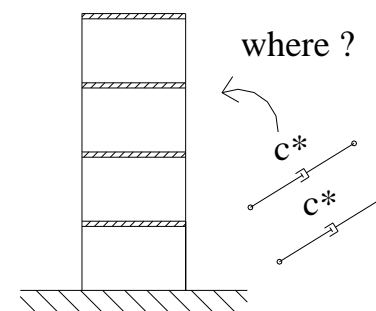
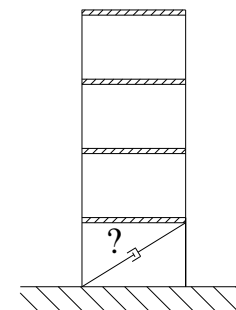
*2010-2011*

*pictures courtesy of  
Ing. Franco Baroni,  
Studio Ceccoli &  
Associati,  
Bologna*

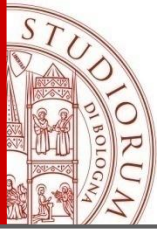
# In the scientific literature:

- **Sophisticated numerical algorithms for dampers optimization** (Takewaki 1997, 2000 and 2009, Shukla and Datta 1999, Lopez Garcia 2001, Singh and Moreschi 2002, Levy and Lavan 2006, ...)
  - **Computational expertise and time** (beyond the typical availabilities of the designers) are needed
  - **Numerical results** which do not provide physical insight into the matter.
- The issue of developing **simple/analytical methods** in order to size and locate the viscous dampers is still open.


**(like equivalent static analysis vs. non-linear time-history analysis)**

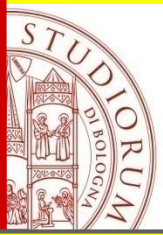






# Design procedures

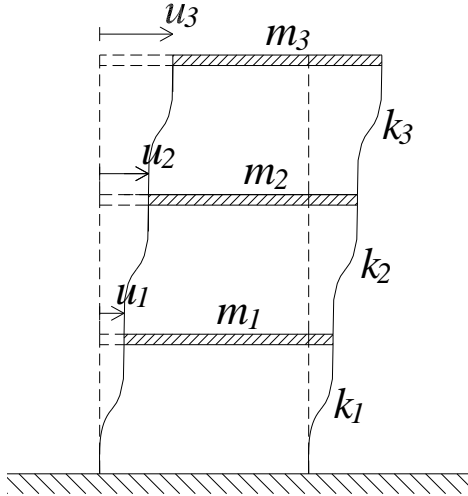
- report NCEER-92-0032 (Constantinou and Symans 1992)
- report MCEER-00-0010 (Ramirez et al. 2000)
- **ASCE 7 (2005) Chapter 18**, which is grounded on the MCEER-00-0010 approach and on the works by Ramirez et al. (2002a and b, and 2003) and by Whittaker et al. (2003), contains systematic procedures for design and analysis of building with damping systems (*use of the residual mode approach*).
- **Lopez-Garcia 2001** developed a simple **algorithm** for optimal damper configuration (placement and properties) in MDOF structures, assuming a constant inter-storey height and a straight-line first modal shape.
- **Christopoulos and Filiatrault (2006)** suggested a design approach for estimating the damping coefficients of added viscous dampers consisting in a *trial and error procedure*.
- **Silvestri et al. 2010**  “five-step procedure”



# Theoretical basis



# Insight into the Rayleigh damping

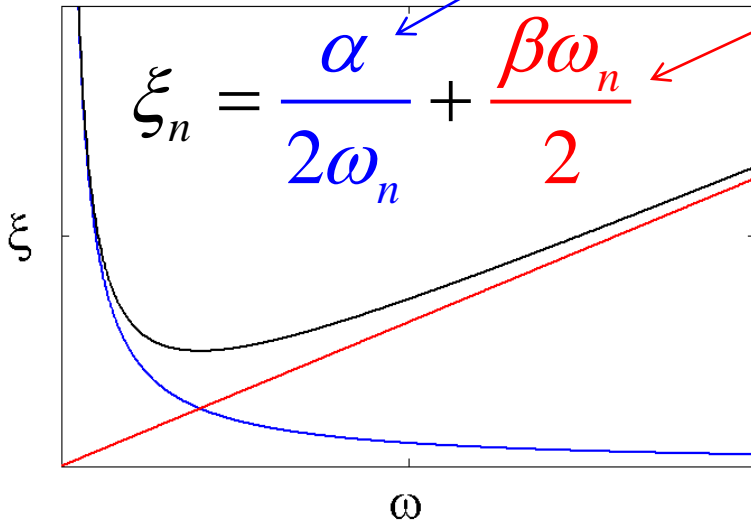


$$\underline{\tilde{m}} \ddot{\underline{u}} + \underline{\tilde{c}} \dot{\underline{u}} + \underline{\tilde{k}} \underline{u} = -\underline{\tilde{m}} \underline{1} \cdot \ddot{u}_g(t)$$

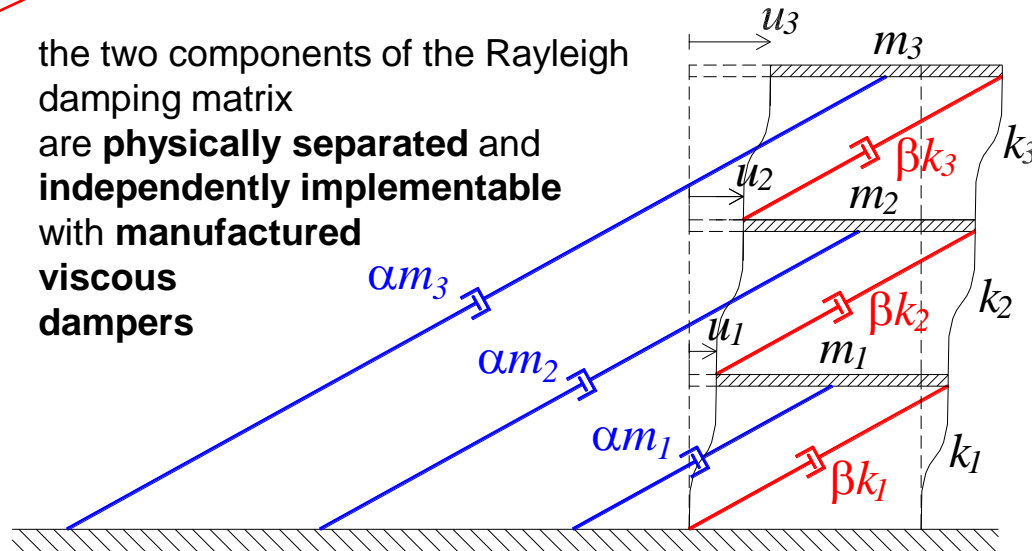
$$\underline{\tilde{c}} = \alpha \underline{\tilde{m}} + \beta \underline{\tilde{k}}$$

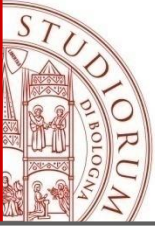
$\underline{u}$  physical coordinates vector  
 $\underline{\tilde{m}}$  mass matrix  
 $\underline{\tilde{k}}$  stiffness matrix

$$\underline{\tilde{c}} = \alpha \begin{bmatrix} m_1 & 0 & 0 \\ 0 & m_2 & 0 \\ 0 & 0 & m_3 \end{bmatrix} + \beta \begin{bmatrix} k_1 + k_2 & -k_2 & 0 \\ -k_2 & k_2 + k_3 & -k_3 \\ 0 & -k_3 & k_3 \end{bmatrix}$$



the two components of the Rayleigh damping matrix are **physically separated** and **independently implementable** with **manufactured viscous dampers**



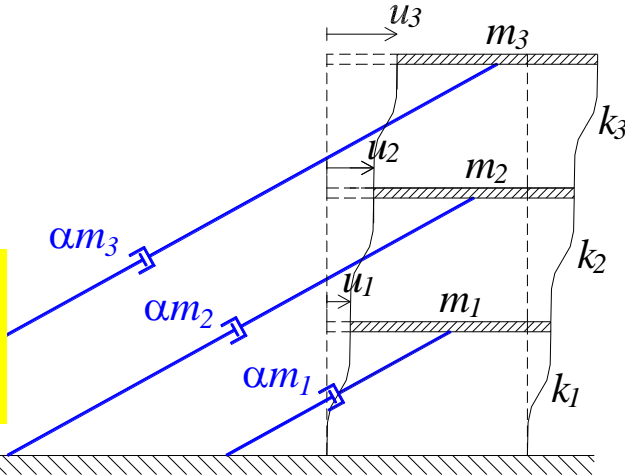


# MPD and SPD systems

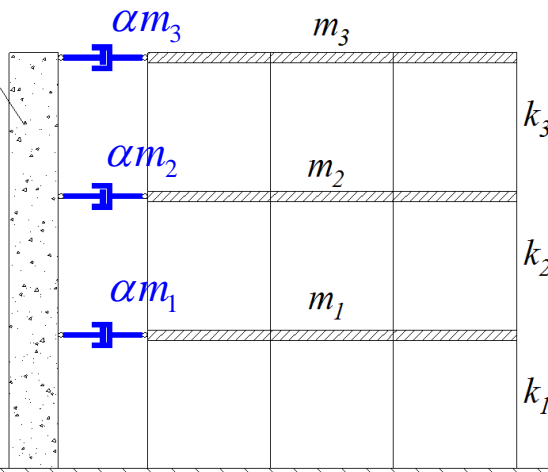
## Mass Proportional Damping system

$$\underline{\underline{c}} = \alpha \underline{\underline{m}}$$

“absolute”  
storey  
velocities



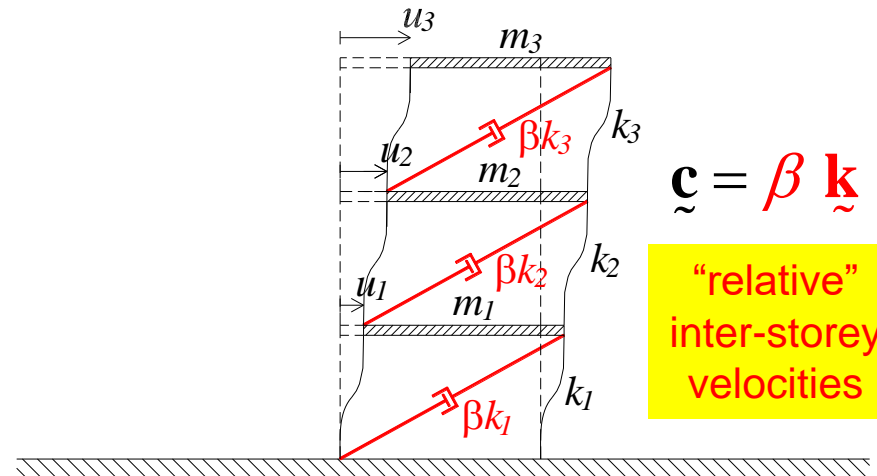
*infinitely stiff*



## Stiffness Proportional Damping system

$$\underline{\underline{c}} = \beta \underline{\underline{k}}$$

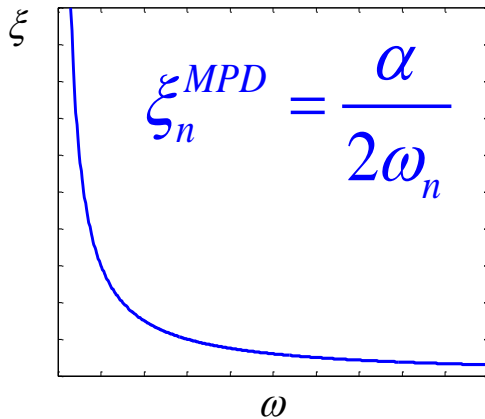
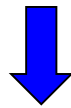
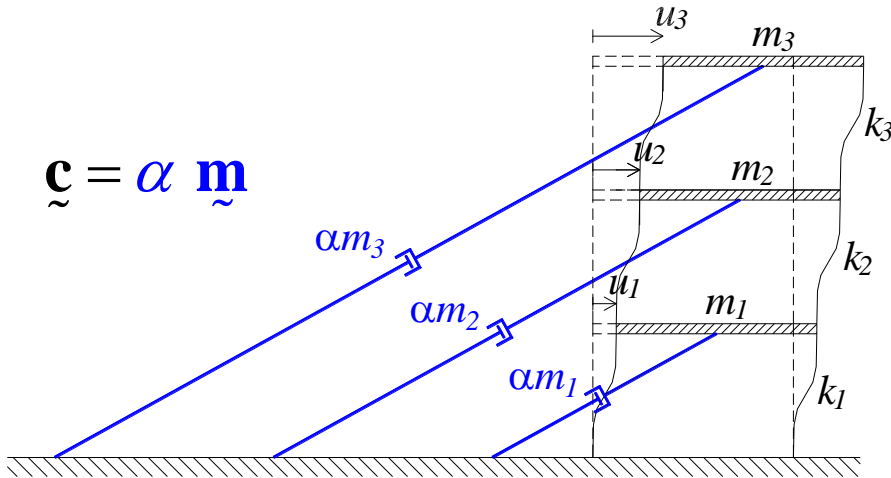
“relative”  
inter-storey  
velocities



# Properties of **MPD** and **SPD** systems (1)

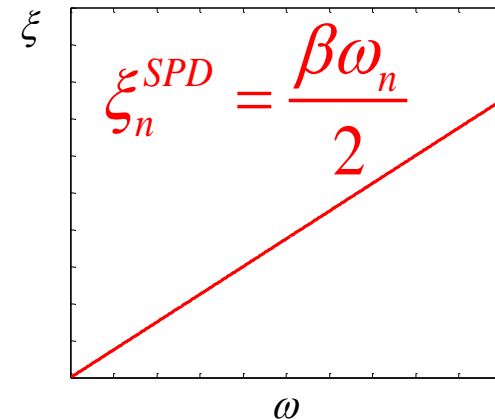
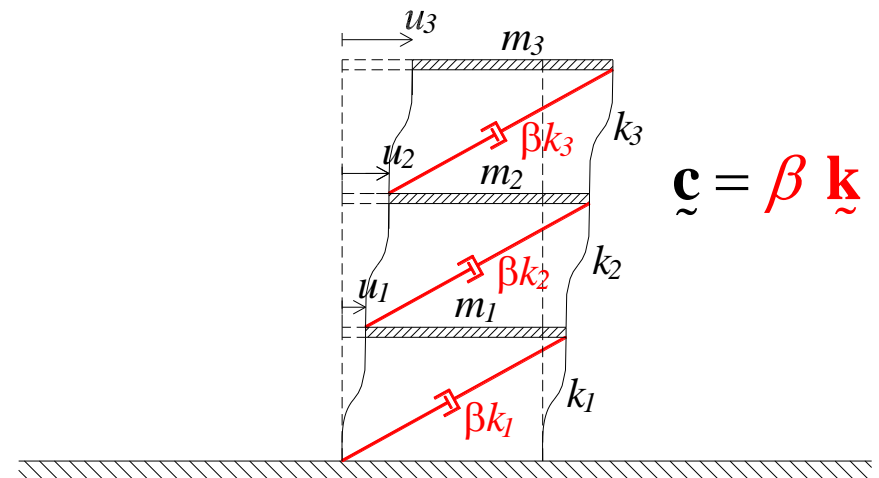
Mass Proportional Damping system

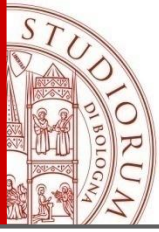
$$\underline{\underline{c}} = \alpha \underline{\underline{m}}$$



Stiffness Proportional Damping system

$$\underline{\underline{c}} = \beta \underline{\underline{k}}$$



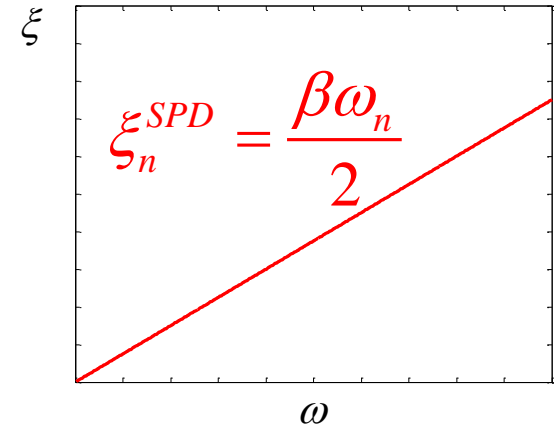
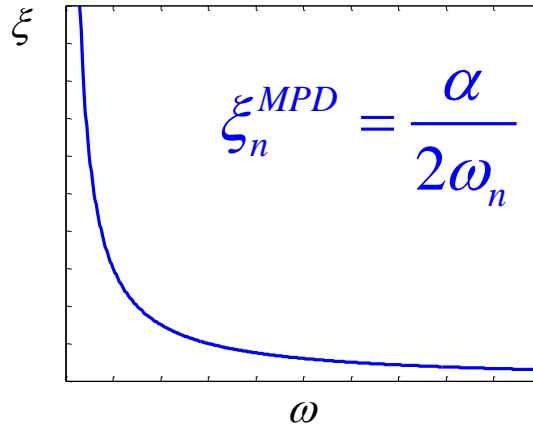


# Properties of **MPD** and **SPD** systems (2)

**HP:**

The two systems have equal total damping:

$$c_{tot} = \sum c_i$$

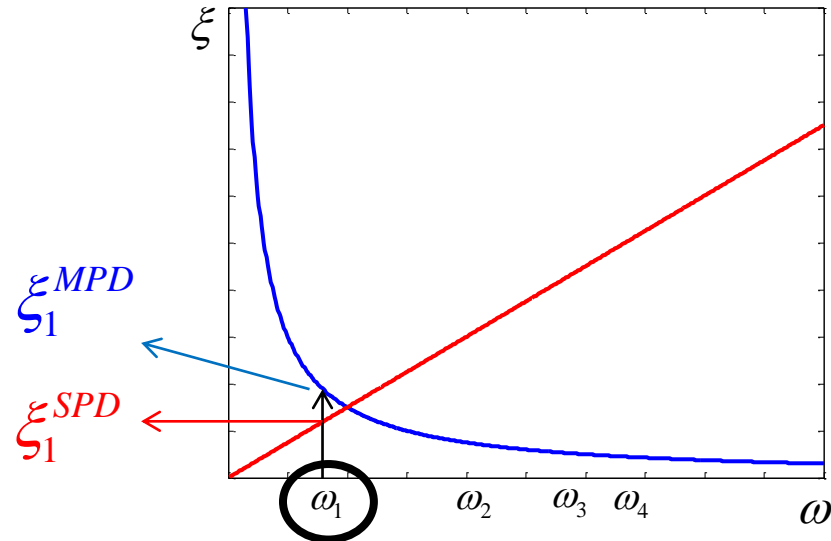


**QUESTION:**

How the **first** modal damping ratios of the SPD system and the “corresponding” MPD system are related to each other?

?

$$\xi_1^{MPD} \begin{matrix} \geq \\ \leq \end{matrix} \xi_1^{SPD}$$



# Properties of MPD and SPD systems (3)

From basic dynamics:

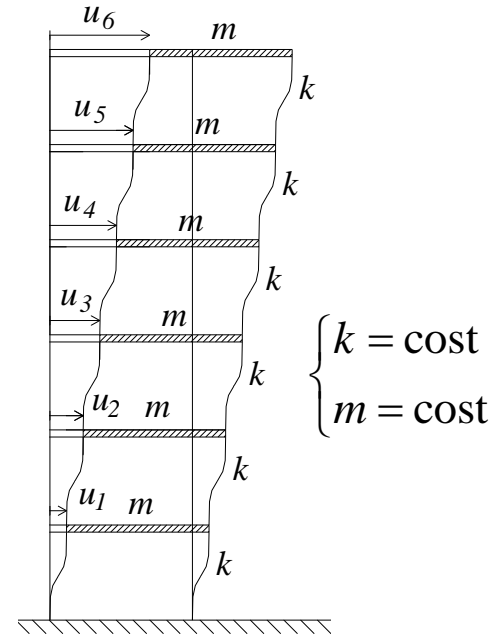
$$\frac{\xi_i^{SPD}}{\xi_i^{MPD}} = \frac{\frac{\beta}{2} \omega_i}{\frac{\alpha}{2\omega_i}} = \frac{\beta}{\alpha} \omega_i^2 = \dots$$



HP1) structures characterised by constant values of lateral stiffness  $k$  and storey mass  $m$

HP2) equal "total cost" constraint

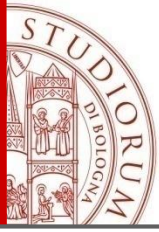
$$\left. \begin{aligned} \bar{\alpha} &= \frac{\bar{c}}{\sum_{i=1}^N m_i} = \frac{\bar{c}}{Nm} \\ \bar{\beta} &= \frac{\bar{c}}{\sum_{i=1}^N k_i} = \frac{\bar{c}}{Nk} \end{aligned} \right\} \bar{\alpha}m = \bar{\beta}k \Rightarrow \frac{\bar{\beta}}{\bar{\alpha}} = \frac{m}{k} = \frac{1}{\omega_0^2} \quad \left( \omega_0 = \sqrt{\frac{k}{m}} \right)$$



$$\frac{\xi_i^{SPD}}{\xi_i^{MPD}} = \frac{\frac{\bar{\beta}}{2} \omega_i}{\frac{\bar{\alpha}}{2\omega_i}} = \frac{\bar{\beta}}{\bar{\alpha}} \omega_i^2 = \frac{\omega_i^2}{\omega_0^2} = \dots$$



$$\frac{\xi_i^{SPD}}{\xi_i^{MPD}} = \frac{\frac{\bar{\beta}}{2} \omega_i}{\frac{\bar{\alpha}}{2\omega_i}} = \frac{\bar{\beta}}{\bar{\alpha}} \omega_i^2 = \frac{\omega_i^2}{\omega_0^2} = \Omega_i^2 = \Lambda_i$$



# Properties of MPD and SPD systems (4)

$$\frac{\xi_i^{SPD}}{\xi_i^{MPD}} = \frac{\frac{\bar{\beta}}{2} \omega_i}{\frac{\bar{\alpha}}{2\omega_i}} = \frac{\bar{\beta}}{\bar{\alpha}} \omega_i^2 = \frac{\omega_i^2}{\omega_0^2} = \Omega_i^2 = \Lambda_i \longrightarrow \text{eigenproblem}$$

The matrix  $\mathbf{A}_N = \frac{1}{\omega_0^2} \mathbf{k}_N \mathbf{m}_N^{-1} =$

$$\begin{bmatrix} 2 & -1 & 0 & \dots & & 0 \\ -1 & 2 & -1 & 0 & \dots & 0 \\ 0 & -1 & 2 & \dots & \dots & \dots \\ \dots & 0 & \dots & \dots & \dots & \dots \\ & & \dots & \dots & -1 & 0 \\ & & & & -1 & 2 & -1 \\ 0 & \dots & \dots & 0 & -1 & 1 \end{bmatrix}$$

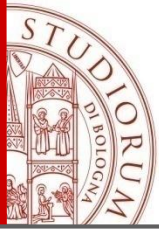
has eigenvalues  $\Lambda_i$

$$\text{if } \Lambda_i < 1 \Rightarrow \xi_i^{SPD} < \xi_i^{MPD}$$



The  $i$ -th damping ratio of the SPD system is less than the “corresponding” one of the MPD system (the two systems with same total damping)





# Properties of MPD and SPD systems (5)

► It can be demonstrated:

$$\frac{\xi_1^{SPD}}{\xi_1^{MPD}} = \Lambda_1 < 1$$

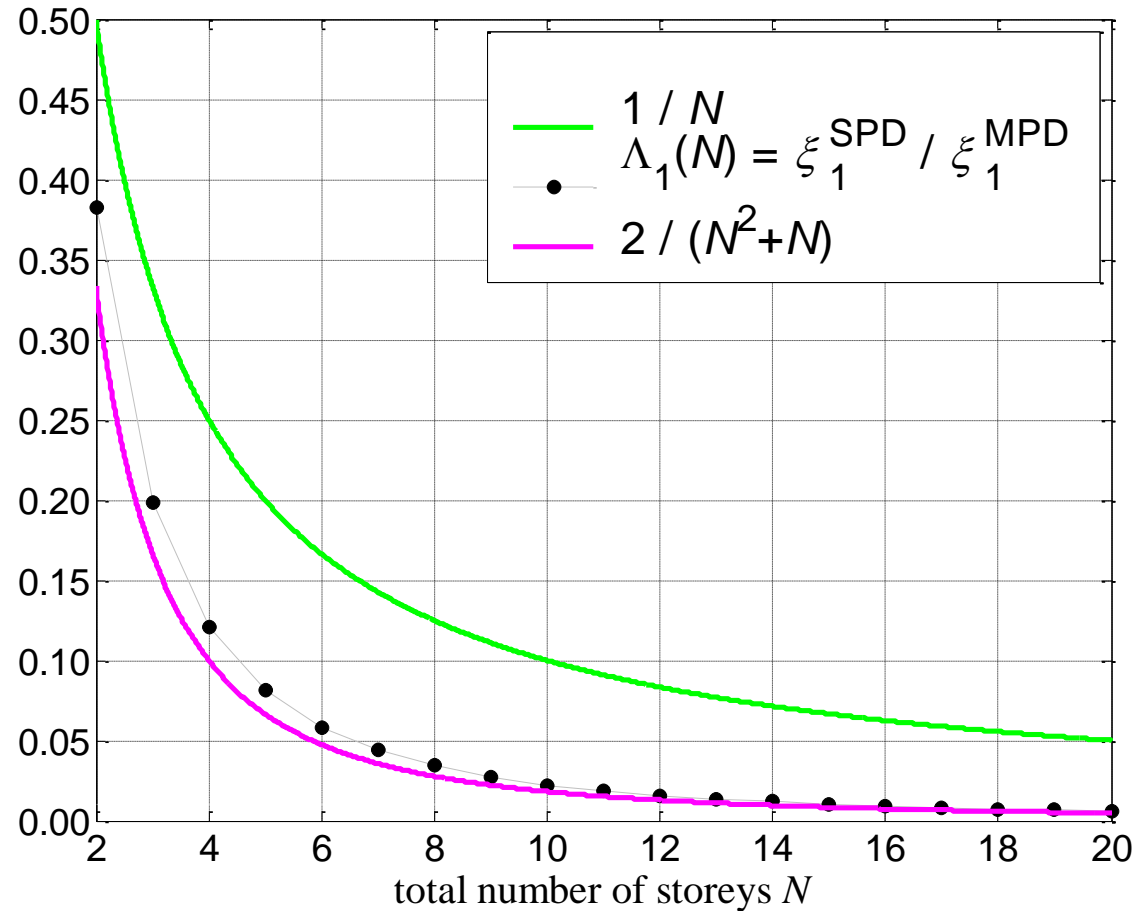
► Upper bound:

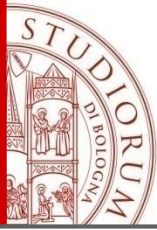
$$\frac{\xi_1^{SPD}}{\xi_1^{MPD}} < \frac{1}{N}$$

► Approximation:

$$\frac{\xi_1^{SPD}}{\xi_1^{MPD}} \cong \frac{2}{N(N+1)}$$

\*





# Properties of **MPD** and **SPD** systems (6)



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## On the modal damping ratios of shear-type structures equipped with Rayleigh damping systems

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Received 29 July 2002; received in revised form 6 July 2005; accepted 15 July 2005

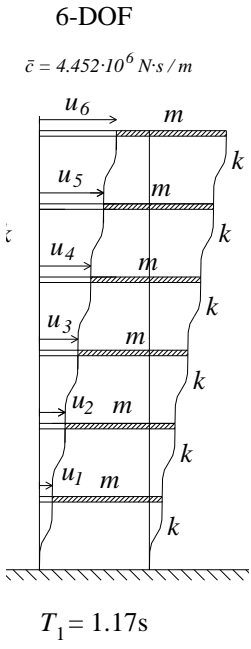
Available online 28 September 2005

### Abstract

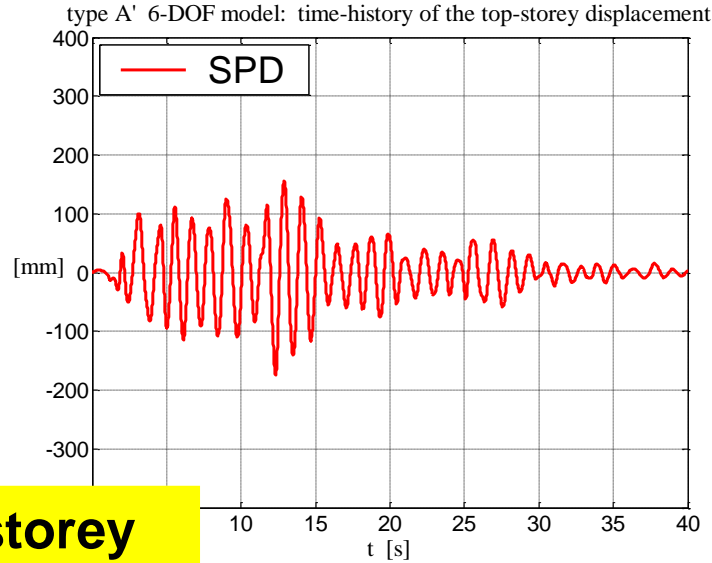
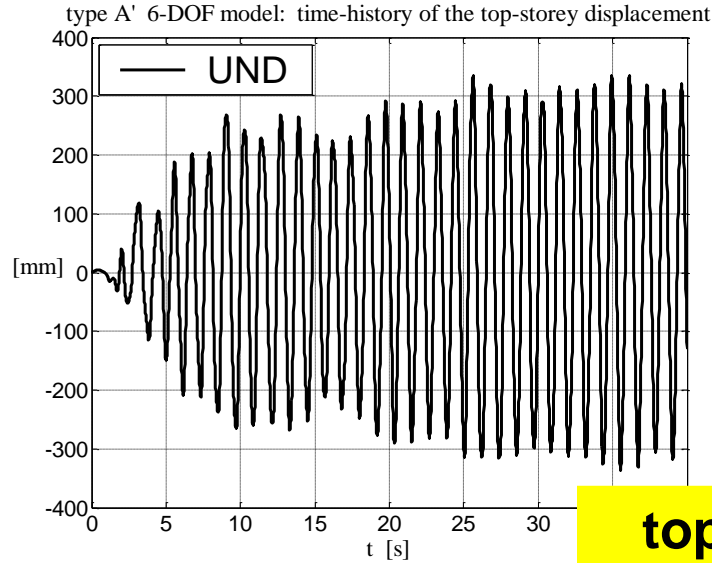
The effects of added manufactured viscous dampers upon shear-type structures are analytically investigated here for the class of Rayleigh damping systems. The definitions of mass proportional damping (MPD) and stiffness proportional damping (SPD) systems are briefly recalled and their physical counterpart is derived. From basic physics, a detailed mathematical demonstration that the first modal damping ratio of a structure equipped with the MPD system is always larger than the first modal damping ratio of a structure equipped with the SPD system is provided here. All results are derived for the class of structures characterised by constant values of lateral stiffness and storey mass, under the equal “total size” constraint. The paper also provides closed form demonstrations of other properties of modal damping



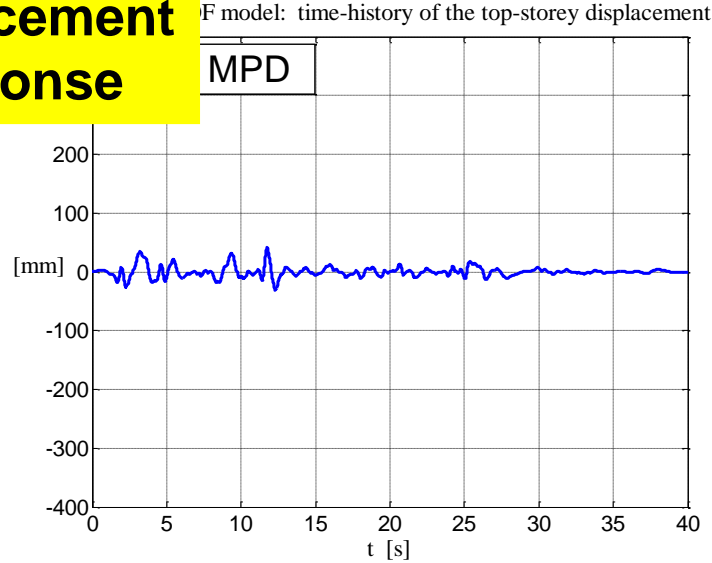
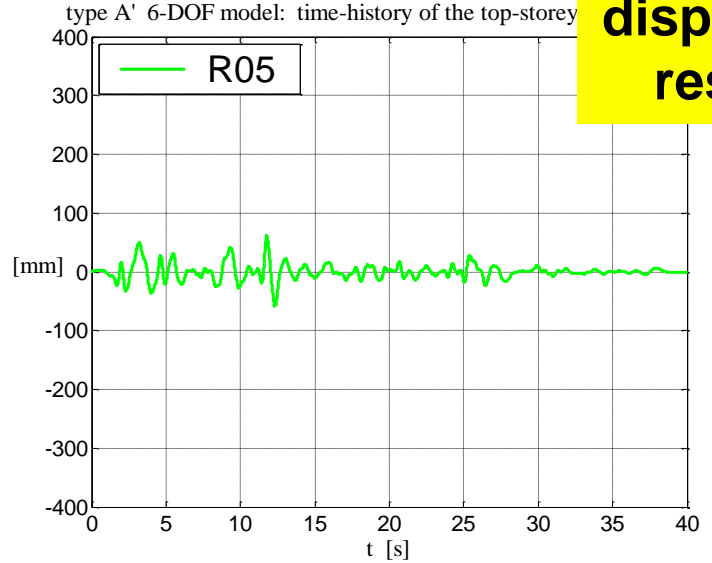
# Seismic response of **MPD** and **SPD** systems



El Centro 1940  
scaled to  
PGA = 0.3g



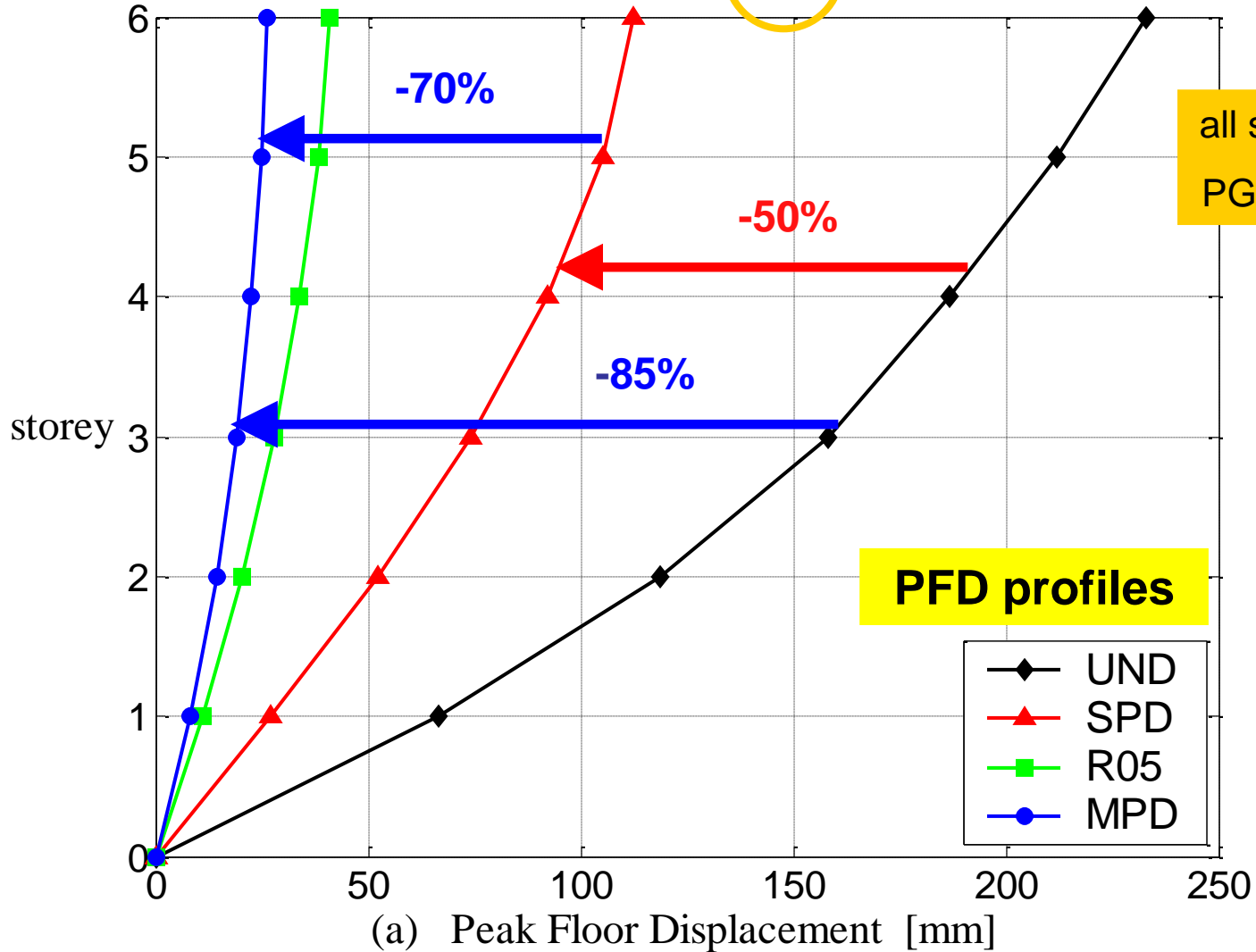
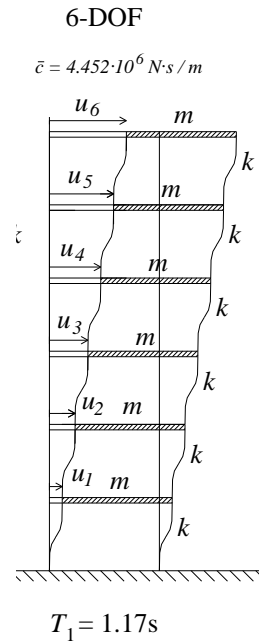
**top-storey displacement response**





# Seismic response of **MPD** and **SPD** systems

type A' 6-DOF model: averages over 40 earthquake ground motions



$\xi_{S_1}^{MPD} = 86\%$

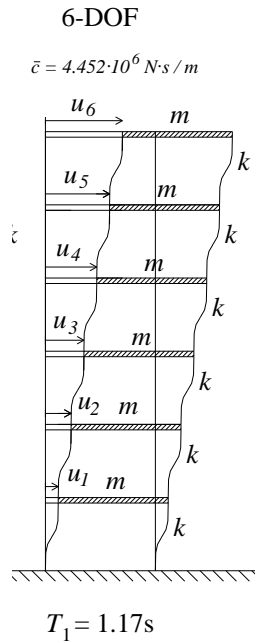
$\xi_{S_1}^{SPD} = 5\%$

$\xi_{S_2}^{MPD} = 29\%$

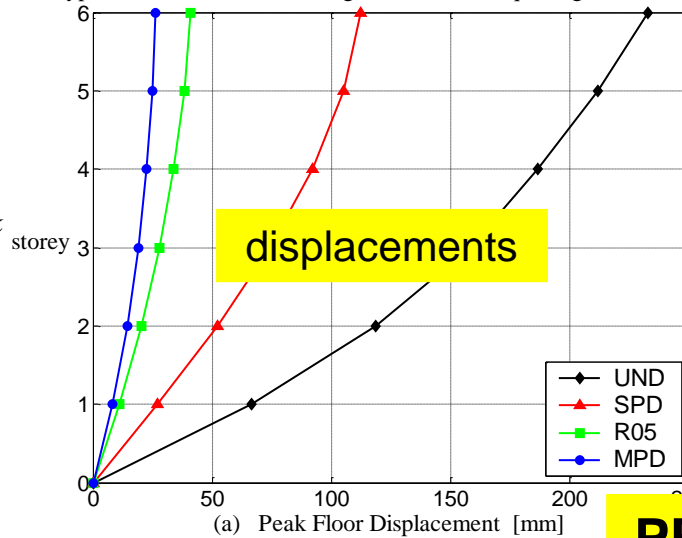
$\xi_{S_2}^{SPD} = 15\%$



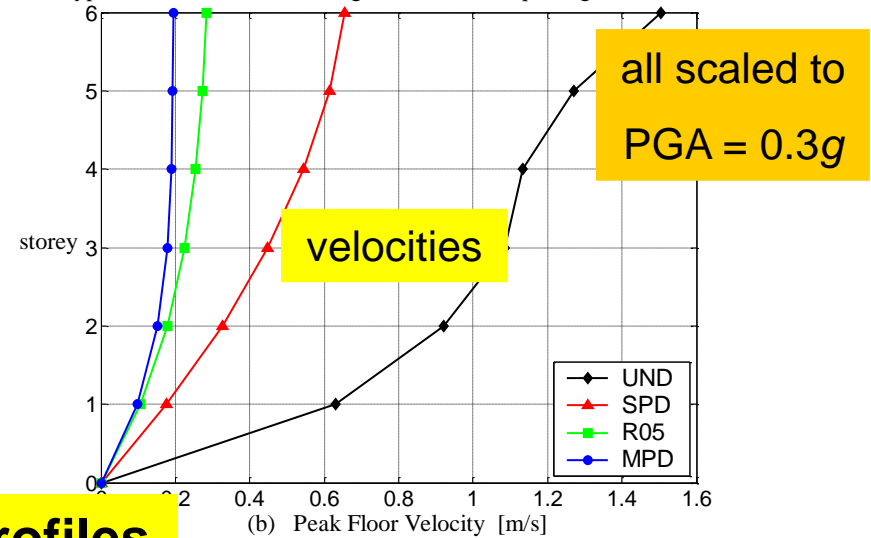
# Seismic response of **MPD** and **SPD** systems



type A' 6-DOF model: averages over 40 earthquake ground motions

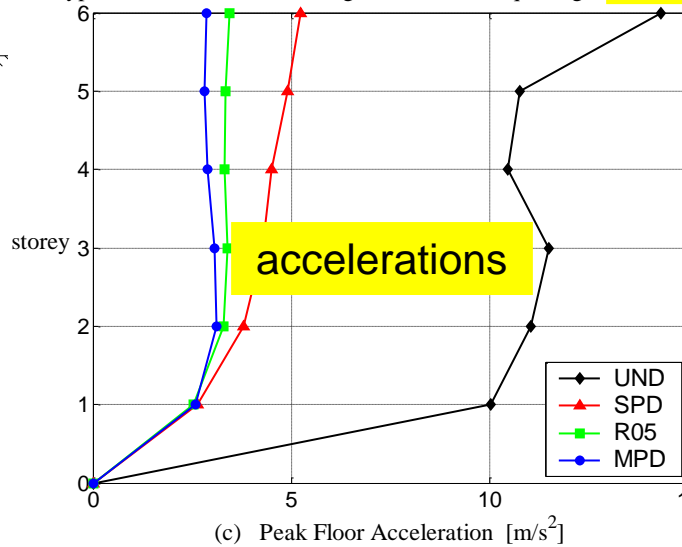


type A' 6-DOF model: averages over 40 earthquake ground motions

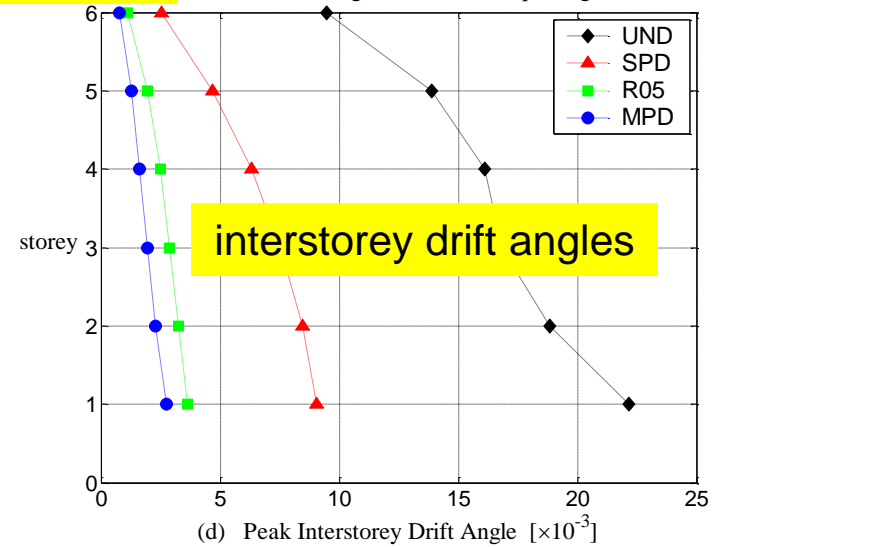


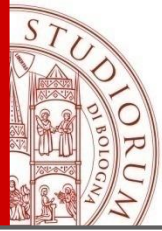
## PF profiles

type A' 6-DOF model: averages over 40 earthquake ground motions



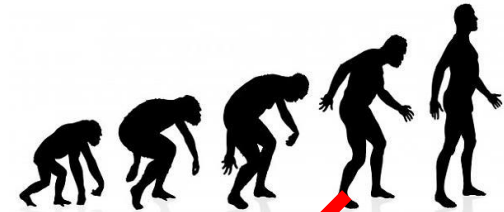
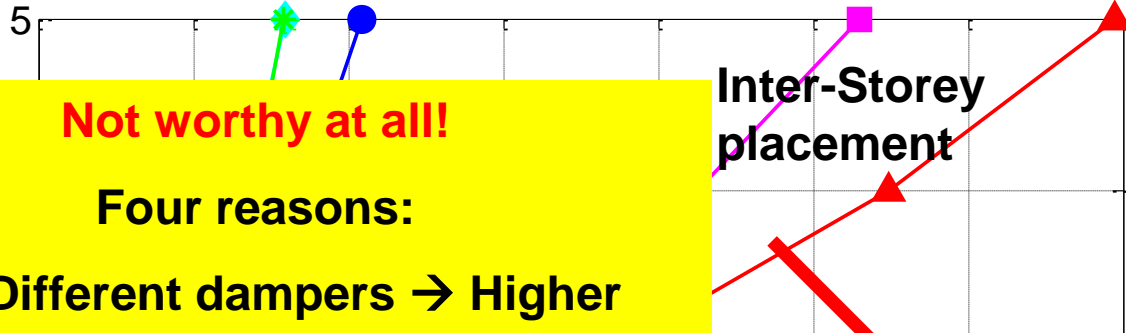
type A' 6-DOF model: averages over 40 earthquake ground motions





# Seismic response of Genetically Identified Optimal (GIO) systems

5-storey r.c. structure: averages over 40 earthquake ground motions

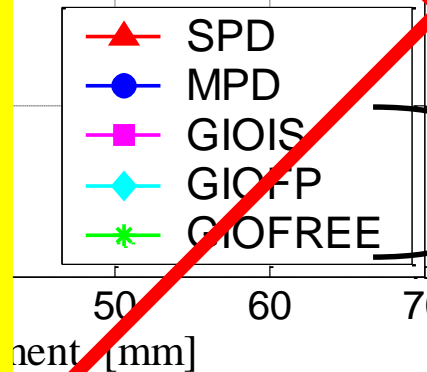
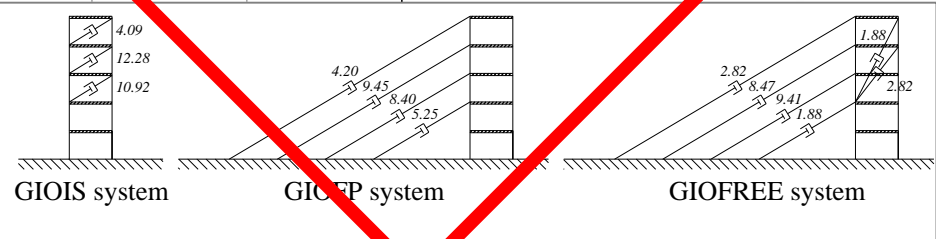


**Not worthy at all!**

**Four reasons:**

- 1) Different dampers → Higher manufacturing costs
- 2) Danger of numerically optimising only few response parameters and forgetting overall behaviour
- 3) Always look for uniformity and regularity in earthquake engineering!
- 4) Limited efficiency due to effects from «non-proportional» (complex) damping

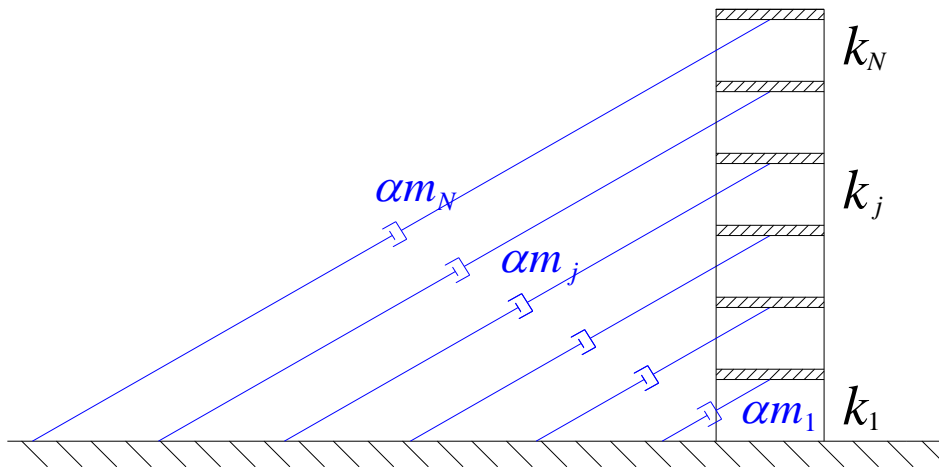
**Inter-Storey placement**



Objective function:  
average of the standard deviations of the interstorey drift angles

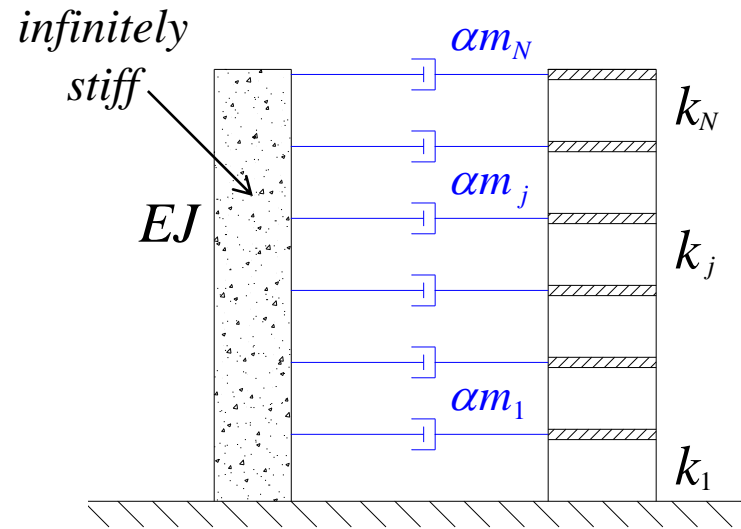


# Implementation of **MPD** systems



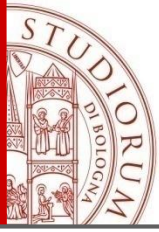
## DIRECT IMPLEMENTATION

Use of long buckling-resistant braces (unbonded braces, buckling-restrained-braces BRB, mega-braces, prestressed steel cables, ...)



## INDIRECT IMPLEMENTATION

Dampers placed between the structure and a **very stiff** vertical lateral-resistant element



# Indirect Implementation of **MPD** systems

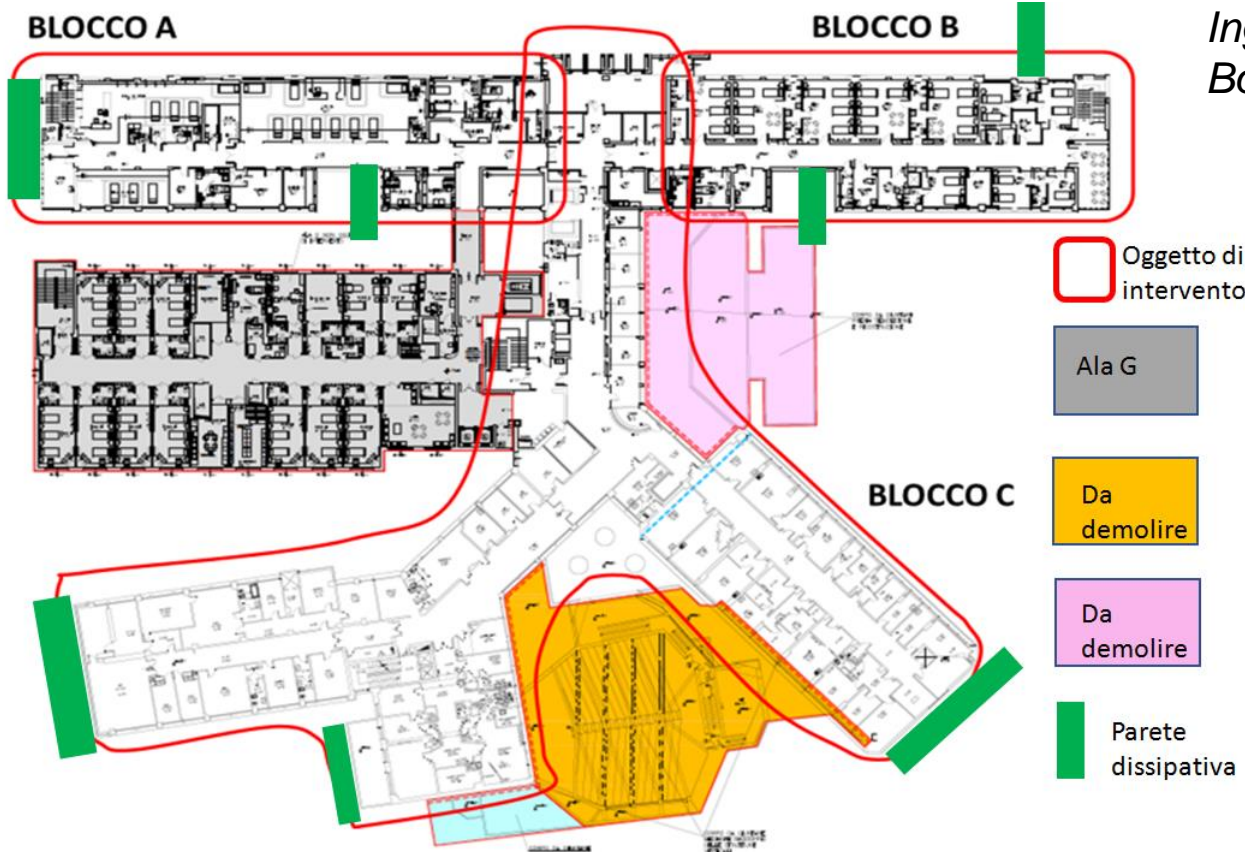
S.Orsola hospital, Bologna  
Pavilion n.5



# Indirect Implementation of **MPD** systems

S.Orsola hospital, Bologna  
Pavilion n.5

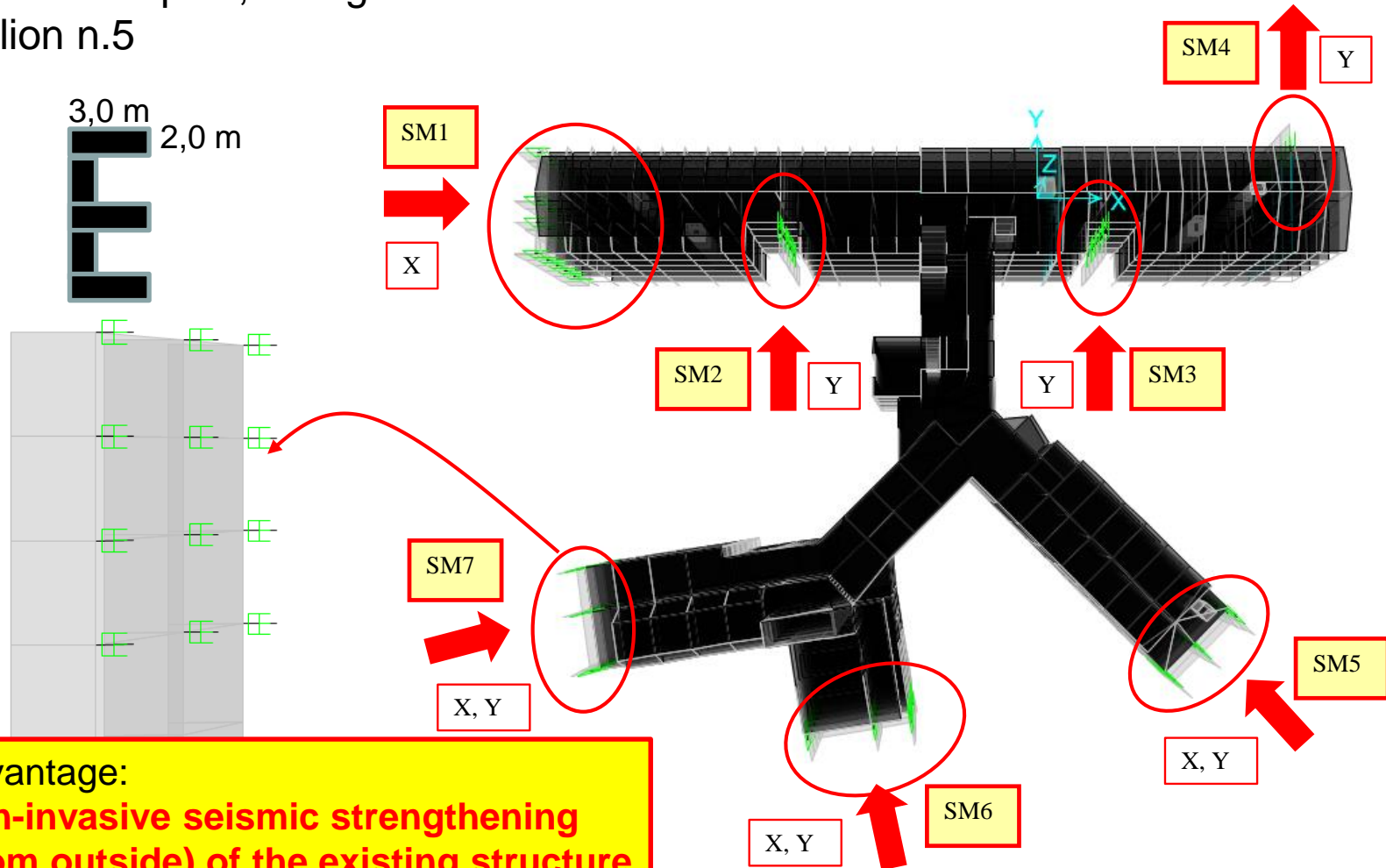
2020-2021  
executive design by:  
Prof. Ing. Tomaso Trombetti  
Ing. Friedrich Drollmann  
Bologna



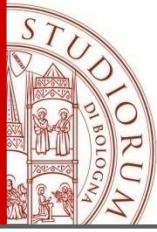


# Indirect Implementation of **MPD** systems

S.Orsola hospital, Bologna  
Pavilion n.5



advantage:  
**non-invasive seismic strengthening  
(from outside) of the existing structure**



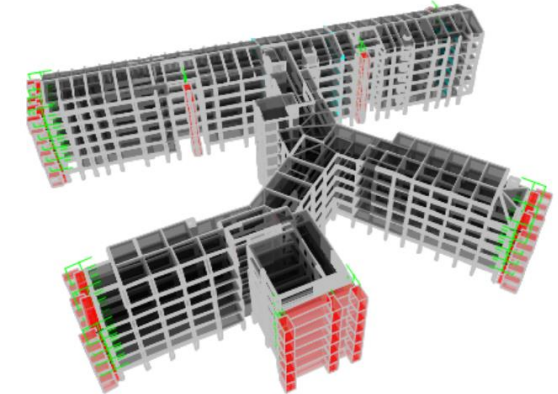
# Indirect Implementation of **MPD** systems

S.Orsola hospital, Bologna  
Pavilion n.5

*Caratteristiche di progetto*

		OTP 68/100	OTP 90/120	OTP 120/150
Quantità		21	12	44
Costante di smorzamento	C	800 kN/(m/s) <sup>α</sup>	1000 kN/(m/s) <sup>α</sup>	1250 kN/(m/s) <sup>α</sup>
Velocità massima	v	0,322 m/s	0,465 m/s	0,762 m/s
Esponente di smorzamento	α	0,15	0,15	0,15
Forza di progetto	F <sub>d</sub>	680 kN	900 kN	1200 kN
Spostamento sismico (SLV)	d <sub>sa</sub>	±23 mm	±29 mm	±36 mm
Scorrimento totale	d <sub>es</sub>	±50 mm	±60 mm	±75 mm
Lunghezza perno-perno	L	1000 +/-50	1110 +/-60	1200 +/-75
Diametro cilindro	øD	ø225		
Dimensione struttura	A	310		
Dimensione struttura	B	310		
Dimensione struttura	E	165		

tot.  
77



**NOTE**

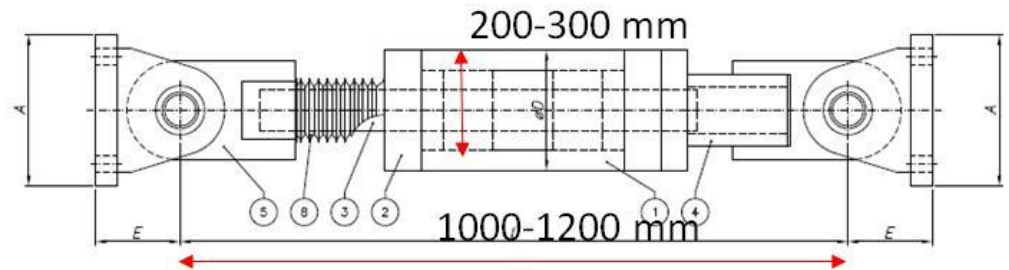
- Viti/barre di ancoraggio (min classe 8.8 ISO898) non sono comprese r
- La geometria indicata consente il montaggio del dispositivo e la rotazi
- La tolleranza di installazione consentita sulla lunghezza è ±5 mm.

**PROTEZIONE DALLA CORROSIONE**

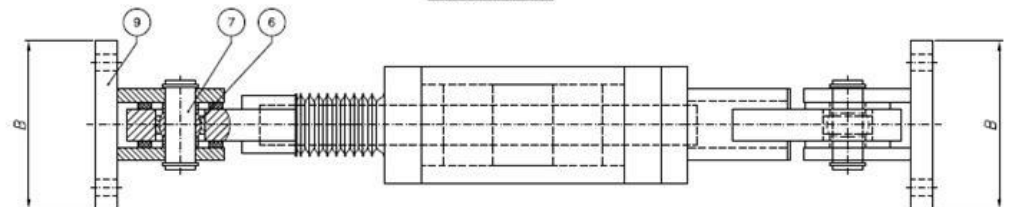
Superficie esterne:

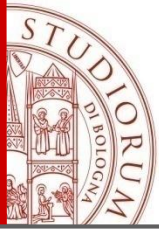
- strato epossì-ammino ciclo-alifatico: 280-350 μm, RAL7035

*Vista laterale*



*Vista dall'alto*

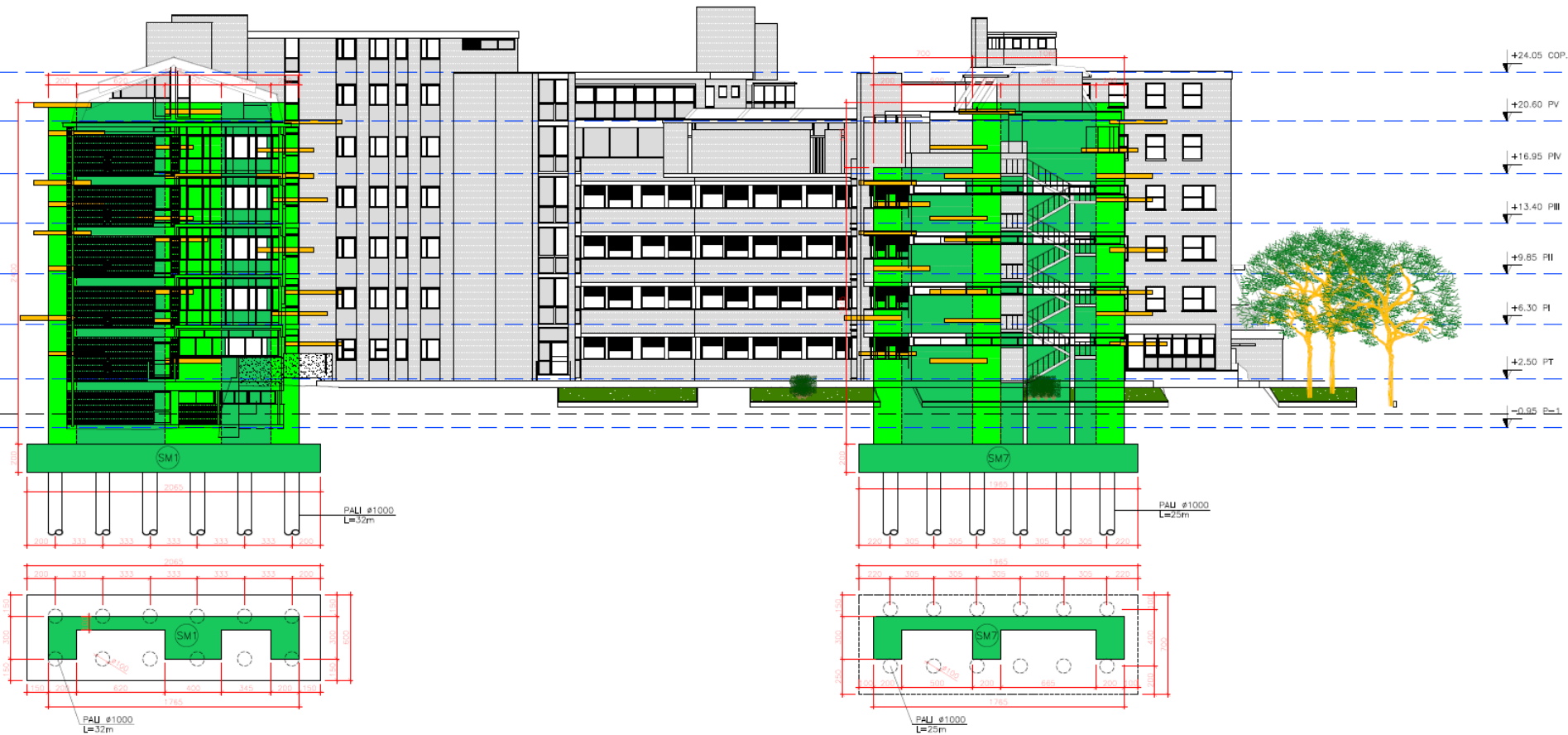




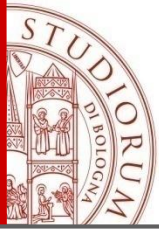
# Indirect Implementation of **MPD** systems

S.Orsola hospital, Bologna  
Pavilion n.5

## PROSPETTO SUD - EST





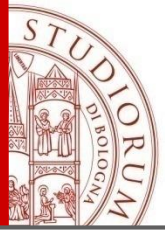


# Indirect Implementation of **MPD** systems

S.Orsola hospital, Bologna  
Pavilion n.5

PROSPETTO SUD - EST



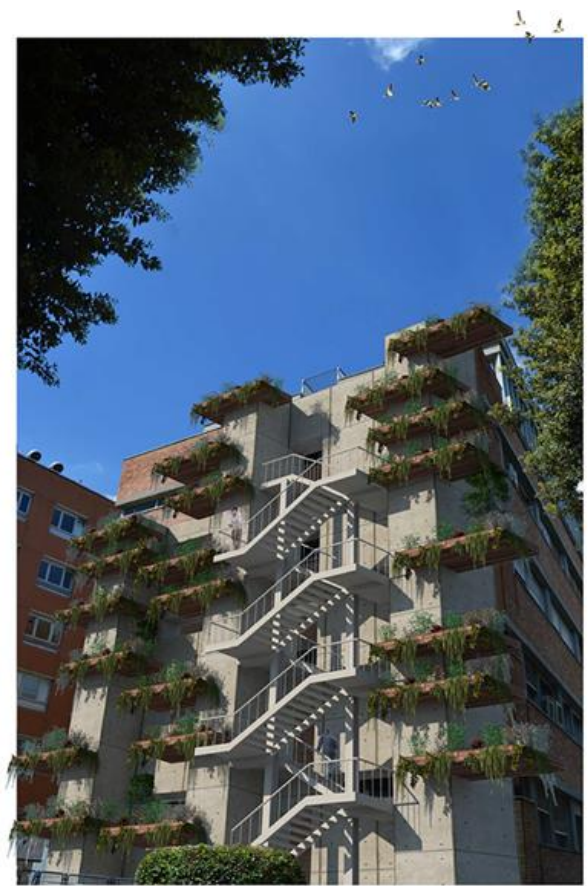


# Indirect Implementation of **MPD** systems

S.Orsola hospital, Bologna  
Pavilion n.5



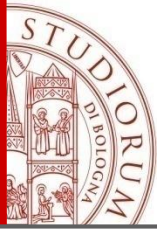
VISTA 1



VISTA 2



VISTA 3



# Properties of **MPD** and **SPD** systems (7)

$$\underline{\mathbf{c}} = \alpha \underline{\mathbf{m}}$$

$$\xi_1^{MPD} = \frac{\alpha}{2\omega_1} \quad \alpha = 2 \cdot \xi_1^{MPD} \cdot \omega_1$$

$$\underline{\mathbf{c}} = 2 \cdot \xi_1^{MPD} \cdot \omega_1 \cdot \underline{\mathbf{m}}$$

$$c_{storey,j} = 2 \cdot \xi_1^{MPD} \cdot \omega_1 \cdot m_j$$

$m_j$  is easy to be calculated

$$c_{tot,MPD} = 2 \cdot \xi_1^{MPD} \cdot \omega_1 \cdot m_{tot}$$

$$\underline{\mathbf{c}} = \beta \underline{\mathbf{k}}$$

$$\xi_1^{SPD} = \frac{\beta\omega_1}{2} \quad \beta = \frac{2 \cdot \xi_1^{SPD}}{\omega_1}$$

$$\underline{\mathbf{c}} = \frac{2 \cdot \xi_1^{SPD}}{\omega_1} \cdot \underline{\mathbf{k}}$$

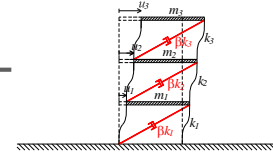
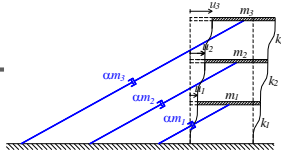
$$c_{storey,j} = \frac{2 \cdot \xi_1^{SPD}}{\omega_1} \cdot k_j$$

$k_j$  is not so immediate ...

$$c_{tot,SPD} = \dots$$



# Properties of MPD and SPD systems (8)



$$C_{tot,MPD} = 2 \cdot \xi_1^{MPD} \cdot \omega_1 \cdot m_{tot}$$

$$C_{tot,SPD} = \xi_1^{SPD} \cdot \omega_1 \cdot m_{tot} \cdot N(N+1)$$

$$\xi_1^{MPD} = \frac{C_{tot}}{2 \cdot \omega_1 \cdot m_{tot}}$$

$$\xi_1^{SPD} = \frac{C_{tot}}{2 \cdot \omega_1 \cdot m_{tot}} \cdot \frac{2}{N(N+1)}$$

$$\xi_1^{SPD} \frac{N(N+1)}{2} = \frac{C_{tot}}{2 \cdot \omega_1 \cdot m_{tot}}$$

\*

$$\frac{\xi_1^{SPD}}{\xi_1^{MPD}} \approx \frac{2}{N(N+1)}$$

$$\xi_1^{MPD} \approx \xi_1^{SPD} \frac{N(N+1)}{2}$$



# Fundamental design formulas

If a target damping ratio is looked for:  
the **fundamental results** are:

$$\xi_1^{SPD} = \bar{\xi}$$

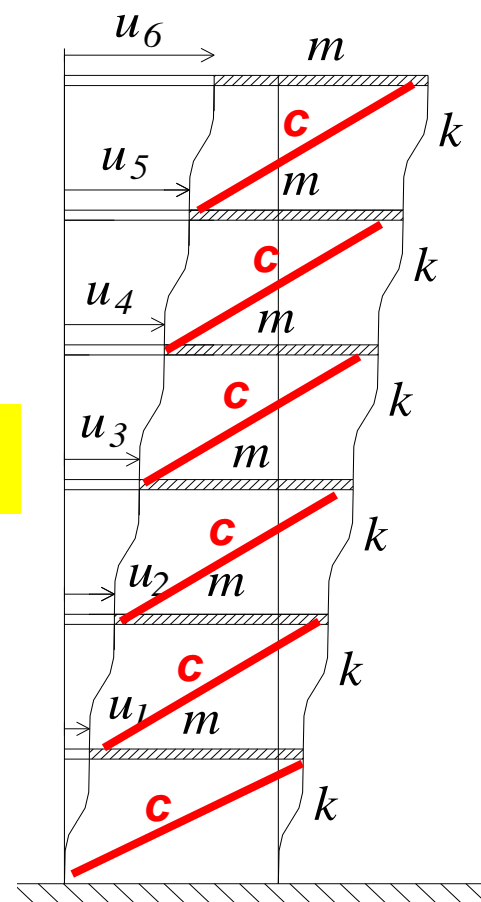
$$C_{tot,SPD} = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot N(N+1)$$

$$C_{storey,SPD} = \frac{C_{tot,SPD}}{N} = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot (N+1)$$

\*\*

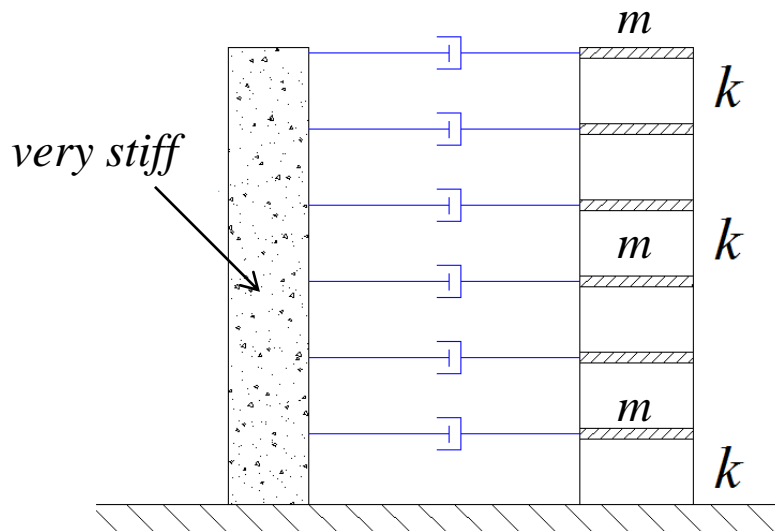
The above equations allow to size the damping coefficients of each damper of an inter-storey dampers system, in order to get a target damping ratio  $\bar{\xi}$ , by **simply knowing:**

- the total mass  $m_{tot}$
- the fundamental period of vibration  $T_1$  ( $\omega_1 = \frac{2\pi}{T_1}$ )
- the total number of storeys  $N$



# Fundamental design formulas

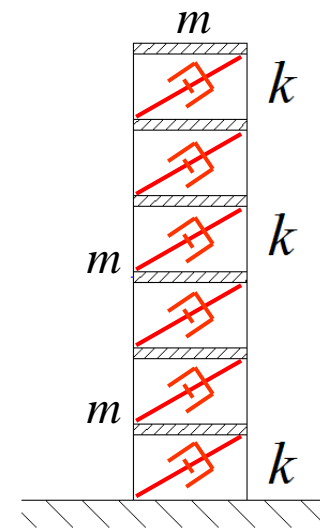
**MPD system**



$$C_{tot,MPD} = 2 \cdot \bar{\xi} \cdot \omega_1 \cdot m_{tot}$$

$$C_{storey,MPD} = \frac{2 \cdot \bar{\xi} \cdot \omega_1 \cdot m_{tot}}{N}$$

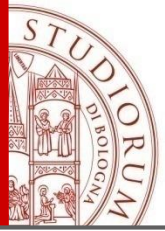
**SPD system**



$$C_{tot,SPD} = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot N(N+1)$$

$$C_{storey,SPD} = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot (N+1) \quad **$$

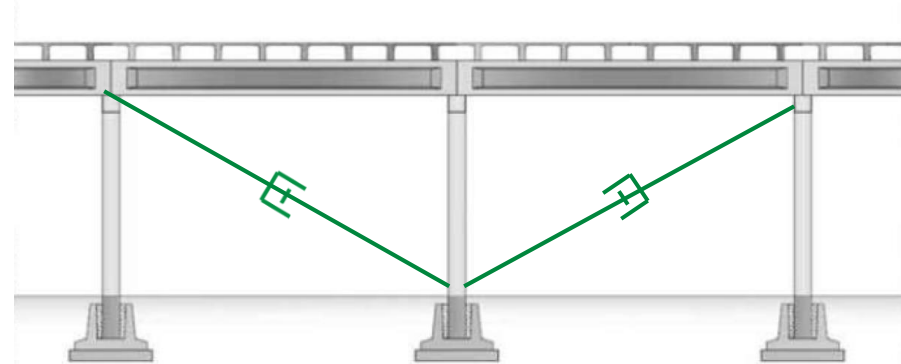
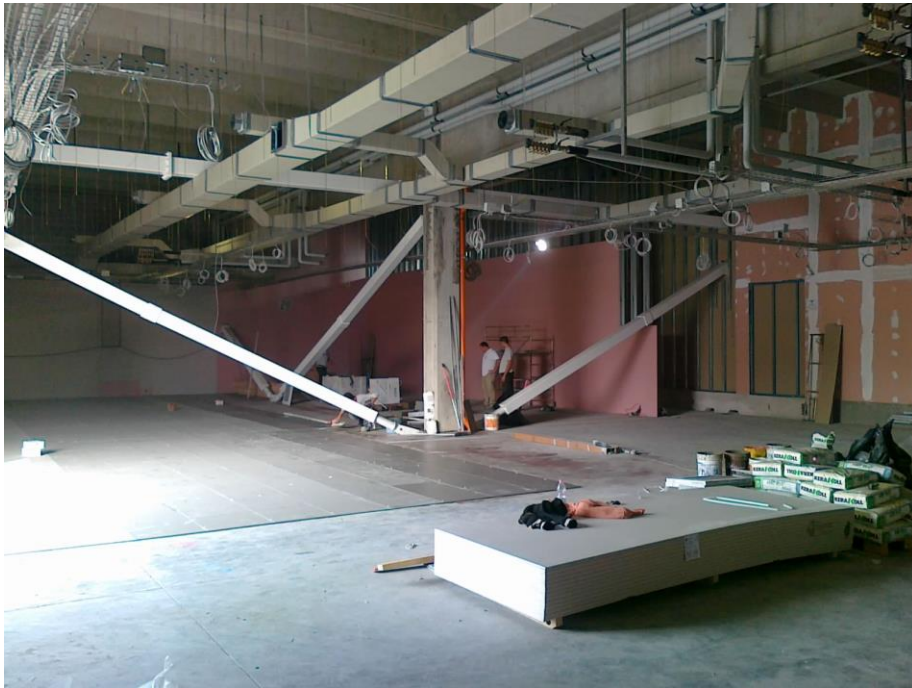




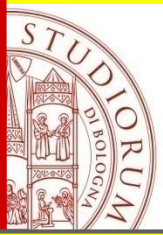
# One-storey buildings: SDOF systems

**MPD** system  $\equiv$  **SPD** system

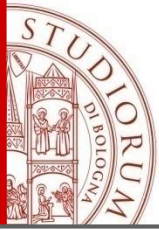
$$C_{tot,MPD} = C_{tot,SPD} = 2 \cdot \bar{\xi} \cdot \omega_1 \cdot m_{tot}$$



*HERA building,  
Imola (BO)*



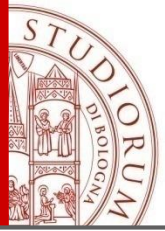
# The five-step procedure (2010)



# Design strategy

- The design philosophy is **to limit the structural damages** under severe earthquakes.
- The structural elements (columns and beams) should remain **in the elastic phase**.
- Let's keep the **ductility resources** of columns and beams **as an additional property** to withstand very severe and unexpected earthquakes.

# The five-step procedure for **inter-storey** dampers placement



DESIGN PROCESS

STEP 1: performance objectives



$$\bar{\eta} \rightarrow \bar{\xi}$$

$$\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}}}$$

STEP 2: linear dampers



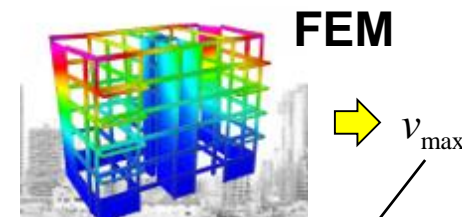
$$\bar{\xi} \rightarrow \bar{c}_L$$

$$\bar{c}_L = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot \left( \frac{N+1}{n} \right)$$

STEP 3: linear TH analyses



structural response



FEM

$v_{max}$

STEP 4: non-linear dampers



$$\bar{c}_L \rightarrow \begin{cases} \bar{c}_{NL} \\ \bar{\alpha} \\ \bar{k}_{oil} \end{cases}$$

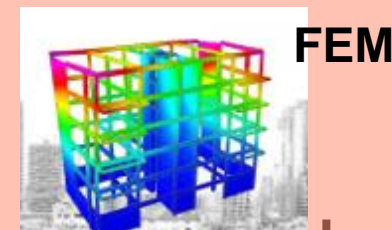
$$\bar{c}_{NL} = \bar{c}_L \cdot (\chi \cdot v_{max})^{1-\bar{\alpha}}$$

VERIFICATION

STEP 5: non-linear TH analyses



structural response



FEM



# The five-step procedure for inter-storey dampers placement

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ISSN: 1363-2469 print / 1559-808X online  
DOI: 10.1080/13632460903093891



## A Five-Step Procedure for the Dimensioning of Viscous Dampers to Be Inserted in Building Structures

STEFANO SILVESTRI, GIADA GASPARINI,  
and TOMASO TROMBETTI

Department DISTART, University of Bologna, Bologna, Italy

*Viscous dampers have widely proved their effectiveness in mitigating the effects of the seismic action upon building structures. In view of the large impact that use of such dissipative devices is already having and would most likely have soon in earthquake engineering applications, this article presents a practical procedure for the seismic design of building structures equipped with viscous dampers, which aims at providing practical tools for an easy identification of the mechanical characteristics of the manufactured viscous dampers which allow to achieve target levels of performances. Selected numerical applications are developed with reference to simple, but yet relevant, cases.*

**Keywords** Added Viscous Dampers; Seismic Design; Design Procedure; Nonlinear Modeling; Damping Ratio

# Starting point

 $\bar{\eta}$ 

$$\bar{\eta} = \frac{V_{base,\xi}}{V_{base,\xi=5\%}}$$

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}}$$

$$\bar{\eta} = \frac{\delta_{top-storey,\xi}}{\delta_{top-storey,\xi=5\%}}$$

## EXAMPLE:

If the bending moment action at the base of a column is  $M_{Ed,\xi=5\%} = 800$  kNm and if the bending moment resistance is  $M_{Rd} = 400$  kNm

then

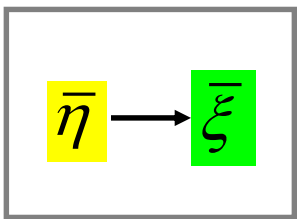
we want that dampers lead to  $M_{Ed,\xi} = 400$  kNm

$$\bar{\eta} = \frac{400}{800} = 0.5$$

$$\bar{\eta} = \frac{\text{target seismic demand (i.e. capacity/strength or acceptable action or drift)}}{\text{actual seismic demand with no dampers}}$$

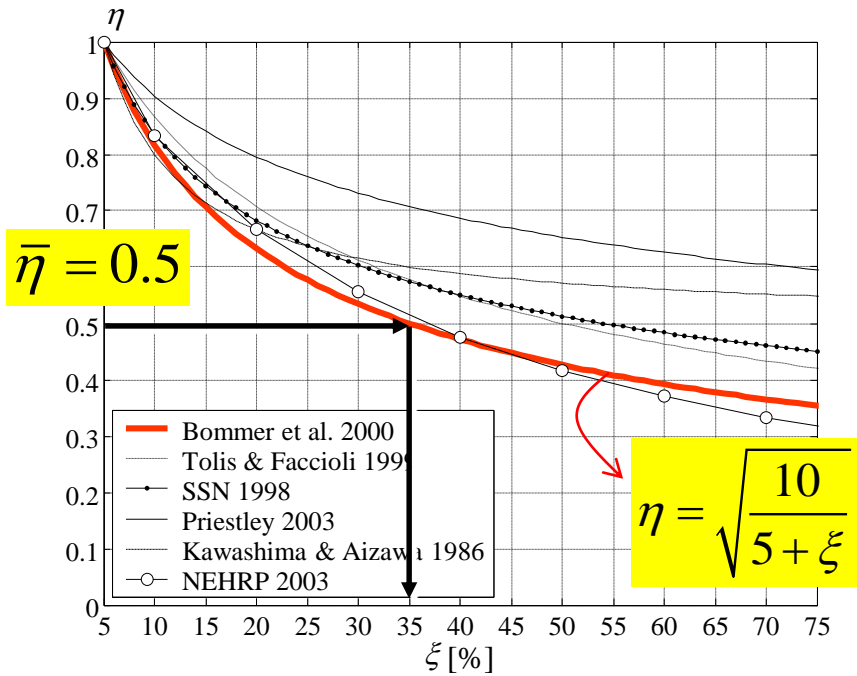


# Step 1

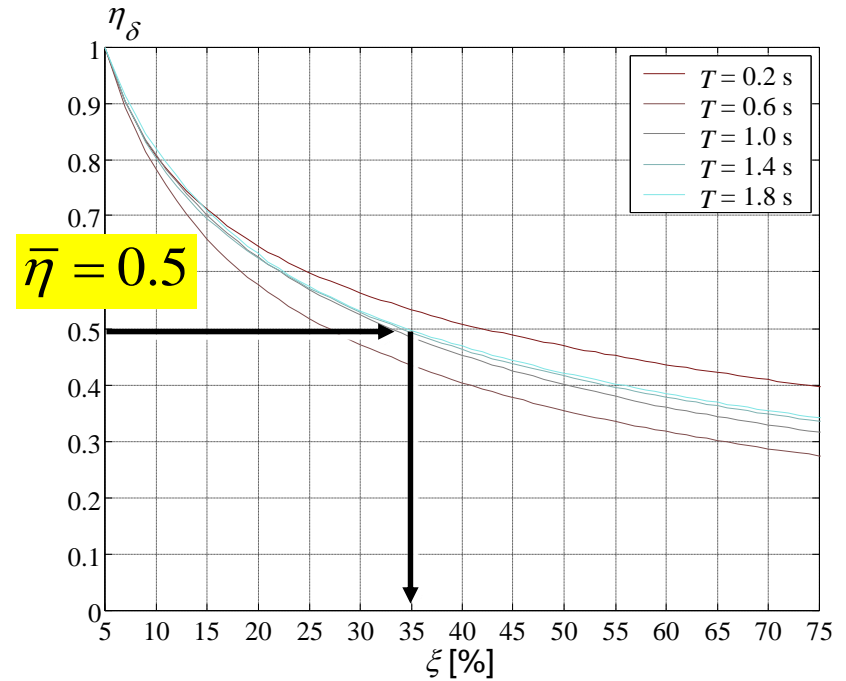


Some available formulations to relate  $\bar{\eta} \longrightarrow \bar{\xi}$

Cardone, Dolce, Rivelli (ANIDIS 2007)

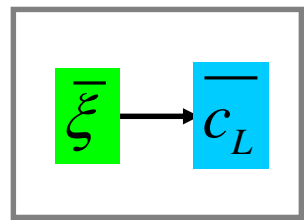


mean SDOF response from T-H analyses



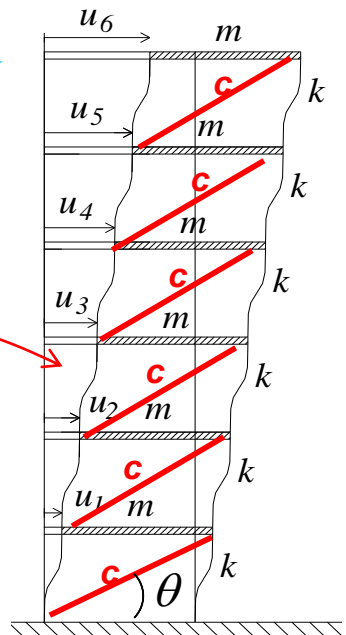
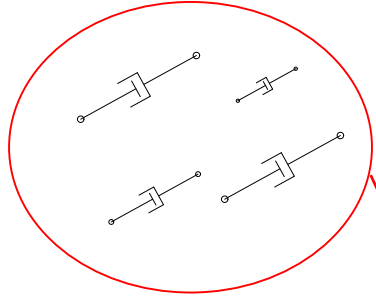
$$\bar{\xi} = \frac{10}{\bar{\eta} - 5}$$

# Step 2



Preliminary sizing of linear viscous damper using analytical formula \*\*

$$\left. \begin{array}{l} c_L \\ \alpha = 1 \\ k_{oil} = \infty \end{array} \right\}$$



$$c_L = \xi \cdot \omega_1 \cdot m_{tot} \cdot \frac{(N+1)}{n}$$

\*\*

$$c_{L,inclined} = c_{L,horizontal} \cdot \left( \frac{1}{\cos^2 \theta} \right)$$

$n$  = number of dampers at a given storey in a given direction

# Step 3

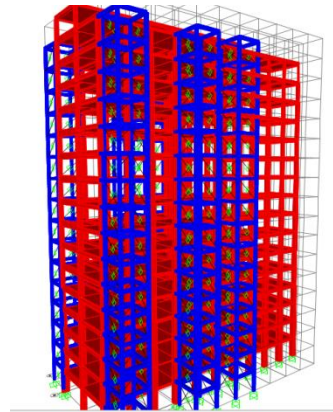
FEM  
simulations

After linear viscous dampers are dimensioned

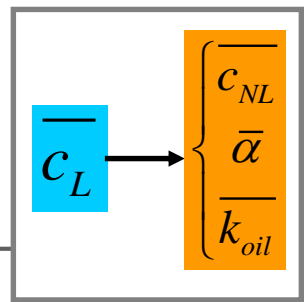
$$c_L = \bar{c}_L \quad , \quad \alpha = 1 \quad , \quad k_{oil} = \infty$$

**Linear TH dynamic analyses are necessary in order to:**

1. Verify by means of **snap-back tests** that the actual damping properties of the model are in line with the expected ones (e.g. **target damping ratio is achieved**)  $\bar{\xi}$
2. Calculate the **maximum working velocities of the linear dampers**  $v_{max}$
3. Calculate **the maximum damper piston-strokes**  $x_{max}$



# Step 4



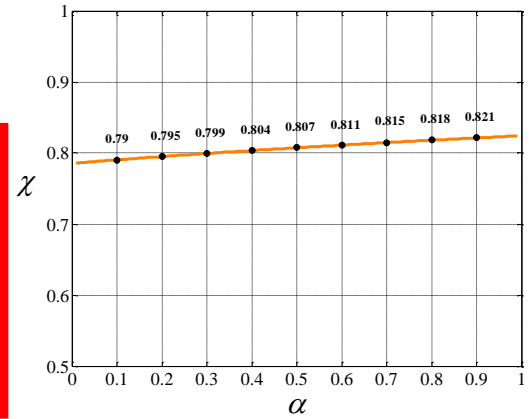
## ENERGETIC APPROACH:

equal energy dissipated over a full cycle of harmonic motion

$$\overline{E_{d,L}} = \overline{E_{d,NL}}$$

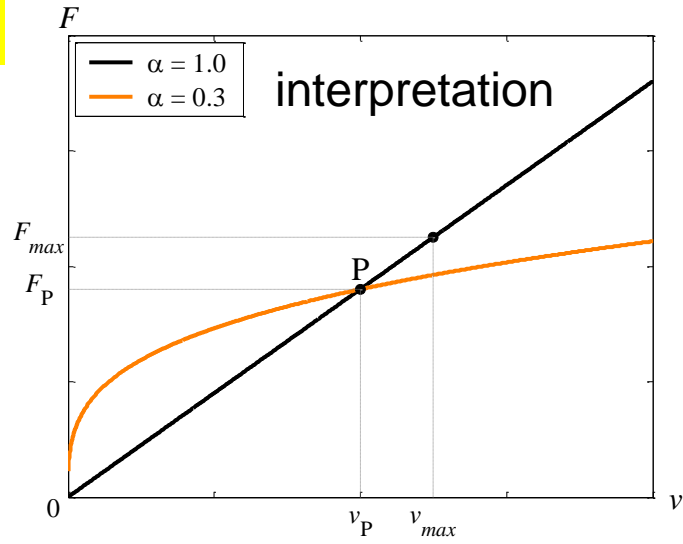


$$\begin{aligned} \overline{c_{NL}} &= \overline{c_L} \cdot (v_{\max})^{1-\overline{\alpha}} \cdot \chi = \\ &= \overline{c_L} \cdot (\chi \cdot v_{\max})^{1-\overline{\alpha}} \cdot \chi^{\overline{\alpha}} \\ &\cong \overline{c_L} \cdot (\chi \cdot v_{\max})^{1-\overline{\alpha}} \cdot 0.8^{0.15} = \overline{c_L} \cdot (\chi \cdot v_{\max})^{1-\overline{\alpha}} \end{aligned}$$



## REFERENCE POINT P:

$$\begin{aligned} v_P &= 0.8 \cdot v_{\max} \\ F_P &= 0.8 \cdot \overline{c_L} \cdot v_{\max} \end{aligned}$$



$$\chi = \left( \frac{\sqrt{\pi}}{2} \frac{\Gamma\left(\frac{\overline{\alpha}+3}{2}\right)}{\Gamma\left(\frac{\overline{\alpha}+2}{2}\right)} \right)^{\frac{1}{1-\overline{\alpha}}} \cong 0.8, \quad \forall \alpha$$

$$\begin{aligned} \overline{\alpha} &= 0.15 \\ \overline{k_{oil}} &\geq 10 \cdot \frac{F_{\max}}{x_{\max}} \cong 10 \cdot \overline{c_L} \cdot \omega_1 \end{aligned}$$

# Step 5

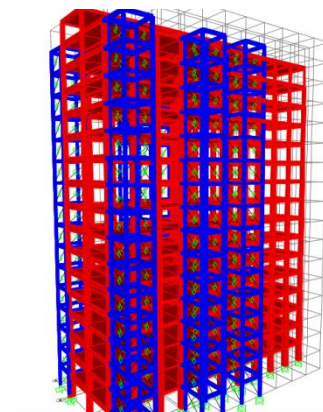
FEM  
simulations

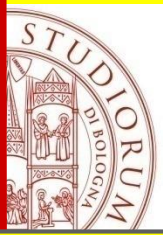
After non-linear viscous dampers are dimensioned

$$c_{NL} = \overline{c_{NL}} \quad , \quad \alpha = \overline{\alpha} \quad , \quad k_{oil} = \overline{k_{oil}} \geq 10 \cdot \overline{c_L} \cdot \omega_1$$

Non-linear TH dynamic analyses are necessary in order to:

1. Verify the effectiveness of the non-linear dampers in reducing the global structural response (e.g. **target damping ratio is achieved, maximum forces in the structural elements are acceptable**)
2. Evaluate the **maximum damper forces in the non-linear dampers**
3. Evaluate **the maximum strokes in the non-linear dampers**





# The direct five-step procedure (2016-2018)

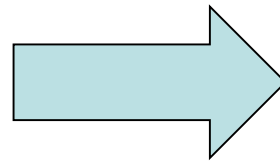
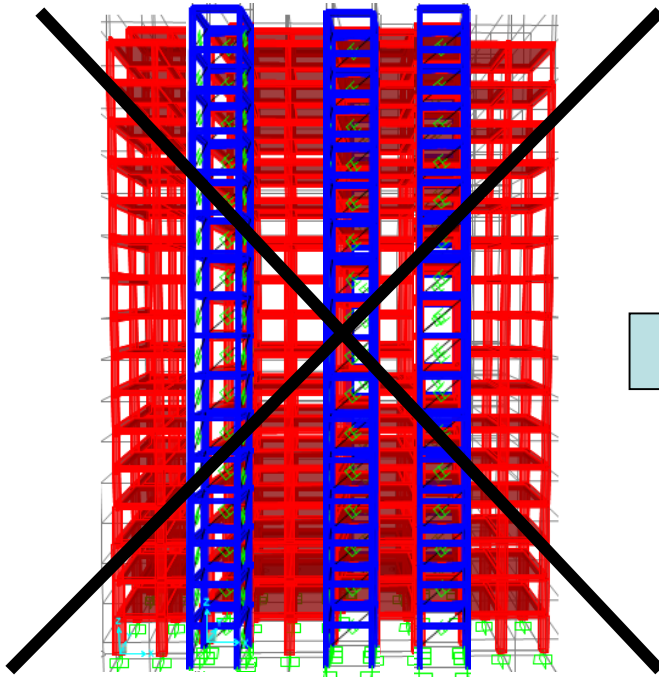




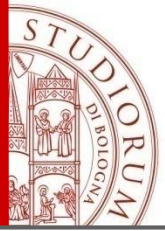
# A step forward: a direct five-step procedure

## The challenge:

Can we directly design (at least PRELIMINARY SIZING) the viscous dampers and the frames without performing TH dynamic analyses?



# The five-step procedure for inter-storey dampers placement



STEP 1: performance objectives



$$\bar{\eta} \rightarrow \bar{\xi}$$

$$\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}}}$$

STEP 2: linear dampers



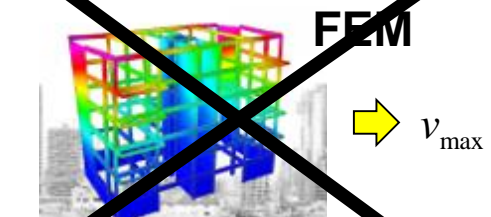
$$\bar{\xi} \rightarrow \bar{c}_L$$

$$\bar{c}_L = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot \left( \frac{N+1}{n} \right)$$

STEP 3: linear TH analyses



structural response



STEP 4: non-linear dampers



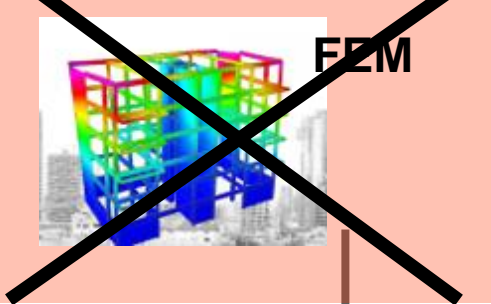
$$\bar{c}_L \rightarrow \begin{cases} \bar{c}_{NL} \\ \bar{\alpha} \\ \bar{k}_{oil} \end{cases}$$

$$\bar{c}_{NL} = \bar{c}_L \cdot (\chi \cdot v_{max})^{1-\bar{\alpha}}$$

STEP 5: non-linear TH analyses



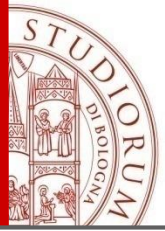
structural response



DESIGN PROCESS

VERIFICATION

# The five-step procedure for inter-storey dampers placement



DESIGN PROCESS

VERIFICATION

STEP 1: performance objectives



$$\bar{\eta} \rightarrow \bar{\xi}$$

$$\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}}}$$

STEP 2: linear dampers




$$\bar{\xi} \rightarrow \bar{c}_L$$

$$\bar{c}_L = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot \left( \frac{N+1}{n} \right)$$

STEP 3: linear TH analyses



structural response



**1. Estimation of inter-storey velocities**

STEP 4: non-linear dampers




$$\bar{c}_L \rightarrow \begin{cases} \bar{c}_{NL} \\ \bar{\alpha} \\ \bar{k}_{oil} \end{cases}$$

$$\bar{c}_{NL} = \bar{c}_L \cdot (\chi \cdot v_{max})^{1-\bar{\alpha}}$$

STEP 5: non-linear TH analyses



structural response

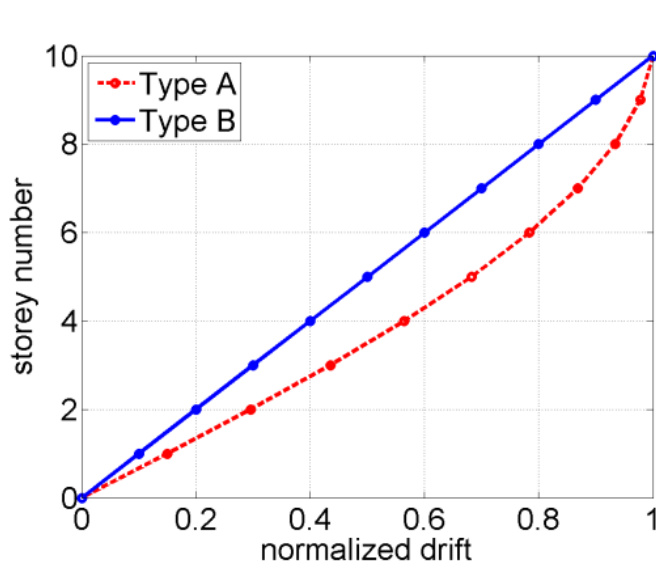


**2. Equivalent Static Analysis (ESA)**



# 1. Inter-storey velocities and damper forces

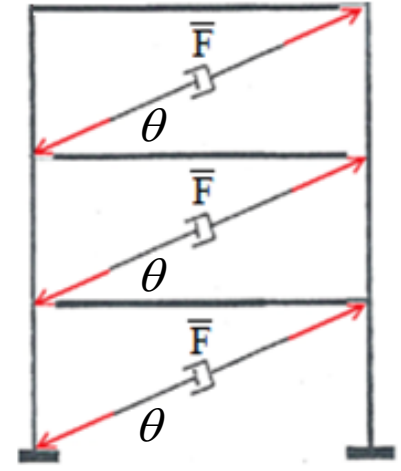
## Analytical Estimations Based On First Mode Response



storey displ.



interstorey drift



$$\delta_{\max} = \frac{S_{e,\xi}(T_1)}{\omega_1^2} \cdot \frac{2}{(N+1)}$$

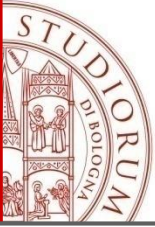
$$v_{\max} = \frac{S_{e,\xi}(T_1)}{\omega_1} \cdot \frac{2}{(N+1)} \cdot \cos \theta$$

$$F_{D\max} = \frac{2 \cdot \xi \cdot m_{tot} \cdot S_{e,\xi}(T_1)}{\cos \theta}$$

$$\delta_{\max} = \frac{S_{e,\xi}(T_1)}{\omega_1^2} \cdot \frac{12N}{(2+5N+5N^2)}$$

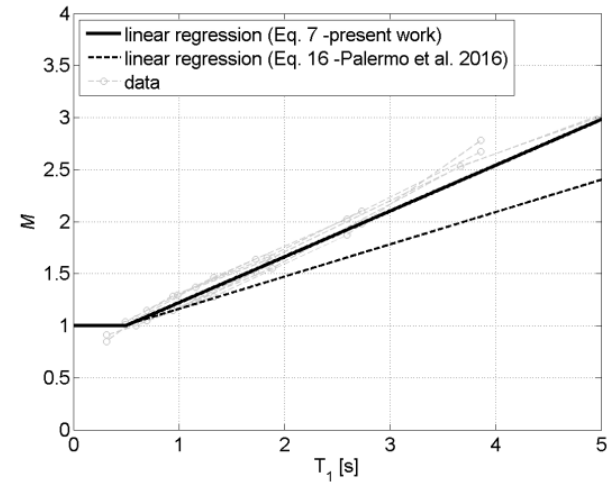
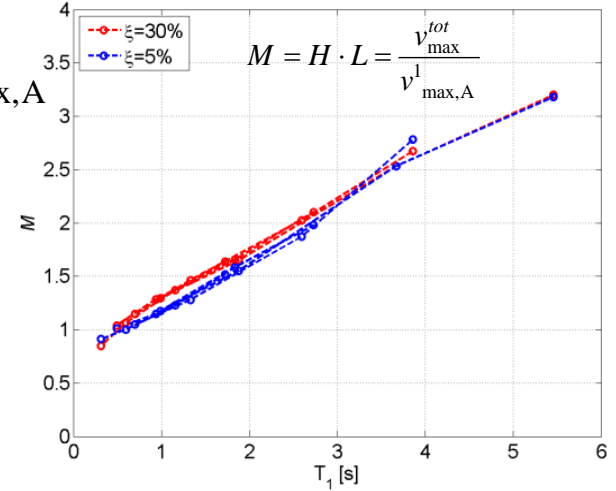
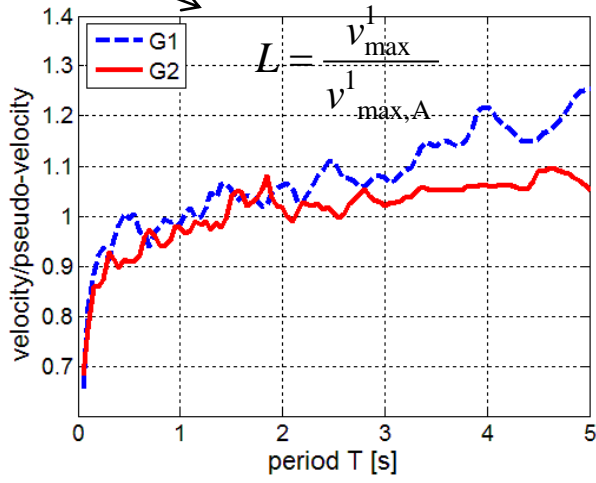
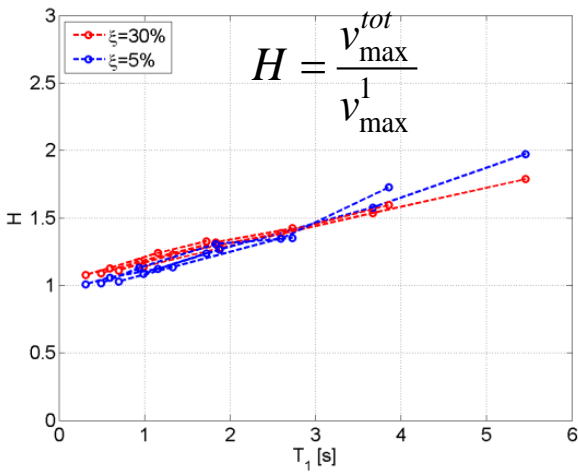
$$v_{\max} = \frac{S_{e,\xi}(T_1)}{\omega_1} \cdot \frac{12N}{(2+5N+5N^2)} \cdot \cos \theta$$

...



# 1. Higher modes contribution

$$v_{\max}^{tot} = \left( \frac{v_{\max}^{tot}}{v_{\max}^1} \right) \cdot \left( \frac{v_{\max}^1}{v_{\max,A}^1} \right) \cdot v_{\max,A}^1 = H \cdot L \cdot v_{\max,A}^1 = M \cdot v_{\max,A}^1$$



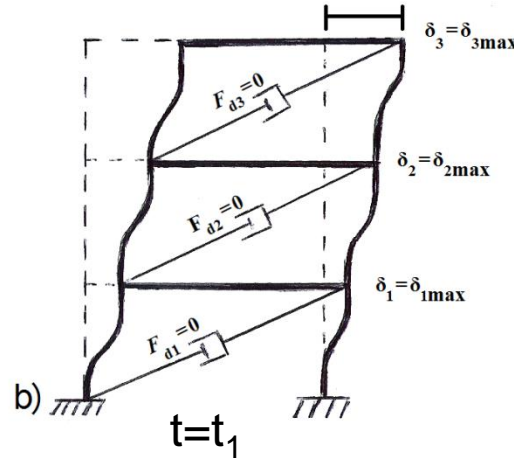
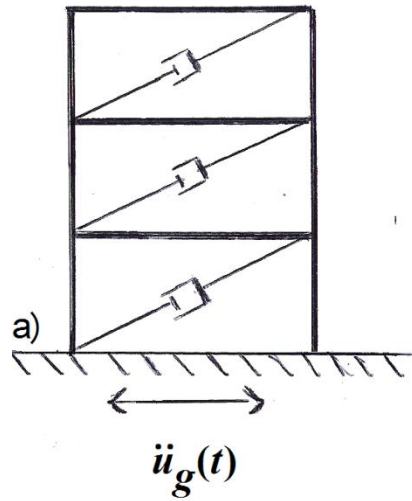
$$v_{\max,A}^{tot} = \begin{cases} \frac{12N}{(2+5N+5N^2)} \cdot \frac{S_a(T_1)}{\omega_1} & \text{for } T_1 \leq 0.5s \\ (0.44 \cdot T_1 + 0.78) \cdot \frac{12N}{(2+5N+5N^2)} \cdot \frac{S_a(T_1)}{\omega_1} & \text{for } 0.5 < T_1 \leq 5.0s \end{cases}$$

**correction factor  $M$**

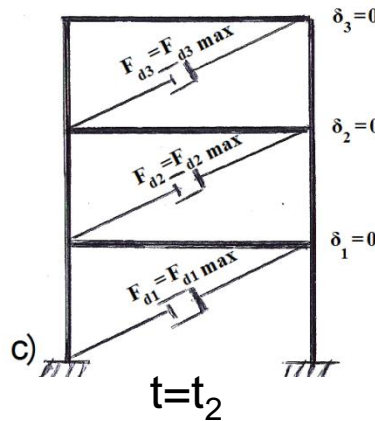
Palermo et al. 2017 (SDEE)



# 2. Equivalent Static Analysis for damped structures

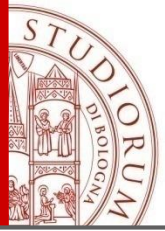


**Maximum Lateral Displacement Configuration (ESA1)**

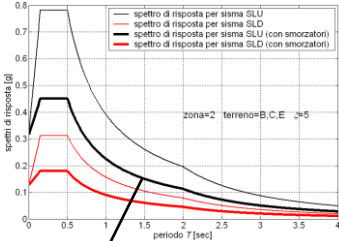


**Maximum Velocity Configuration (Max Damper Force) (ESA2)**

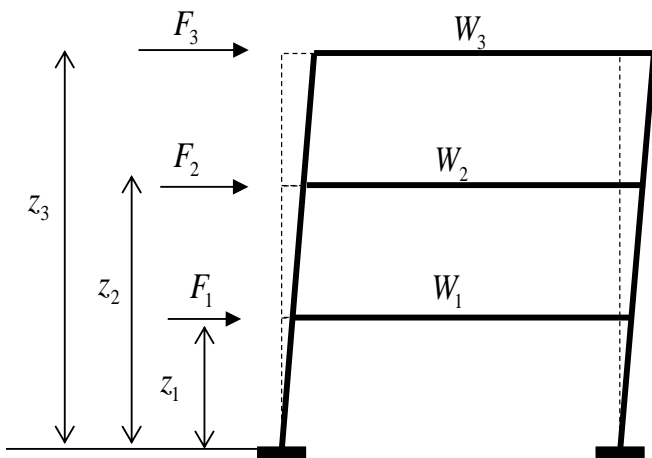
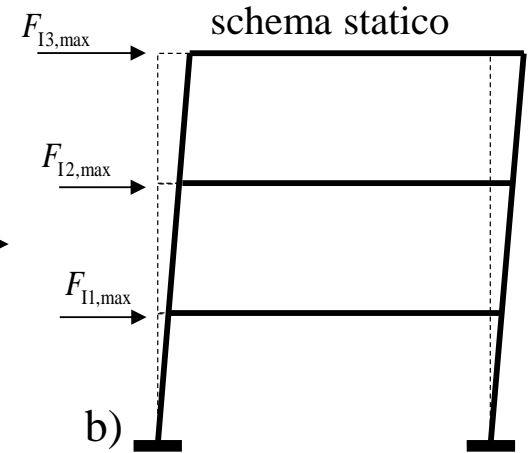
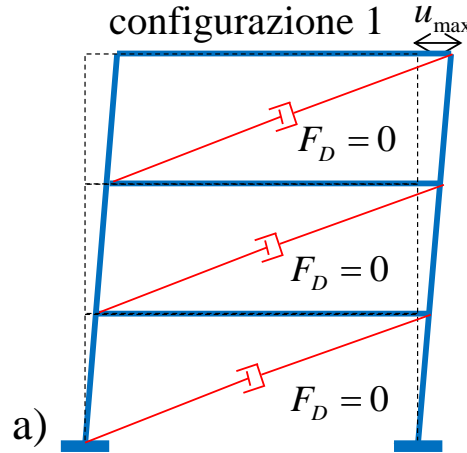




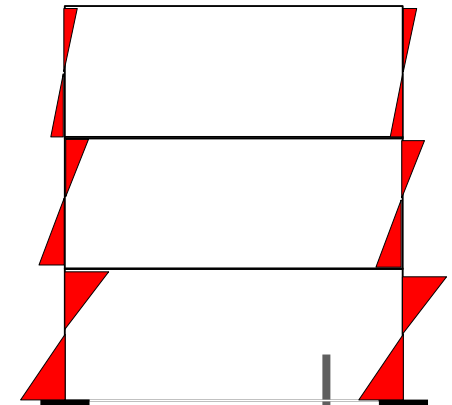
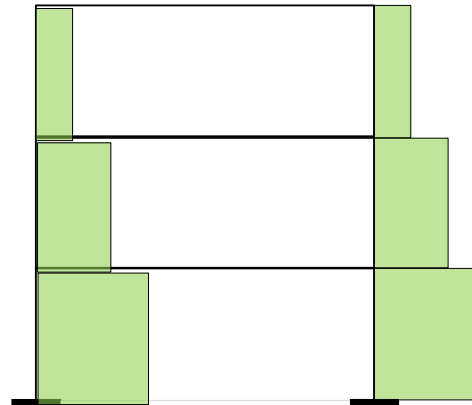
# How to perform Equivalent Static Analysis ESA1

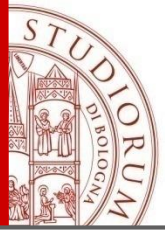


$$F_i = S_{e,\xi} \cdot \frac{W_i}{\sum_{i=1,2,\dots,N} W_i \cdot z_i}$$

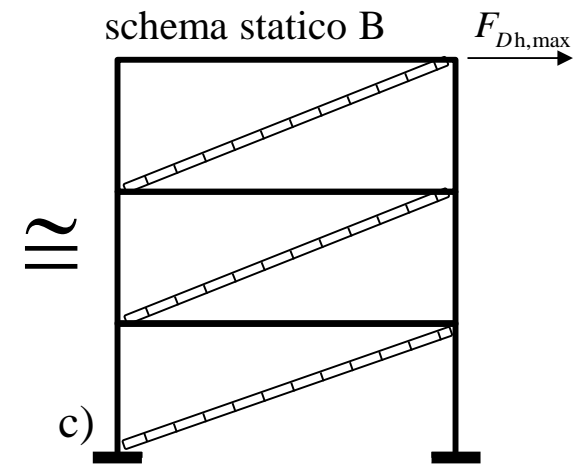
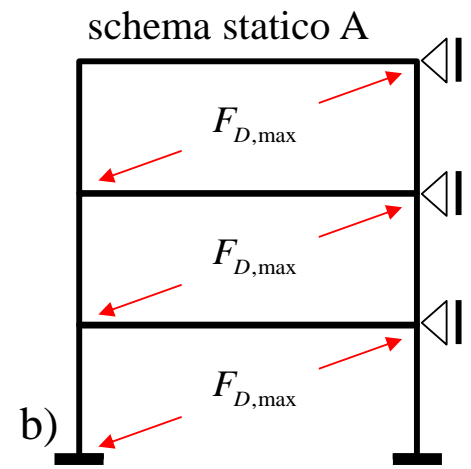
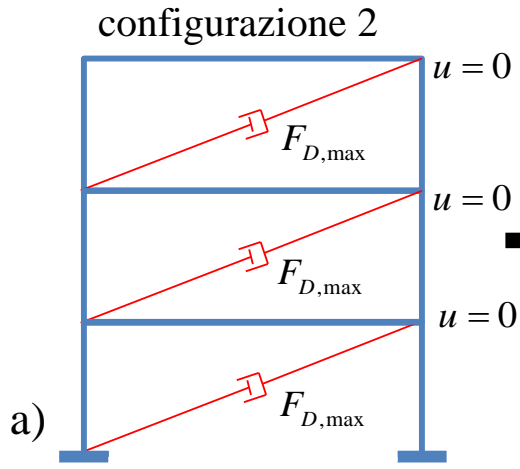


taglio  
 momento flettente

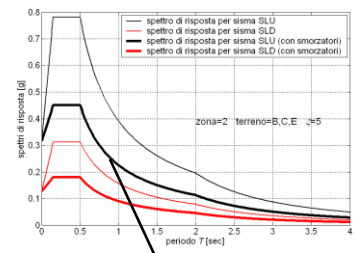
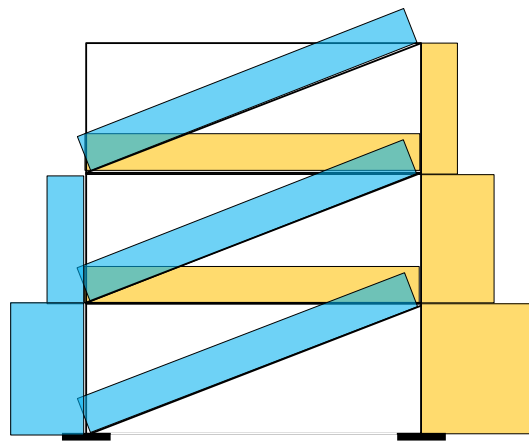
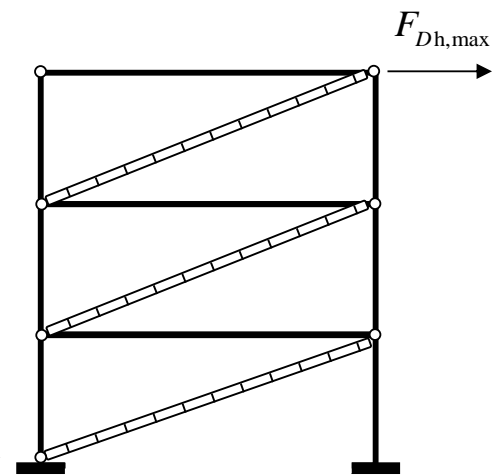




# How to perform Equivalent Static Analysis ESA2

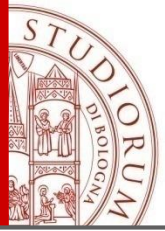


sforzo assiale (compressione)  
 sforzo assiale (trazione)



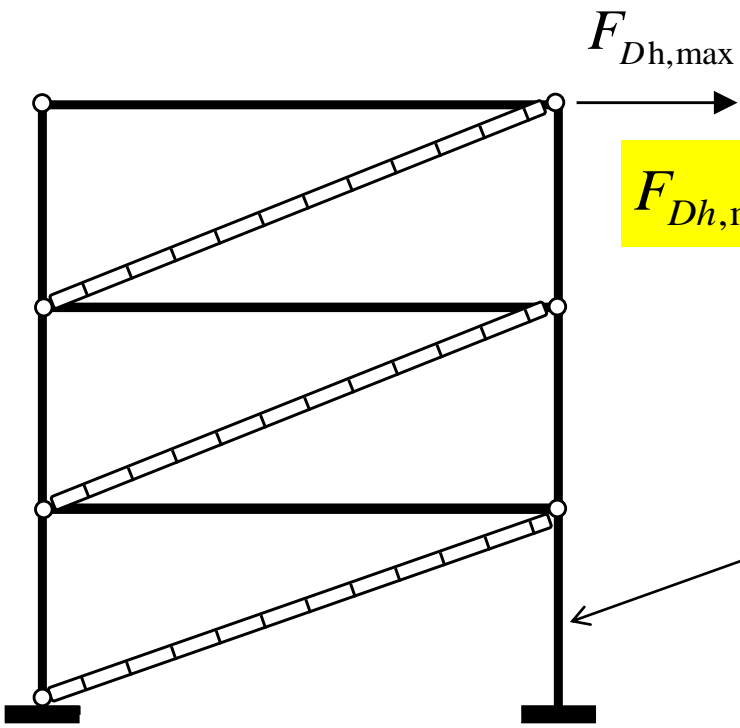
COLUMNS AXIAL FORCES DUE TO DAMPERS

$$P_{i,max} = (N - i + 1) F_{d,v,max} = \frac{2 \cdot \xi \cdot W_{tot}}{n} S_{e,\xi} \tan \theta$$



# How to perform Equivalent Static Analysis ESA2

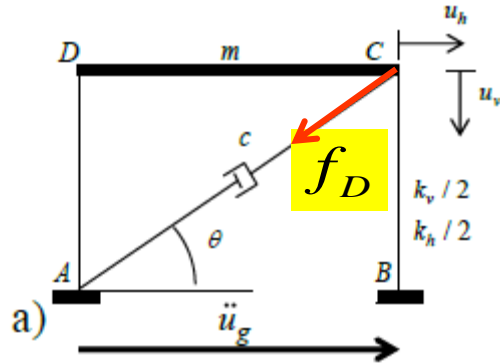
## ESA2



$$F_{Dh,max, struttura} = 0.8^{1-\bar{\alpha}} \cdot 2 \cdot \bar{\xi}_{visc} \cdot m_{tot} \cdot S_e(T_1, \bar{\eta})$$

objective:  
 $N_{column}$

# 2. The rationale behind ESA: the damped frame



dynamic equations

$$\begin{cases} f_{Ih} + f_{Dh} + f_{Sh} = 0 \\ f_{Iv} + f_{Dv} + f_{Sv} = 0 \end{cases}$$

two coupled equations  
(due to the damper)

$$\begin{cases} m\ddot{u}_h + c_h\dot{u}_h + c_v\dot{u}_v + k_h u_h = -m\ddot{u}_g(t) \\ m\ddot{u}_v + c_{hv}\dot{u}_h + c_v\dot{u}_v + k_v u_v = 0 \end{cases}$$

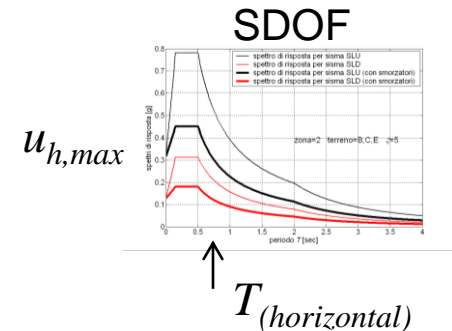


$$k_v \gg k_h$$

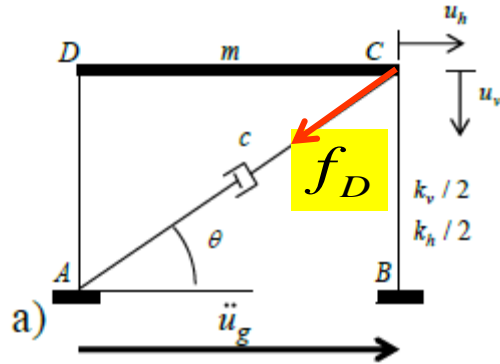
$\dot{u}_v$  can be neglected in the first equation

first equation  
(only in the horizontal d.o.f.)

$$m\ddot{u}_h + c_h\dot{u}_h + k_h u_h = -m\ddot{u}_g(t)$$



## 2. The rationale behind ESA: the damped frame



$u_h(t)$  or  $u_{h,max}$  is obtained  
and the damper force is obtained as:

$$c_h \dot{u}_h(t) = f_{Dh}(t) = f_D(t) \cdot \cos \theta$$

$$f_D(t) = \frac{c_h \dot{u}_h(t)}{\cos \theta}$$



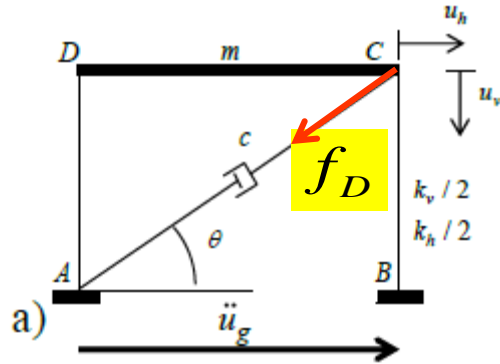
second  
equation

$$m \ddot{u}_v + c_v \dot{u}_v + k_v u_v = -c_{hv} \dot{u}_h = -f_{Dv}(t) = -f_D(t) \cdot \sin \theta$$

$$m \ddot{u}_v + c_v \dot{u}_v + k_v u_v = -f_{Dv}(t)$$

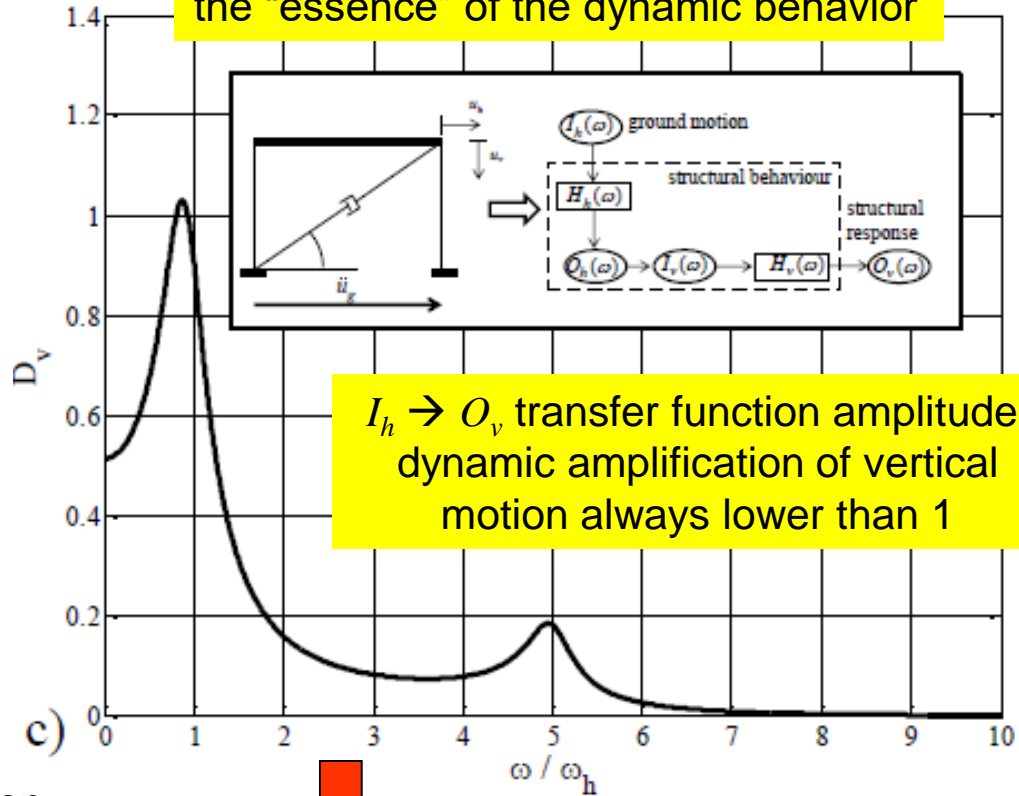
the input for the vertical  
d.o.f. is given by the  
damper force  
(coupled response)

# 2. The rationale behind ESA: the damped frame



$$k_v \gg k_h$$

the "essence" of the dynamic behavior



$I_h \rightarrow O_v$  transfer function amplitude: dynamic amplification of vertical motion always lower than 1

the second dynamic equation can be treated as a static equation

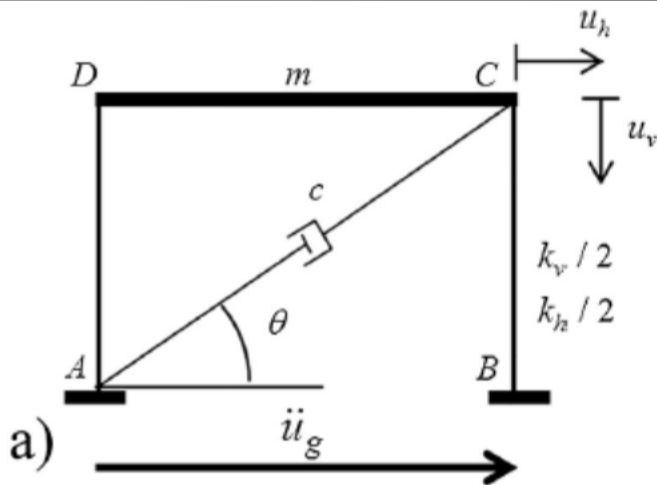
$$m \cancel{u_v} + c \cancel{\dot{u}_v} + k_v u_v = -f_{Dv}(t)$$

axial force in the column

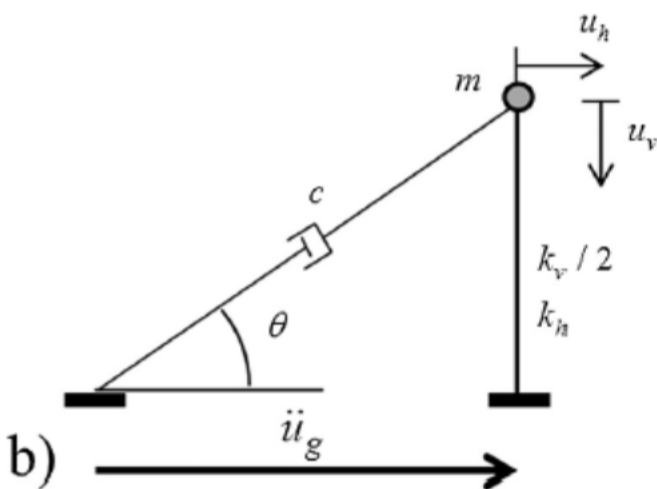
$$k_v u_{v,\max} = -f_{Dv,\max}$$



# 2. The rationale behind ESA: the damped frame



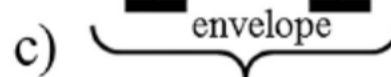
$$f_{Dv,max} = 2 \cdot \xi \cdot m \cdot S_{\epsilon, \bar{z}}(T_1) \cdot \tan \theta$$



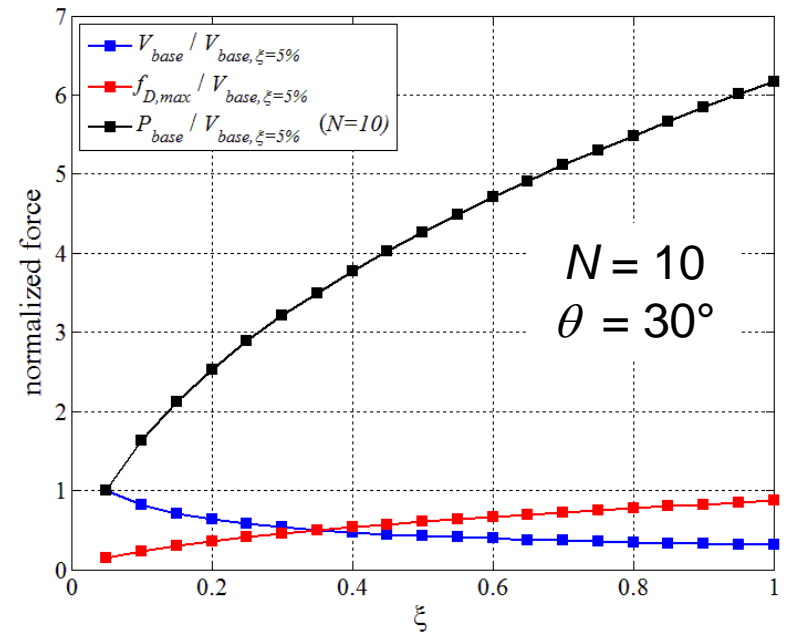
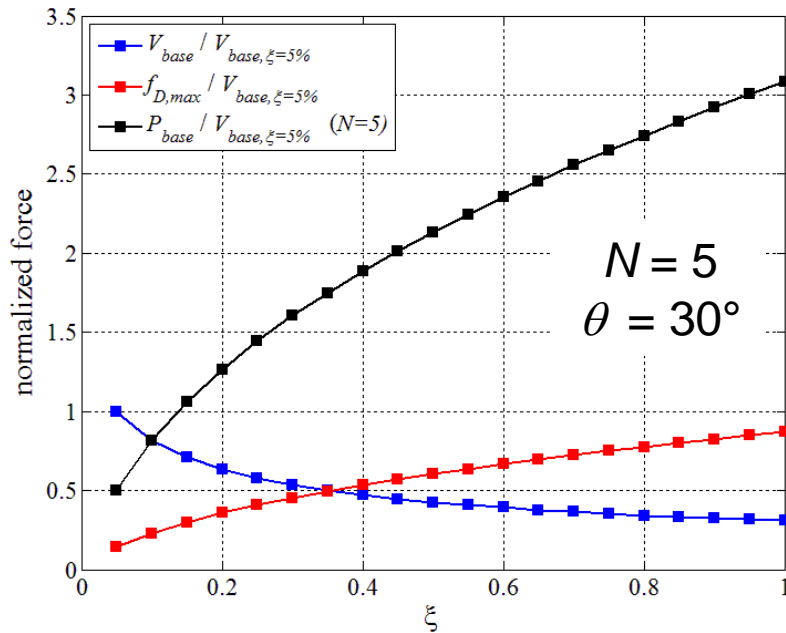
$$f_{Dh,max} = m \cdot S_{\epsilon, \bar{z}}(T_1)$$

**ESA1**

**ESA2**

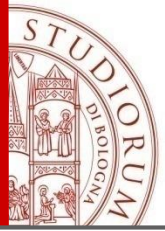


# Axial forces in the columns due to dampers



**REMEMBER:** For tall buildings the axial forces due to dampers may become even larger than the axial forces due to static vertical loads

# The direct five-step procedure for inter-storey dampers placement



STEP 1: performance objectives



$$\bar{\eta} \rightarrow \bar{\xi}$$

$$\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}}}$$

STEP 2: linear damper

$$v_{\max} = \frac{S_{e,\xi}(T_1)}{\omega_1} \cdot \frac{2}{(N+1)} \cdot \cos \theta$$

$$c_L = \bar{\xi} \cdot \omega_1 \cdot m_{tot} \cdot \left( \frac{N+1}{n} \right)$$

STEP 3: linear TH

analytical estimations

response

$$v_{\max} = \frac{S_{e,\xi}(T_1)}{\omega_1} \cdot \frac{2}{(N+1)} \cdot \cos \theta$$

$$F_{D\max} = \frac{2 \cdot \xi \cdot m_{tot} \cdot S_{e,\xi}(T_1)}{\cos \theta}$$

STEP 4: non-linear

$$F_{D\max} = \frac{2 \cdot \xi \cdot m_{tot} \cdot S_{e,\xi}(T_1)}{\cos \theta}$$

$(k_{oil})$

$$c_{NL} = c_L \cdot (\chi \cdot v_{\max})^{1-\alpha}$$

STEP 5:

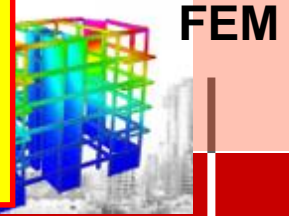
$$P_{i,\max} = (N - i + 1) \cdot 0.8^{1-\alpha} \cdot \frac{2 \cdot \xi \cdot m_{tot} \cdot S_{e,\xi}}{n} \cdot \tan \theta$$

$$) \cdot 0.8^{1-\alpha} \cdot \frac{2 \cdot \xi \cdot m_{tot} \cdot S_{e,\xi}}{n} \cdot \tan \theta$$

or  
ESA2 procedure

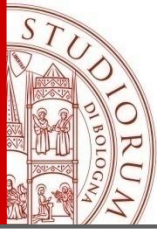
or

ESA2 procedure



FEM

# “Direct five-step procedure”



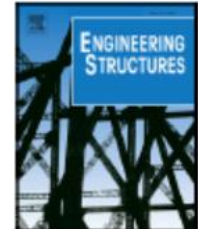
Engineering Structures 173 (2018) 933–950



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## A “direct five-step procedure” for the preliminary seismic design of buildings with added viscous dampers

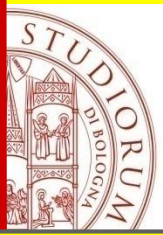


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### ABSTRACT

In the present work a direct procedure for the preliminary seismic design of building structures with added dampers is described which represents the simplification of the so-called “five-step procedure” originally developed in 2010 by some of the authors. The procedure is applicable to yielding frame structures with a generic along-the-height distribution of inter-storey viscous dampers. It is aimed at guiding the structural engineer through the sizing of both viscous dampers and structural elements making use of an equivalent static analysis approach. First, the peak structural response under earthquake excitation is reduced by imposing an overall reduction factor accounting for both the ductility demand and the viscous damping provided by the added dampers. Second, linear damping coefficients are calculated in order to reduce the structural response according to the selected target damping ratio. Then, analytical formulas allow the estimation of peak velocities and forces in the dissipative devices, and an energy criterion is used to identify the non-linear mechanical characteristics of the actual manufactured viscous dampers. Finally, the internal actions in the structural elements are estimated through the envelope of two equivalent static analyses (ESA). At this initial stage of the research, the procedure appears suitable for the preliminary design phase, while correction factors for the higher modes contributions need to be applied to improve its accuracy, especially for high-rise buildings. A numerical verification of the final behaviour of the system by means of non-linear time-history analyses is recommended. An applicative example is finally developed to highlight the soundness of the procedure.



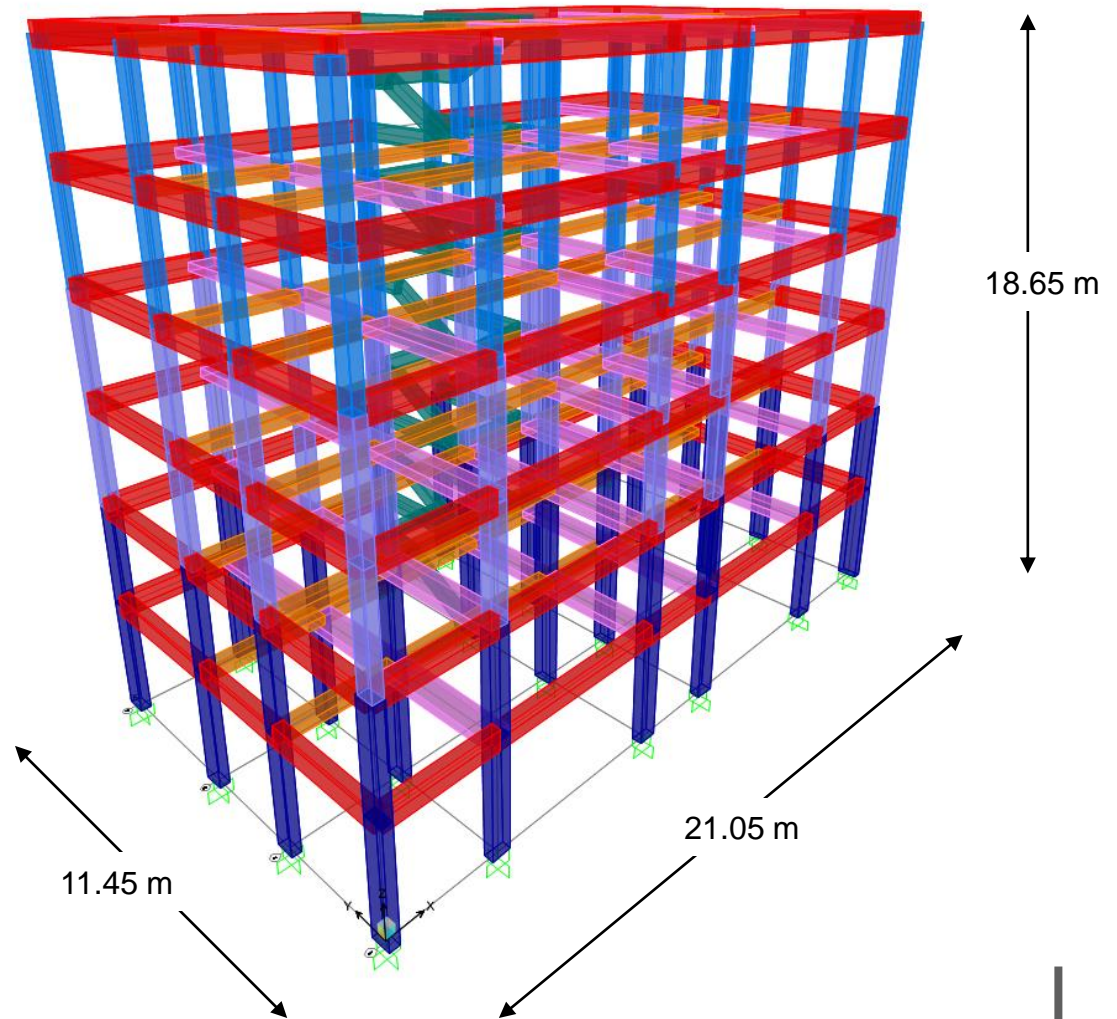
# Applicative example



# The case study

## NEW DESIGN

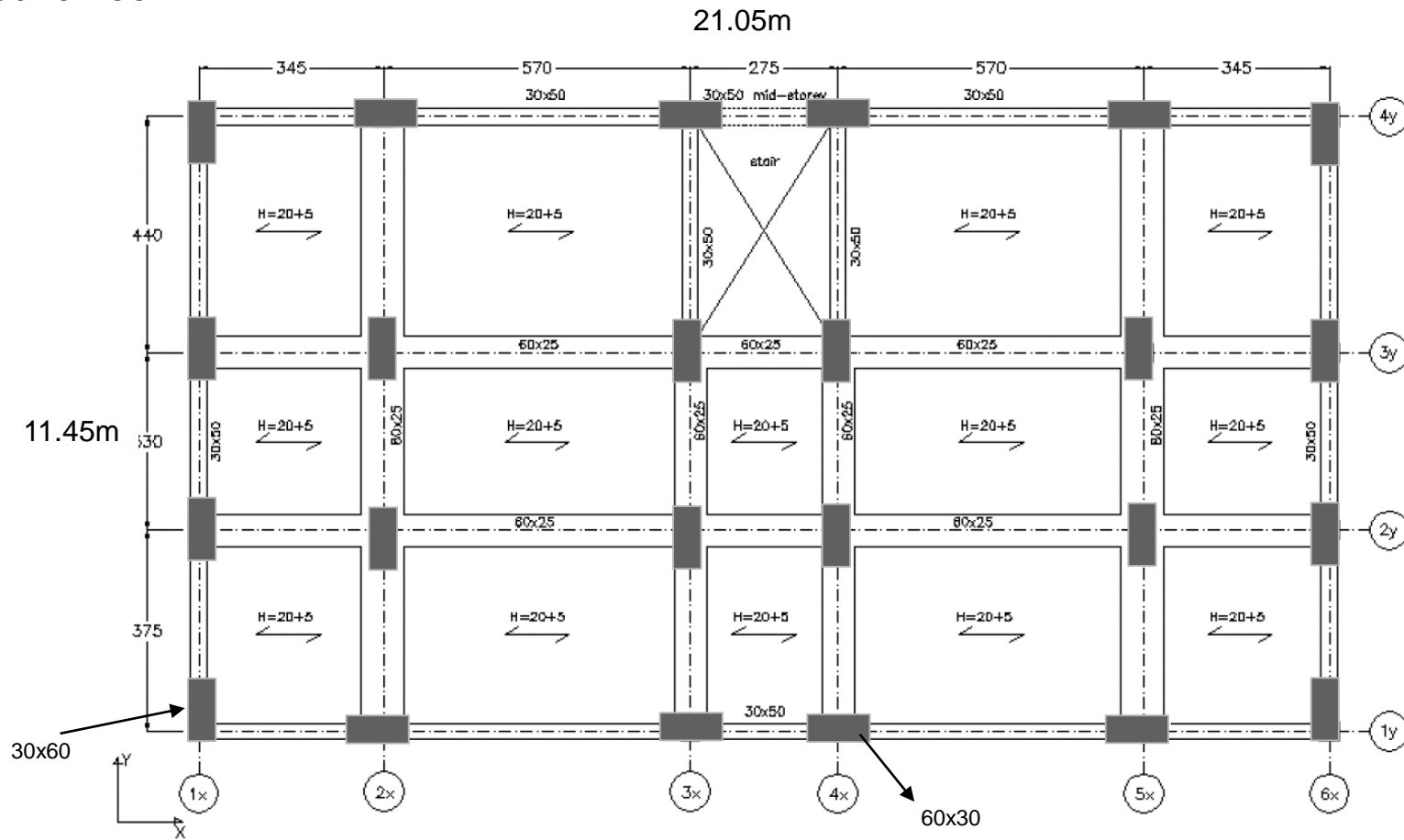
Reinforced-Concrete  
6-storey building  
supposed  
to be located in L'Aquila  
(Central Italy)





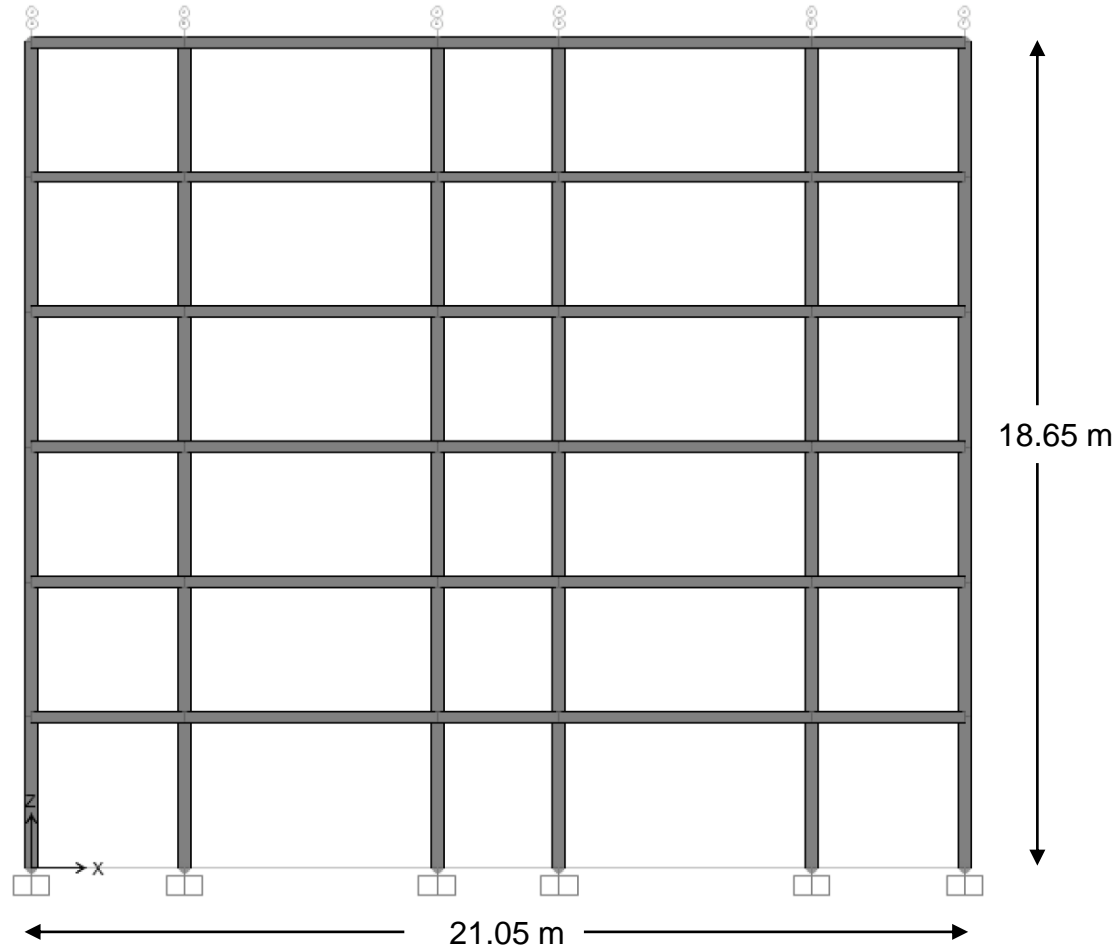
# The case study

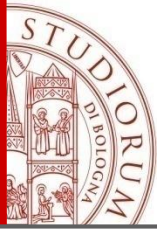
Ground floor:



# The case study

Frame  
along X  
direction:





# The case study

Load analysis:

Loads	From floor 1 to floor 5	Floor 6 (attic + roof)
<i>Dead</i>	To be considered floor by floor	To be considered floor by floor
<i>Permanent G1</i>	3,0 [kN/m <sup>2</sup> ]	3,0 [kN/m <sup>2</sup> ]
<i>Permanent G2</i>	2,5 [kN/m <sup>2</sup> ]	1,8 [kN/m <sup>2</sup> ]
<i>Imposed Loads Q</i>	2,0 [kN/m <sup>2</sup> ]	2,0 [kN/m <sup>2</sup> ]
<i>TOTAL in static conditions + Dead</i>	7.5 [kN/m <sup>2</sup> ]	6.8 [kN/m <sup>2</sup> ]
<i>TOTAL in seismic conditions + Dead</i>	6,05 [kN/m <sup>2</sup> ]	5,35 [kN/m <sup>2</sup> ]

$$A_{floor} = 21.05 \text{ m} \cdot 11.45 \text{ m} = 241 \text{ m}^2$$

$$W_{floor} = p_{seismic, floor} \cdot A_{floor} = 6.05 \frac{\text{kN}}{\text{m}^2} \cdot 241 \text{ m}^2 = 1458 \text{ kN}$$

$$W_{roof} = p_{seismic, roof} \cdot A_{floor} = 5.35 \frac{\text{kN}}{\text{m}^2} \cdot 241 \text{ m}^2 = 1289 \text{ kN}$$

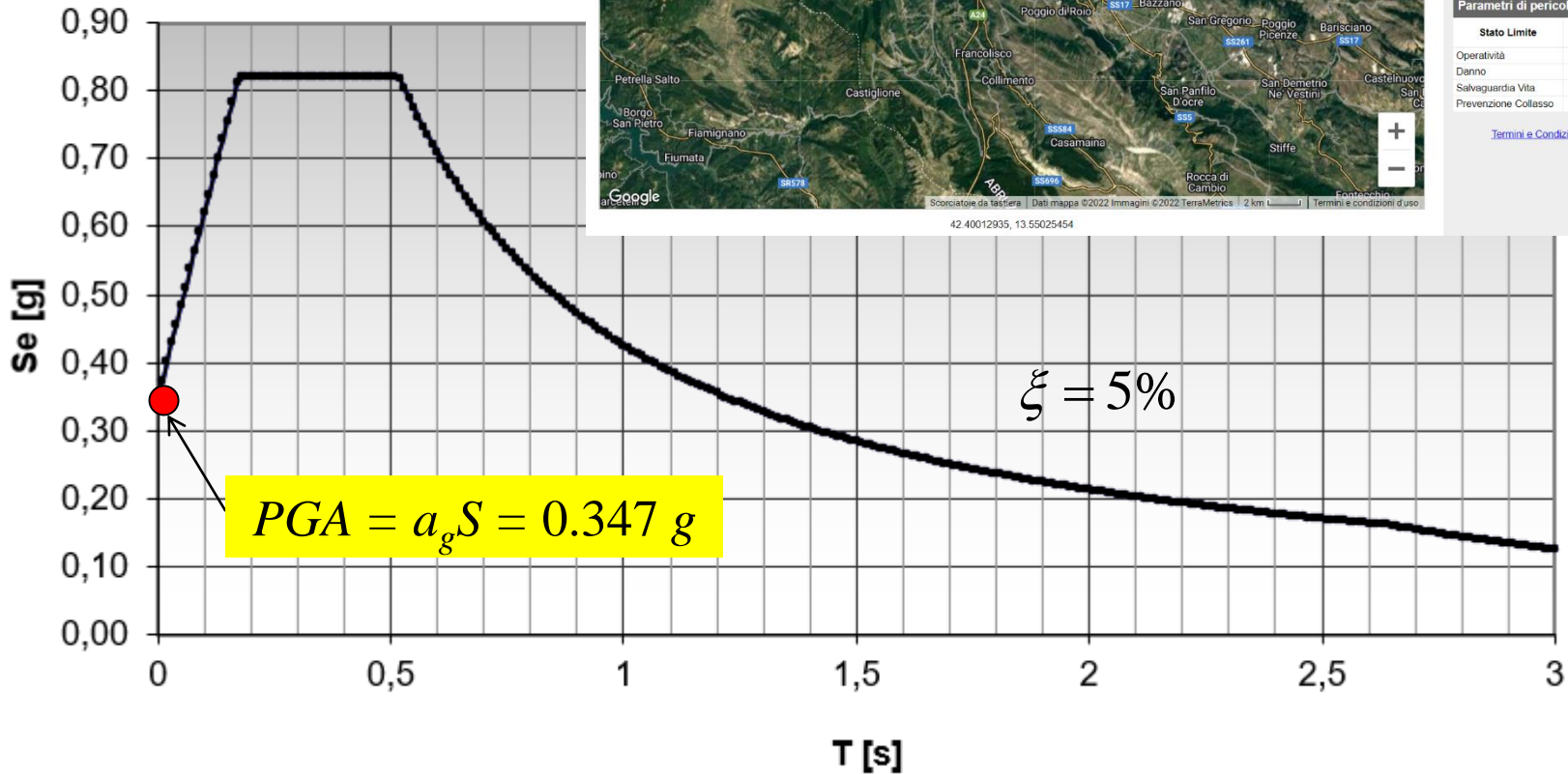
$$W_{perimeter walls} = 455 \text{ kN}$$

$$W_{beams and columns} = (V_{columns} + V_{beams}) \cdot \gamma_{cls} \approx 1000 \text{ kN}$$

total weight in seismic conditions  
 $W_{tot} = 16600 \text{ kN}$

# The case study

The horizontal pseudo-acceleration elastic response spectrum:



EdiLus-MS è il software ACCA per individuare la pericolosità sismica di tutte le località italiane direttamente dalla mappa. Scrivi l'indirizzo e/o sposta il segnalino sul sito che ti interessa e otterrai dinamicamente tutti i parametri di pericolosità sismica.  
ad es. "Contrada Rosole, 13 BAGNOLI IRPINO"

L'Aquila

Mappa Satellite

Scorciatoie da tastiera | Dati mappa ©2022 Immagini ©2022 TerraMetrics | 2 km

42.40012935, 13.55025454

Latitudine (WGS84)  Longitudine (WGS84)

Latitudine (ED50)  Longitudine (ED50)

Altitudine (mt)

Classe dell'edificio  
I: Costruzioni il cui uso preveda normali affollamenti

Vita Nominale Struttura

Periodo di Riferimento per l'azione sismica

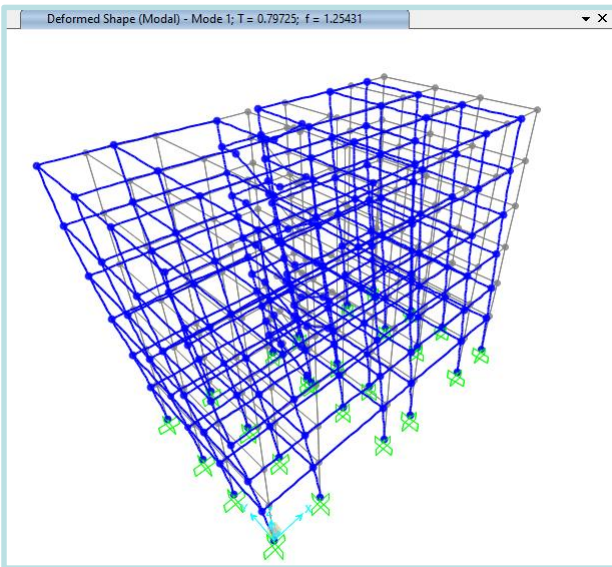
**Parametri di pericolosità Sismica**

Stato Limite	$T_f$ [anni]	$a_g/g$ [g]	$F_0$ [g]	$T_c$ [s]
Operatività	30	0.079	2.400	0.270
Denno	50	0.104	2.330	0.280
Salvaguardia Vita	475	0.261	2.360	0.350
Prevenzione Collasso	975	0.334	2.400	0.360

[Termini e Condizioni di utilizzo di EdiLus-MS](#)

# The case study

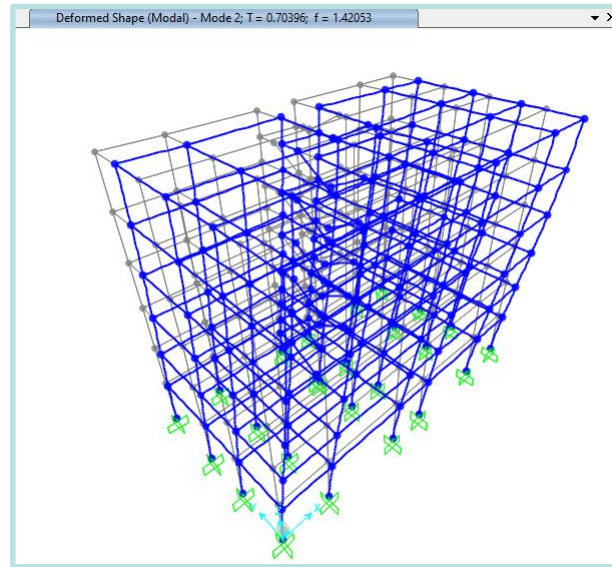
Modes of vibration:



Mode 1  
Translational along X

$$T = 0.797 \text{ s}$$

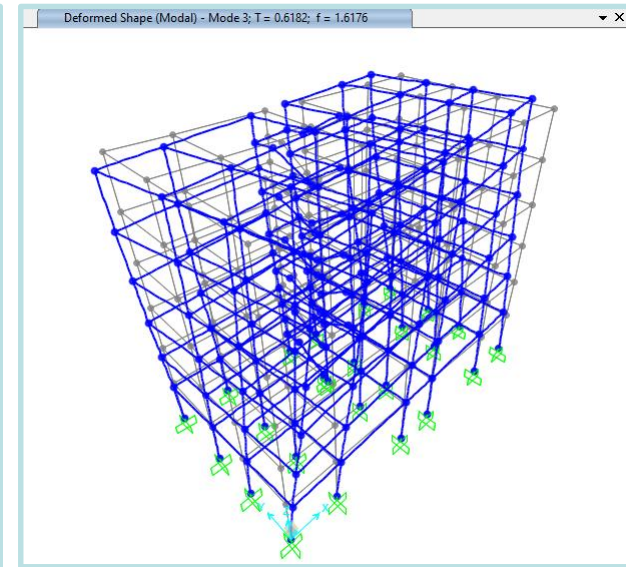
$$M_{\%,UX} = 81.4 \%$$



Mode 2  
Translational along Y

$$T = 0.704 \text{ s}$$

$$M_{\%,UY} = 80.3 \%$$



Mode 3  
Rotational

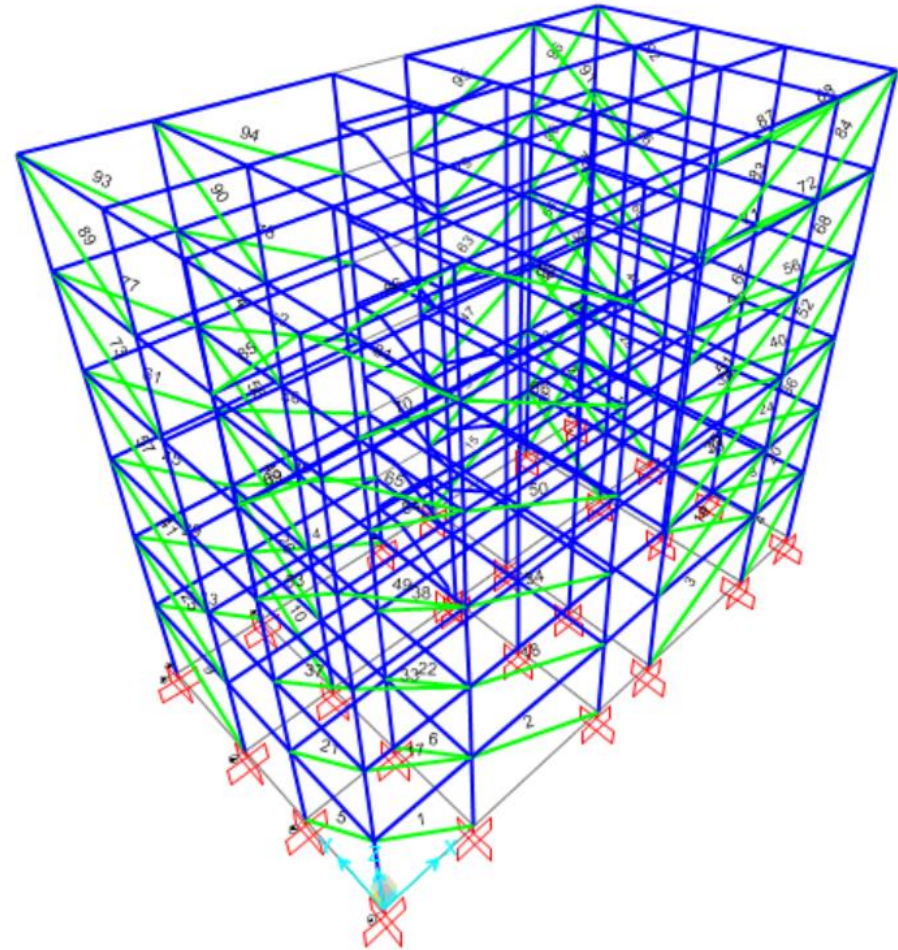
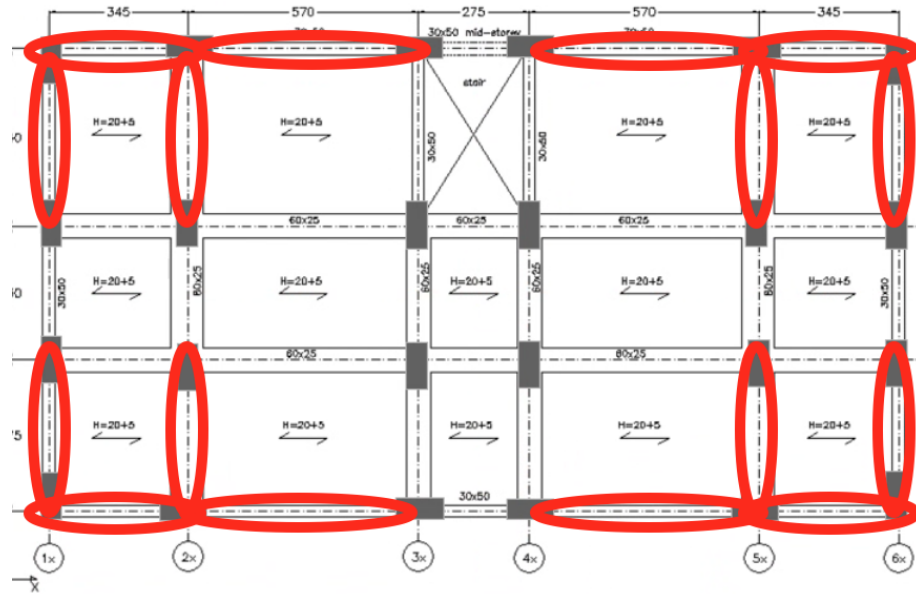
$$T = 0.618 \text{ s}$$

$$M_{\%,RZ} = 80.8 \%$$



# The case study

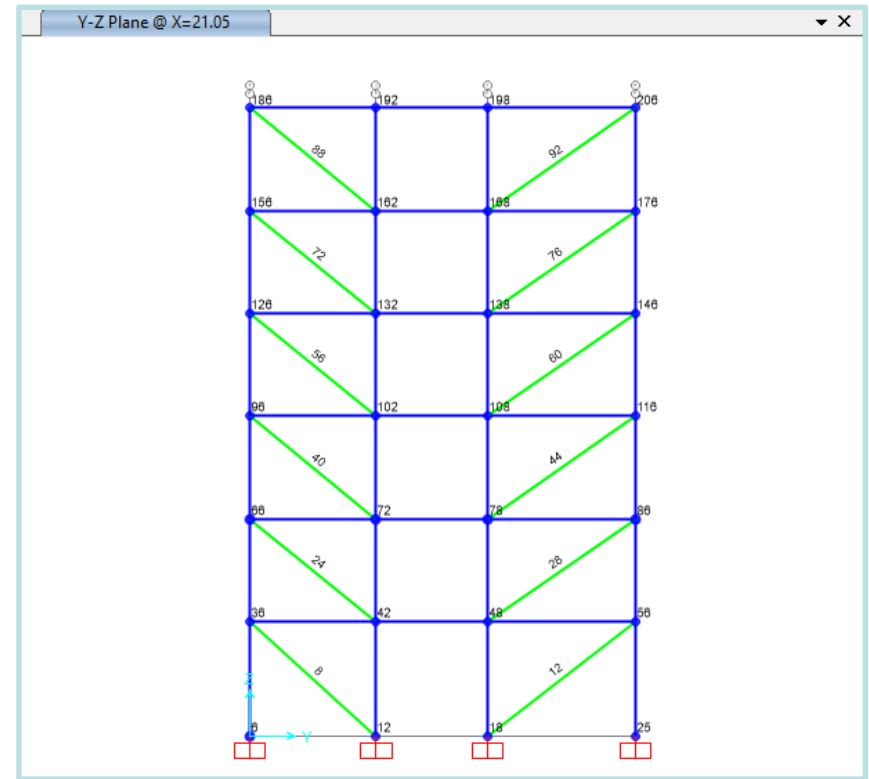
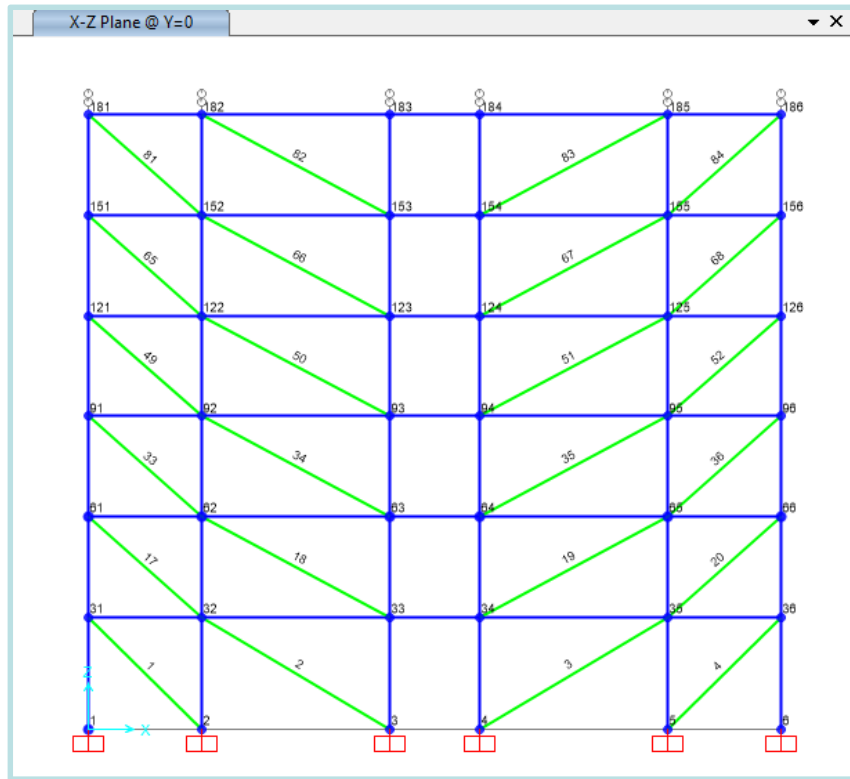
Dampers location:





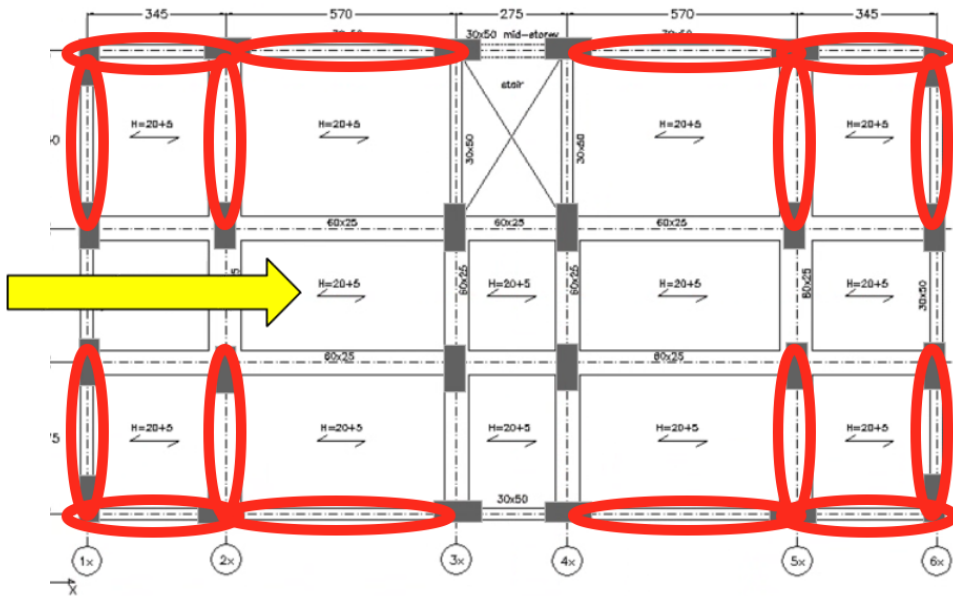
# The case study

Dampers location:



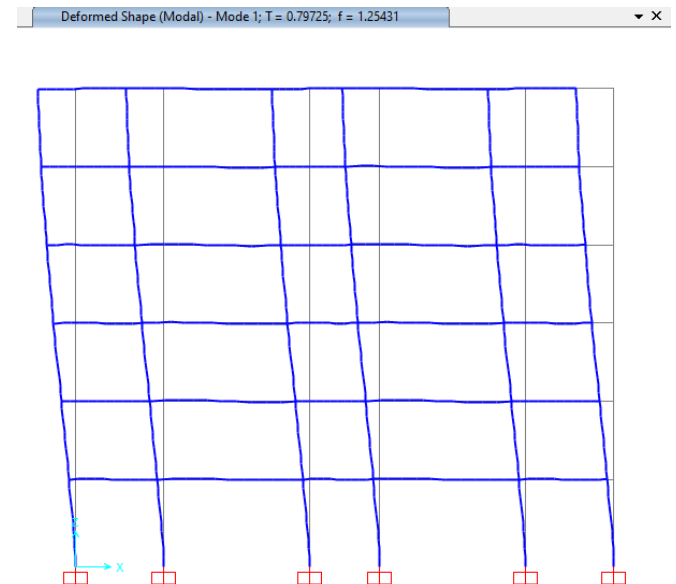
# The direct five-step procedure applied to the case study

seismic action along the X-direction



First mode along the X-direction

$$T_{1,x} = 0.797 \text{ s}$$



# Application - Step 1

## STEP 1

Target damping ratio:

$$\bar{\xi}_{tot} = \xi_{intr} + \bar{\xi}_{visc} = 5\% + ? = ?$$

through dampers



Corresponding response reduction factor:

$$\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}_{tot}}} = \sqrt{\frac{10}{5 + ?}} = ?$$

Fundamental period along the considered (longitudinal) direction:  $T_1 = 0.797$  s

**How can we define the size of the needed dampers  
in a  
«preliminary quick design / dimensioning phase»?**

# Application - Step 1

 $\bar{\eta}$ 

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{\text{Demand reduced by dampers}}{\text{Demand}} = \frac{\text{Capacity}}{\text{Demand}}$$

*Elastic Demand:*

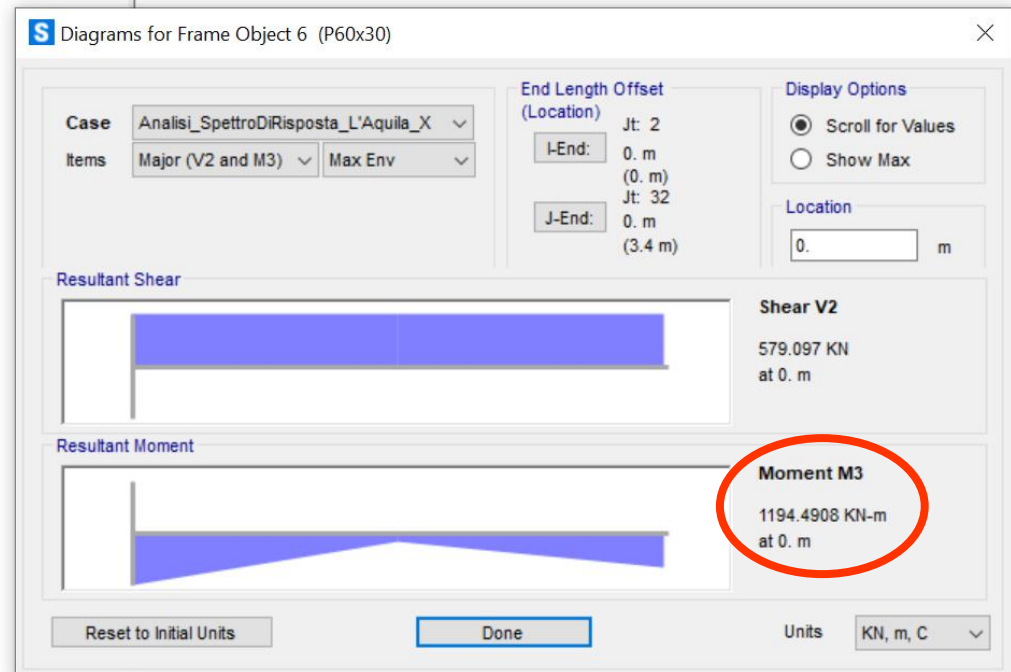
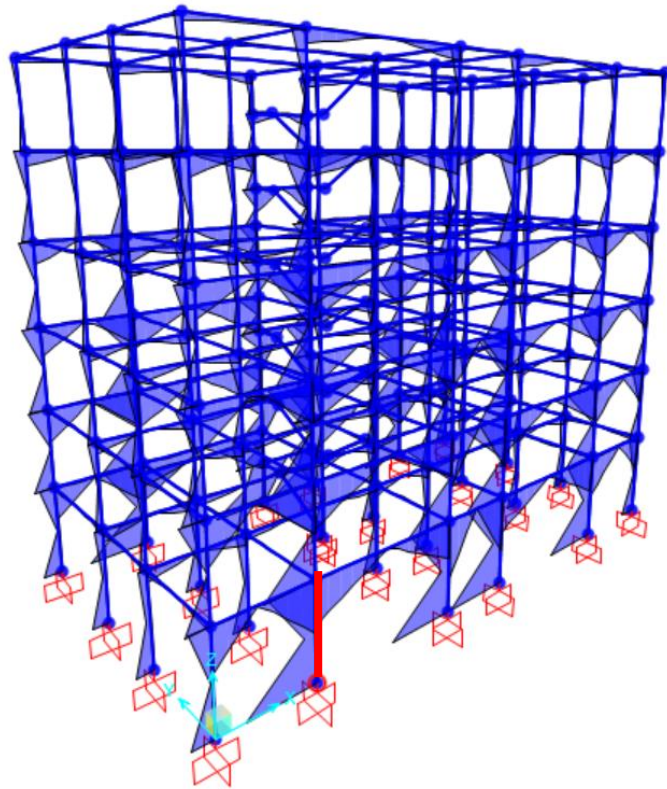
The bending moment generated by an elastic response spectrum analysis at the base of the **most stressed ground floor column** is:

$$M_{Ed,\xi=5\%} = 1194 \text{ kNm}$$

# Application - Step 1

$\bar{\eta}$

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{\text{Demand reduced by dampers}}{\text{Demand}} = \frac{\text{Capacity}}{\text{Demand}}$$



# Application - Step 1

 $\bar{\eta}$ 

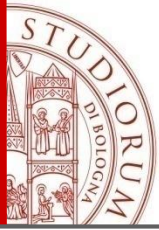
$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{\text{Demand reduced by dampers}}{\text{Demand}} = \frac{\text{Capacity}}{\text{Demand}}$$

*Capacity:*

The yielding bending moment of the base cross-section of the **most stressed ground floor column** is, for a reasonable amount of reinforcement bars and for the axial force corresponding to the seismic condition ( $N = 686$  kN) is:

$$M_{Rd} = 510 \text{ kNm}$$

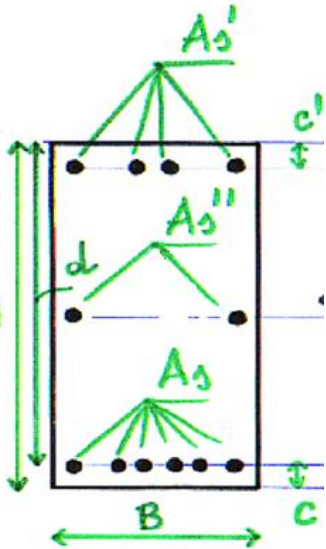




# Application - Step 1

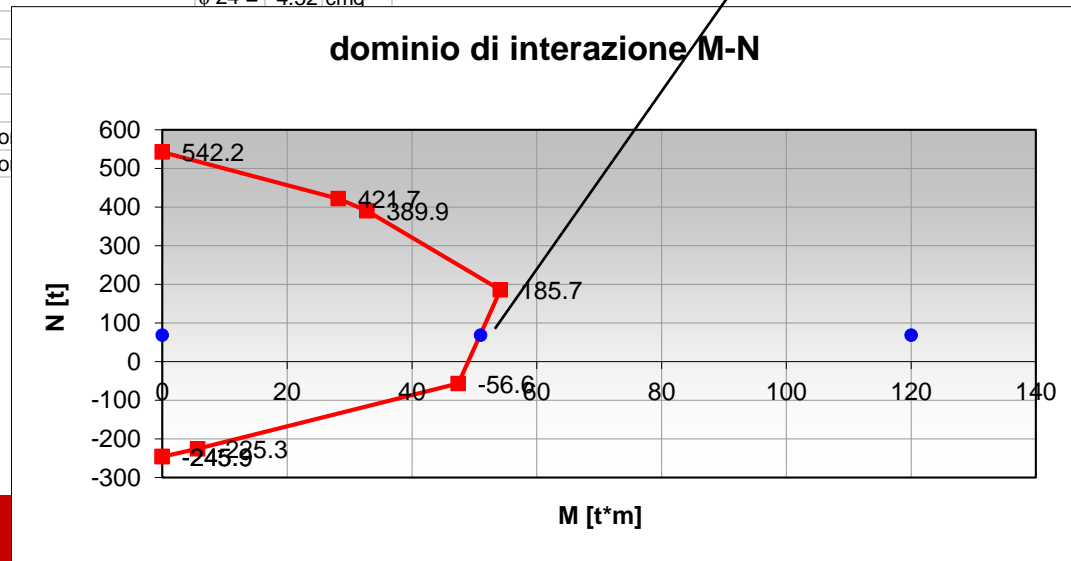
$\bar{\eta}$

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{\text{Demand reduced by dampers}}{\text{Demand}} = \frac{\text{Capacity}}{\text{Demand}}$$



DATI DELLA SEZIONE		(in rosso i dati di input)	
B =	30 cm	base	$\phi 6 = 0.28 \text{ cmq}$
H =	60 cm	altezza	$\phi 8 = 0.50 \text{ cmq}$
c =	4 cm	copriferro ferro teso	$\phi 10 = 0.79 \text{ cmq}$
c' =	4 cm	copriferro ferro compresso	$\phi 12 = 1.13 \text{ cmq}$
d = H-c =	56 cm	altezza utile	$\phi 14 = 1.54 \text{ cmq}$
As =	15.71 cmq	area ferro teso	$\phi 16 = 2.01 \text{ cmq}$
As' =	15.71 cmq	area ferro compresso	$\phi 18 = 2.54 \text{ cmq}$
As'' =	31.42 cmq	area ferro centrale	$\phi 20 = 3.14 \text{ cmq}$
Astot =	62.83 cmq	area totale	$\phi 22 = 3.80 \text{ cmq}$
fyk =	4500 kg/cmq		$\phi 24 = 4.52 \text{ cmq}$
Es =	2100000 kg/cmq		
Rck =	350 kg/cmq		
fyd =	3913 kg/cmq		
fcd =	165 kg/cmq		
$\epsilon_{su} =$	6.75E-02	deformazio	
$\epsilon_{se} =$	1.86E-03	deformazio	

M [t*m]	N [t]
0	68.6
120	68.6
51	68.6



# Application - Step 1

 $\bar{\eta}$ 

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{\text{Demand reduced by dampers}}{\text{Demand}} = \frac{\text{Capacity}}{\text{Demand}}$$

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{M_{Rd}}{M_{Ed,\xi=5\%}} = \frac{510 \text{ kNm}}{1194 \text{ kNm}} = 0.43$$

# Application - Step 1

$\bar{\eta}$

$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{M_{Rd}}{M_{Ed,\xi=5\%}} = \frac{510 \text{ kNm}}{1194 \text{ kNm}} = 0.43$$

Now, two possibilities corresponding to two different strategies:

- **To rely on the behaviour factor** (dissipation due to damage in the structural elements)

➔ lower immediate costs, but lower performances (and also possible higher future costs in the event of a strong ground motion)

- **To introduce dampers** (dissipation with no damage in the structural elements)

➔ higher immediate costs, but higher performances (and, most likely, no future costs in the event of a strong ground motion). Also, plastic resources (which are anyway there) are saved for a very very strong earthquake

# Application - Step 1

 $\bar{\eta}$ 

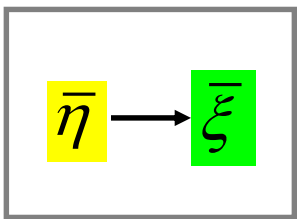
$$\bar{\eta} = \frac{M_{Ed,\xi}}{M_{Ed,\xi=5\%}} = \frac{M_{Rd}}{M_{Ed,\xi=5\%}} = \frac{510 \text{ kNm}}{1194 \text{ kNm}} = 0.43$$

Let's go for **dampers**.

Let's assume:  $\bar{\eta} = 0.50$

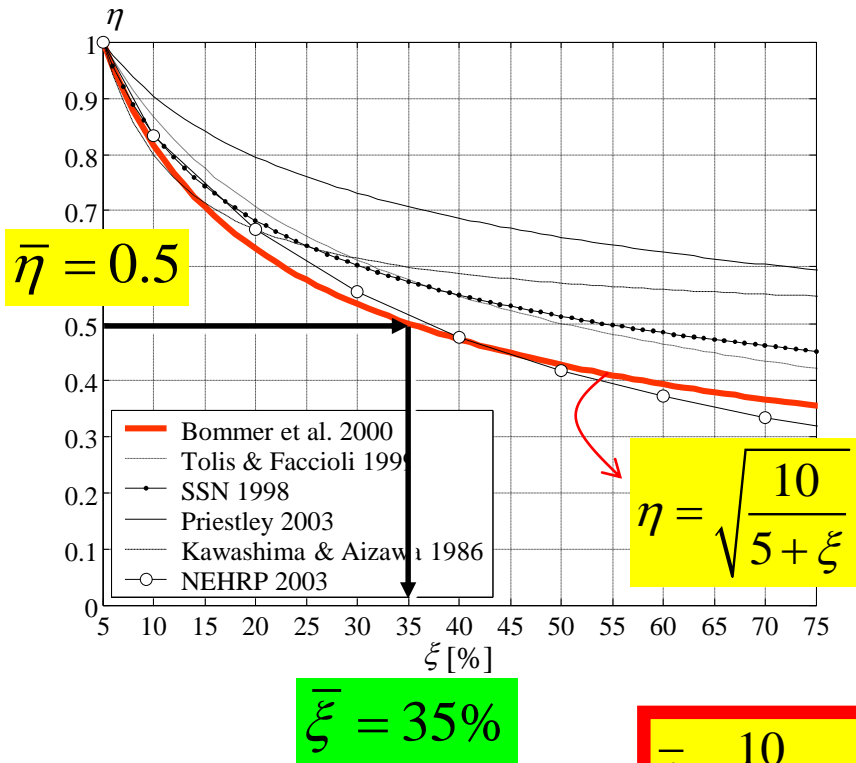
even if it could be not enough ...

# Application - Step 1

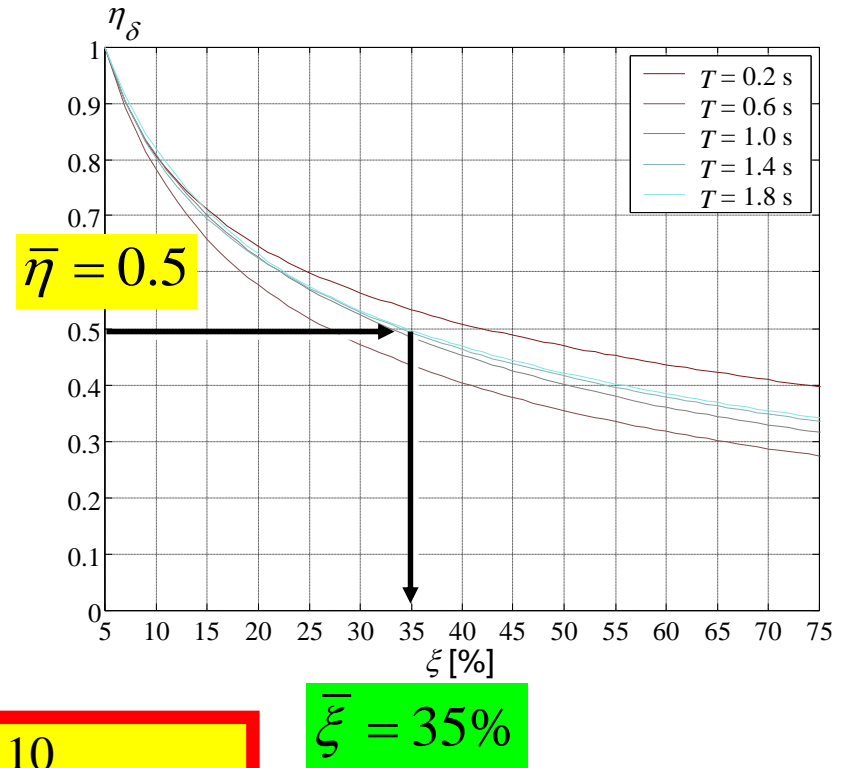


Some available formulations to relate  $\bar{\eta} \rightarrow \bar{\xi}$

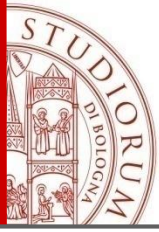
Cardone, Dolce, Rivelli (ANIDIS 2007)



mean SDOF response from T-H analyses



$$\bar{\xi} = \frac{10}{\bar{\eta}^2} - 5 = \frac{10}{0.5^2} - 5 = 35$$



# Application - Step 1

## STEP 1

Assumed target damping ratio:  $\bar{\xi}_{tot} = \xi_{intr} + \bar{\xi}_{visc} = 5\% + 30\% = 35\%$

through dampers

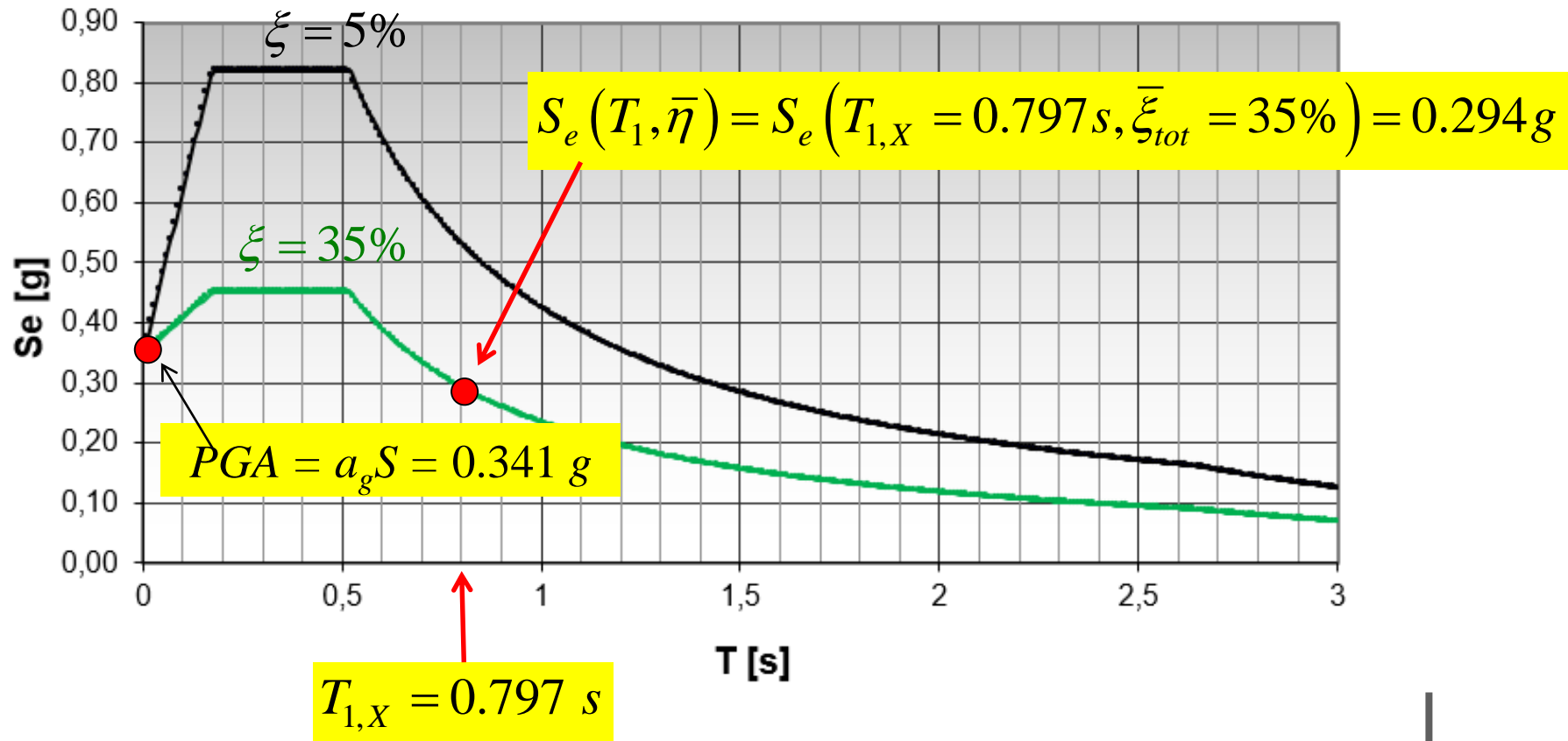
Corresponding response reduction factor:  $\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}_{tot}}} = \sqrt{\frac{10}{5 + 35}} = 0.50$

Fundamental period along the considered (longitudinal) direction:  $T_1 = 0.797\text{ s}$

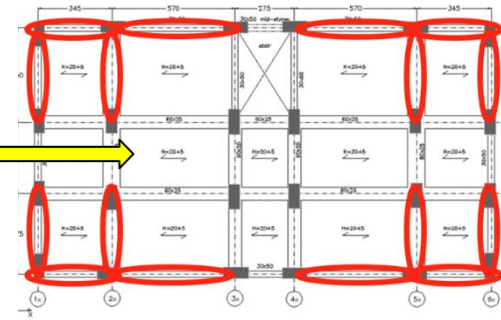
Spectral acceleration: 
$$S_e(T_1, \bar{\eta}) = a_g \cdot S \cdot \bar{\eta} \cdot F_o \cdot \left( \frac{T_c}{T_1} \right) =$$
$$= 0.261\text{ g} \cdot 1.333 \cdot 0.50 \cdot 2.360 \cdot \frac{0.520}{0.797} \cong 0.294\text{ g}$$



# Application – Step 1



# Application - Step 2



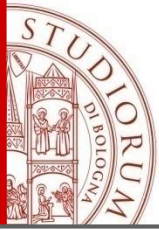
## STEP 2

Number of dampers per floor placed along the X-direction:  $n = 8$

Average damper inclination with respect to the horizontal line:  $\theta = 36^\circ$

Linear damping coefficient:

$$\begin{aligned}
 \bar{c}_L &= \bar{\zeta}_{visc} \cdot \omega_1 \cdot \frac{W_{tot}}{g} \cdot \left( \frac{N+1}{n} \right) \frac{1}{\cos^2 \theta} = \\
 &= 0.30 \cdot \frac{2\pi}{0.797s} \cdot \frac{16600 \text{ kN}}{9.81 \frac{m}{s^2}} \cdot \left( \frac{6+1}{8} \right) \cdot \frac{1}{\cos^2 36^\circ} \cong 5384 \frac{\text{kN} \cdot s}{m}
 \end{aligned}$$

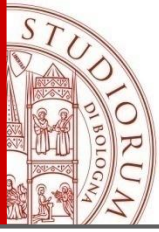


# Application - Step 3

## STEP 3

Peak damper **velocity** estimation for the equivalent linear damper:

$$\begin{aligned} v_{\max} &= \frac{S_e(T_1, \bar{\eta})}{\omega_1} \cdot \frac{2}{N+1} \cdot \cos \theta = \\ &= \frac{0.294 \cdot 9.81 \frac{\text{m}}{\text{s}^2}}{\left( \frac{2\pi}{0.797\text{s}} \right)} \cdot \frac{2}{6+1} \cdot \cos 36^\circ \cong 0.084 \frac{\text{m}}{\text{s}} \end{aligned}$$

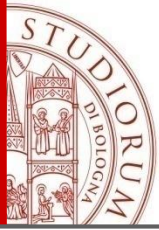


# Application - Step 3

## STEP 3

Peak damper **force** estimation for the single equivalent linear damper:

$$\begin{aligned} F_{L,\max} &= 2 \cdot \bar{\xi}_{visc} \cdot \frac{W}{g} \cdot \frac{S_e(T_1, \bar{\eta})}{n \cdot \cos \theta} = \\ &= 2 \cdot 0.30 \cdot \frac{16600 \text{ kN}}{g} \cdot \frac{0.294g}{8 \cdot \cos 36^\circ} \cong 454 \text{ kN} \end{aligned}$$

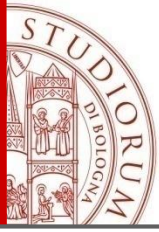


# Application - Step 3

## STEP 3

Peak damper **stroke** estimation for the equivalent linear damper:

$$\begin{aligned} s_{\max} &= \frac{S_e(T_1, \bar{\eta})}{\omega_1^2} \cdot \frac{2}{N+1} \cdot \cos \theta = \\ &= \frac{0.294 \cdot 981 \frac{\text{cm}}{\text{s}^2}}{\left(\frac{2\pi}{0.797\text{s}}\right)^2} \cdot \frac{2}{6+1} \cdot \cos 36^\circ \cong 1.07 \text{ cm} \end{aligned}$$



# Application - Step 4

## STEP 4

$\alpha$ -exponent of the commercial damper:  $\alpha = 0.15$

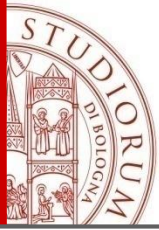
Non-linear damping coefficient of the commercial damper:

$$\begin{aligned}\overline{c}_{NL} &= \overline{c}_L \cdot (0.8 \cdot v_{\max})^{1-\bar{\alpha}} = \\ &= 5384 \frac{\text{kN} \cdot \text{s}}{\text{m}} \cdot \left(0.8 \cdot 0.084 \frac{\text{m}}{\text{s}}\right)^{1-0.15} \cong 544 \frac{\text{kN} \cdot \text{s}^{0.15}}{\text{m}^{0.15}}\end{aligned}$$

Minimum axial stiffness of the device (non-linear damper + supporting brace):

$$\begin{aligned}\overline{k}_{axial} &\geq 10 \cdot \overline{c}_L \cdot \omega_1 = \\ &= 10 \cdot 5384 \frac{\text{kN} \cdot \text{s}}{\text{m}} \cdot \frac{2\pi}{0.797\text{s}} = 4.24 \cdot 10^5 \frac{\text{kN}}{\text{m}} \longrightarrow 4.5 \cdot 10^5 \frac{\text{kN}}{\text{m}}\end{aligned}$$



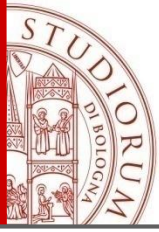


# Application - Step 4

## STEP 4

Peak damper **force** estimation for the single “non-linear” damper:

$$\begin{aligned} F_{NL,\max} &= 0.8^{1-\bar{\alpha}} \cdot F_{L,\max} = \\ &= 0.8^{1-0.15} \cdot 454 \text{ kN} \cong 375 \text{ kN} \end{aligned}$$



# Application - Step 5

## STEP 5

Peak **axial force** in the base column ( $i=1$ ):

$$P_{i,\max} = (N - i + 1) \cdot 0.8^{1-\bar{\alpha}} \cdot \frac{2 \cdot \bar{\xi}_{\text{visc}} \cdot m_{\text{tot}} \cdot S_e(T_1, \bar{\eta})}{n} \cdot \tan \theta$$

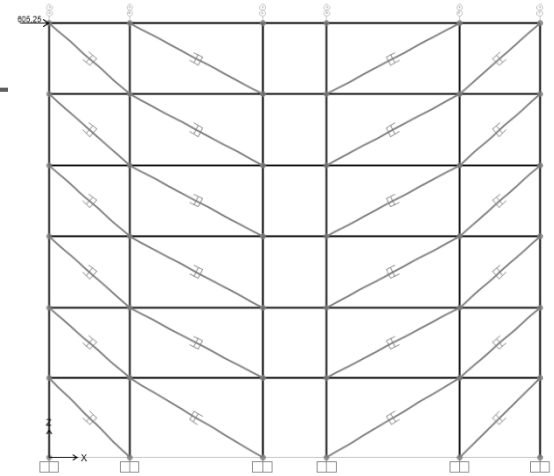
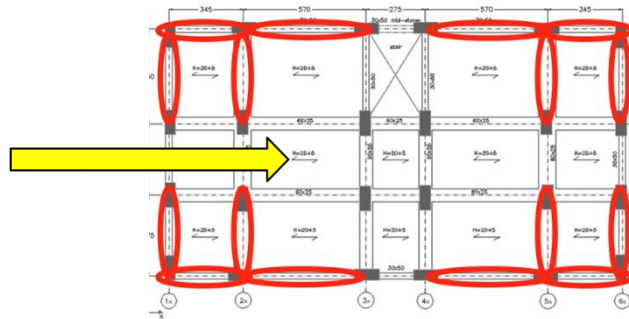
$$i = 1$$

$$P_{\text{base},\max} = P_{1,\max} = (6 - 1 + 1) \cdot 0.8^{1-0.15} \cdot \frac{2 \cdot 0.30 \cdot \frac{16600 \text{ kN}}{g} \cdot 0.294g}{8} \cdot \tan 36^\circ = 1332 \text{ kN}$$

# Application - Step 5

STEP 5

ESA2

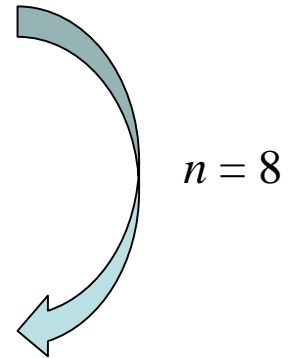


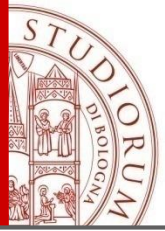
$$F_{D,h,max,struttura} = 0.8^{1-\bar{\alpha}} \cdot 2 \cdot \bar{\xi}_{visc} \cdot m_{tot} \cdot S_e(T_1, \bar{\eta})$$

$$F_{D,h,max,struttura} = 0.8^{1-0.15} \cdot 2 \cdot 0.30 \cdot \frac{16600 \text{ kN}}{g} \cdot 0.294 g = 2421 \text{ kN}$$

$$F_{D,h,max,specchiatura} = 0.8^{1-\bar{\alpha}} \cdot \frac{2 \cdot \bar{\xi}_{visc} \cdot m_{tot} \cdot S_e(T_1, \bar{\eta})}{n}$$

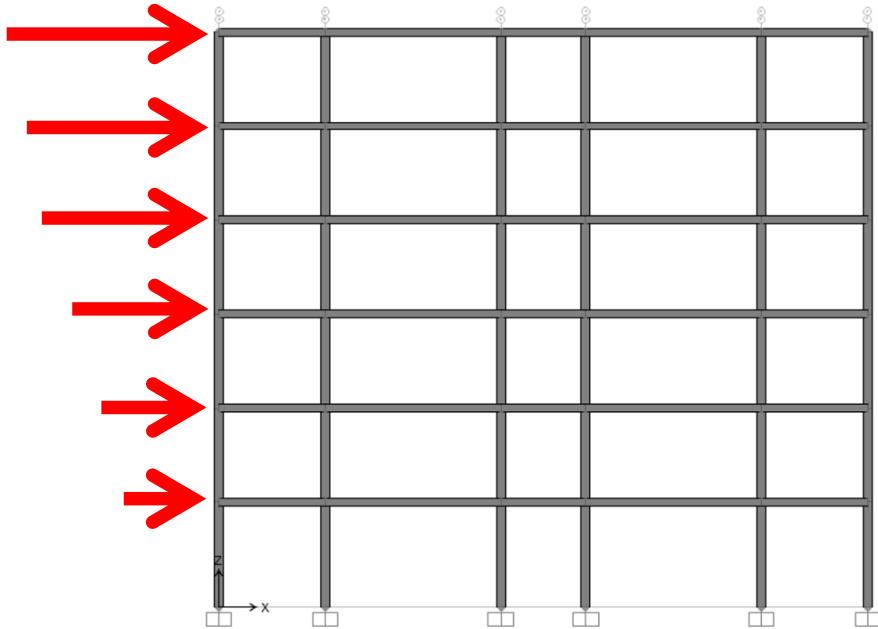
$$F_{D,h,max,specchiatura} = 0.8^{1-0.15} \cdot \frac{2 \cdot 0.30 \cdot \frac{16600 \text{ kN}}{g} \cdot 0.294 g}{8} = 303 \text{ kN}$$



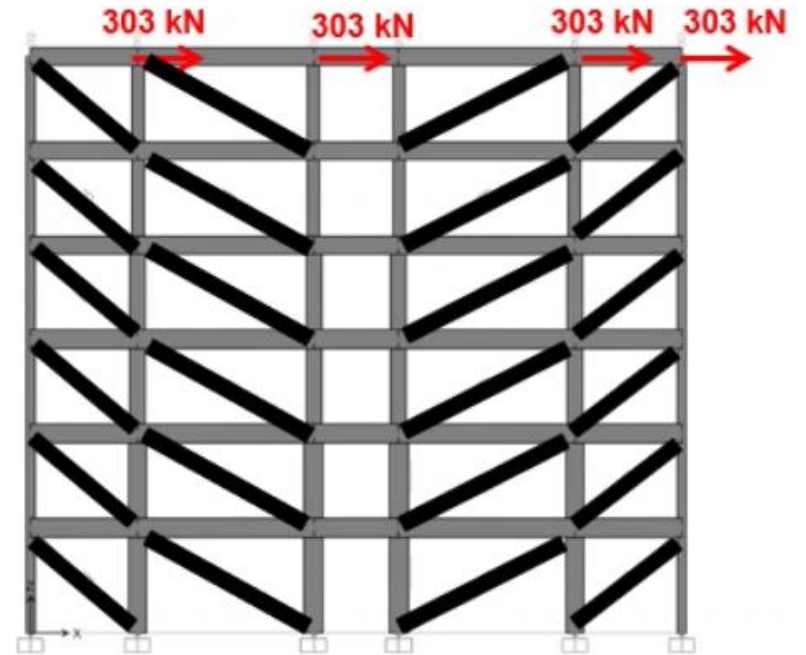


# Application - Step 5

$F_h \text{ tot} = 4877 \text{ kN}$

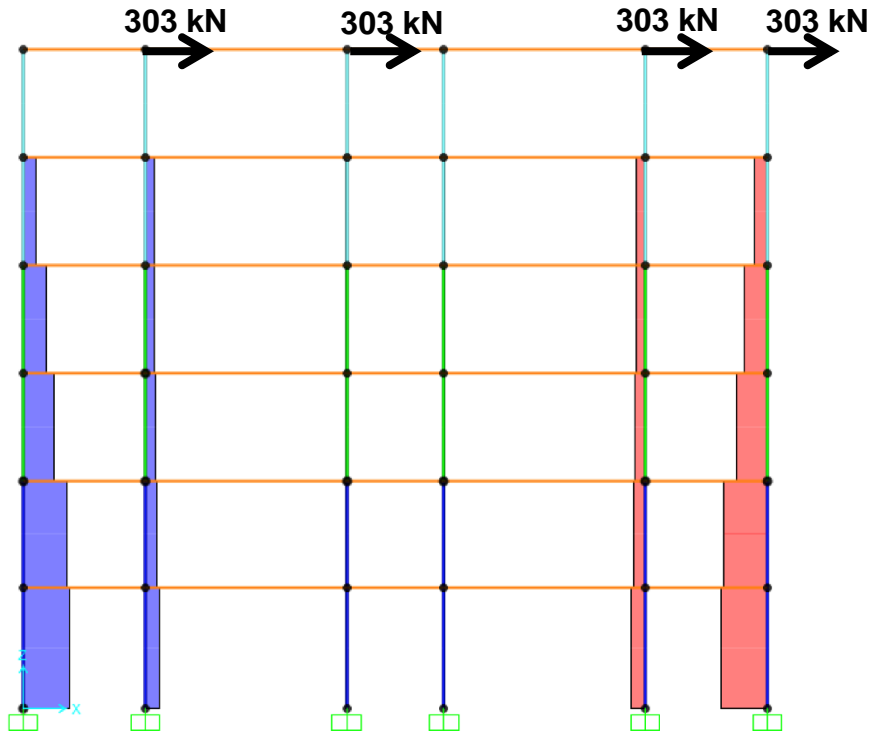


**ESA1**



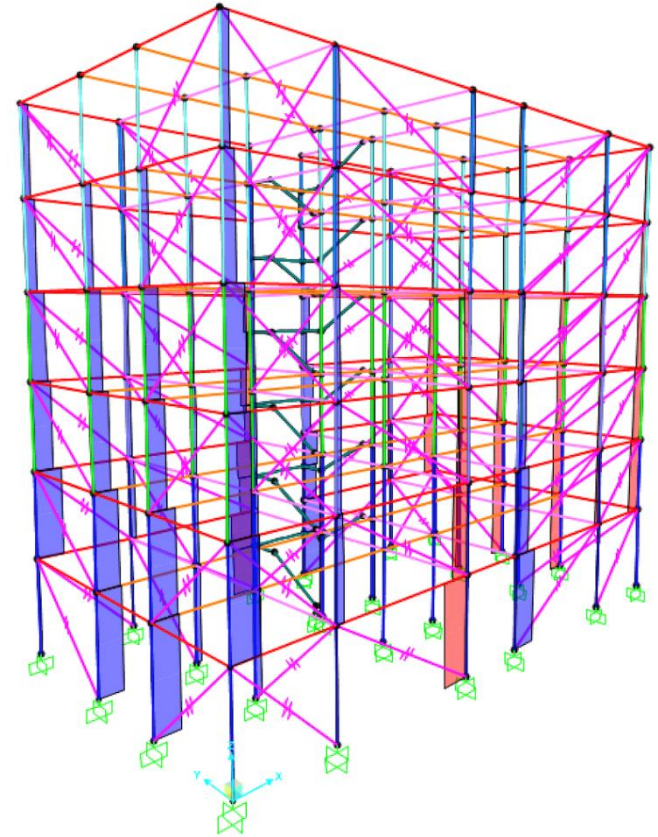
**ESA2**

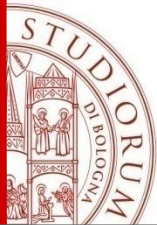
# Application - Step 5



**ESA2**

axial forces in  
the columns



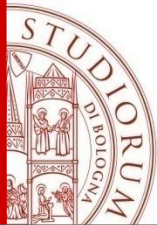


# XLS file of the procedure

		dir. long. (x)	dir. trasv. (y)	unità di misura
<b>STEP 1</b>				
smorzamento intrinseco	$\xi$ intr =	0,05	0,05	
smorzamento viscoso	$\xi$ visc =	0,30	0,30	
smorzamento totale di target	$\xi$ tot =	0,35	0,35	
fattore riduzione risposta di target	$\eta$ =	0,500	0,500	

<b>STEP 2</b>				
numero totale piani	N =	6	6	
peso totale struttura	Wtot =	16600	16600	kN
periodo fondamentale struttura	T1 =	0,797	0,704	s
pulsazione fondamentale struttura	$\omega$ 1 =	7,88	8,93	rad/s
numero di smorzatori per piano	n =	8	8	
inclinazione smorzatori	$\theta$ =	36	38	°
coefficiente smorzamento lineare	cL =	5384	6461	kNs/m
rigidezza assiale	kaxial =	infinita	infinita	

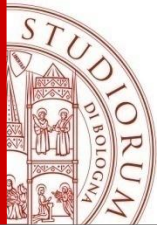




# XLS file of the procedure

STEP 3				
accelerazione spettrale	Sa(T1) =	0,294	0,333	g
coefficiente correttivo	M =	1,00	1,00	
velocità massima smorzatori lineari	vmax =	0,084	0,082	m/s
forza massima smorzatori lineari	FLmax =	454	529	kN
corsa massima pistone	smax =	1,07	0,92	cm

STEP 4				
esponente	$\alpha$ =	0,15	0,15	
coefficiente smorzamento non-lineare	cNL =	544	637	kN (s/m) <sup>a</sup>
forza massima smorzatori non-lineari	FNLmax =	375	437	kN
rigidezza assiale minima	kaxial >	424327	576634	kN/m

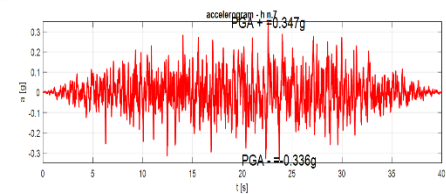
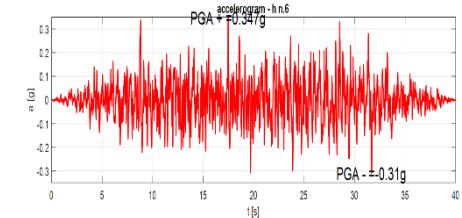
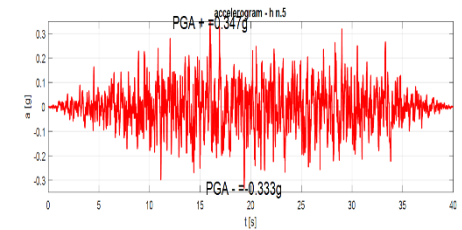
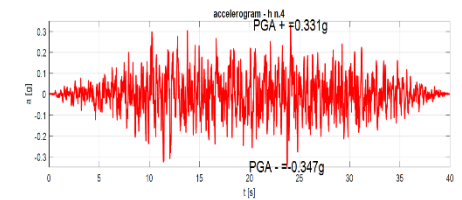
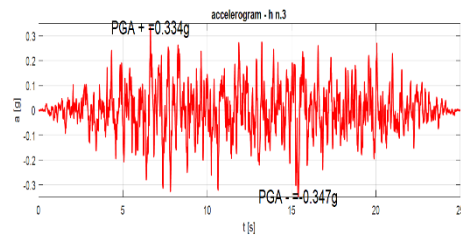
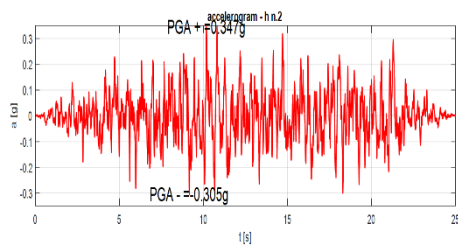
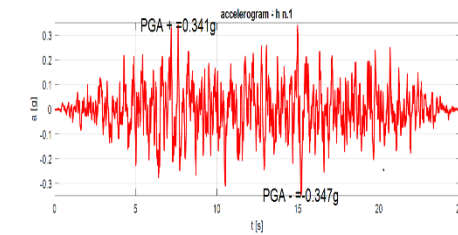
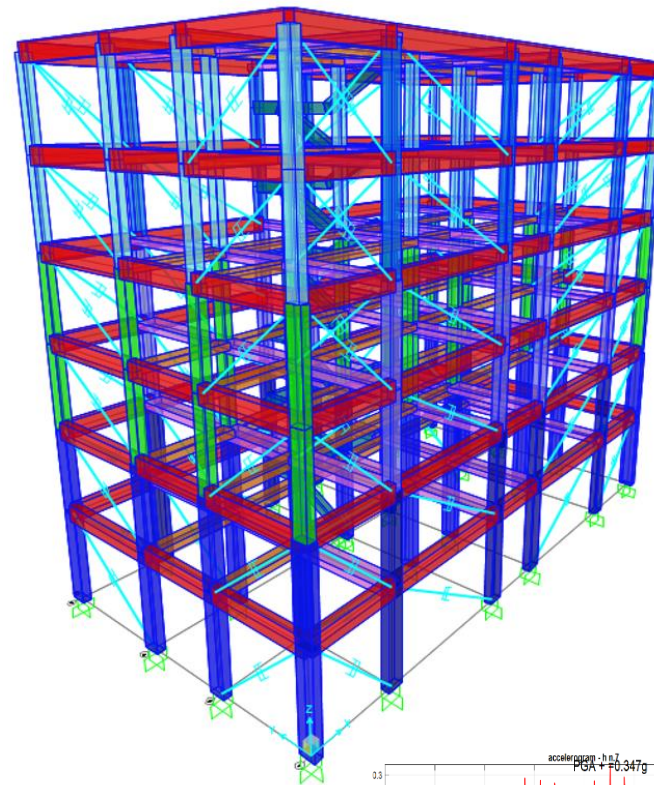


# XLS file of the procedure

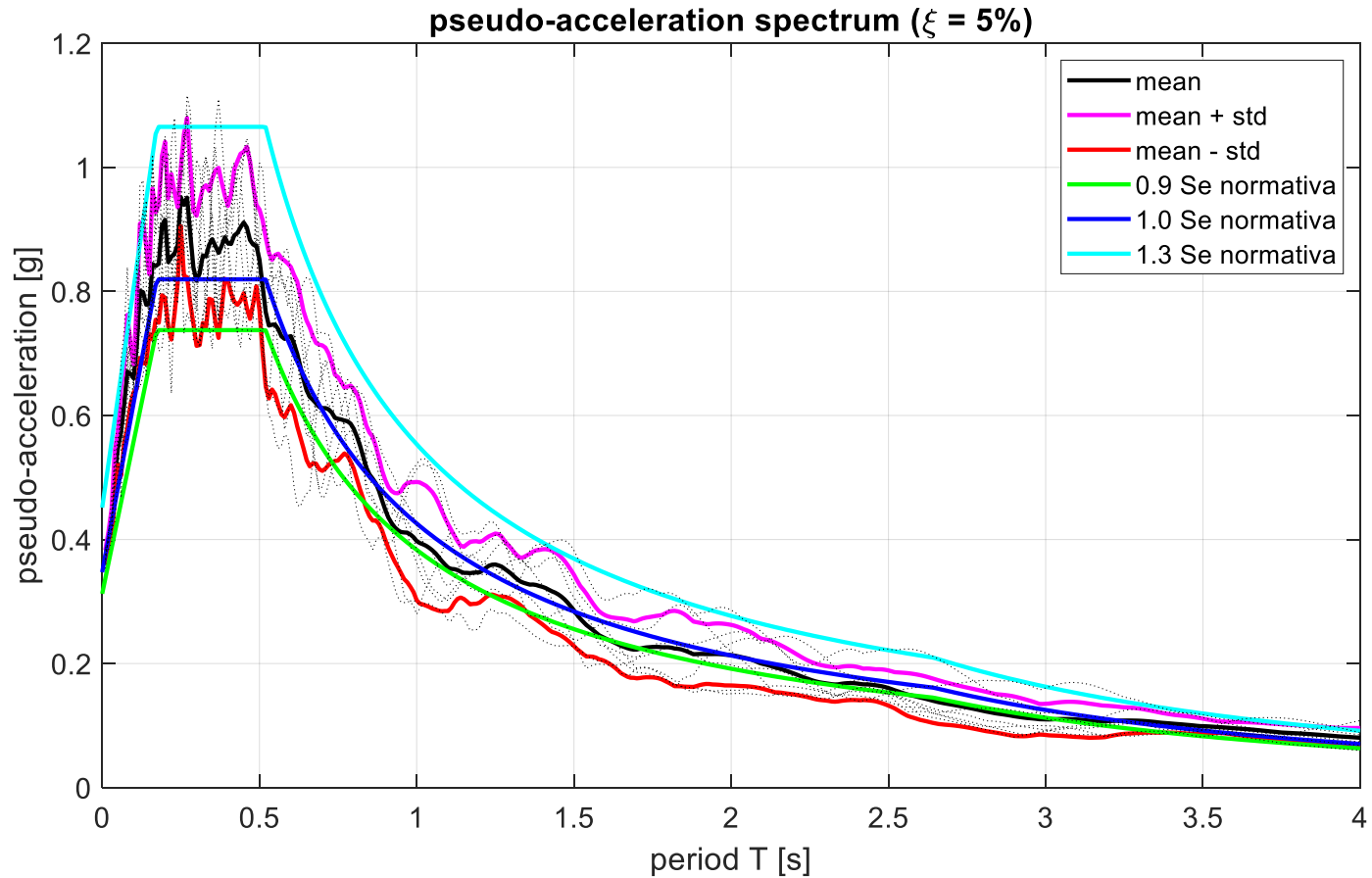
STEP 5				
<i>ESA1</i>				
forza totale	Fh =	4877	5523	kN
<i>ESA2</i>				
forza struttura	Fstructure =	2421	2741	kN
numero telai con smorzatori	n frames =	2	4	
forza telaio	Fframe =	1210	685	kN
numero specchiature con smorzatori nel telaio	n bays =	4	2	
forza specchiatura (singola reticolare)	Fbay =	303	343	kN
<i>sforzo normale max nelle colonne</i>				
	P1,max =	1332	1631	kN
	P2,max =	1110	1359	kN
	P3,max =	888	1088	kN
sforzo normale max alla base singola colonna	Pbase =	1332	1631	kN

# TH verification

7 artificial accelerograms which are consistent with the elastic spectrum:

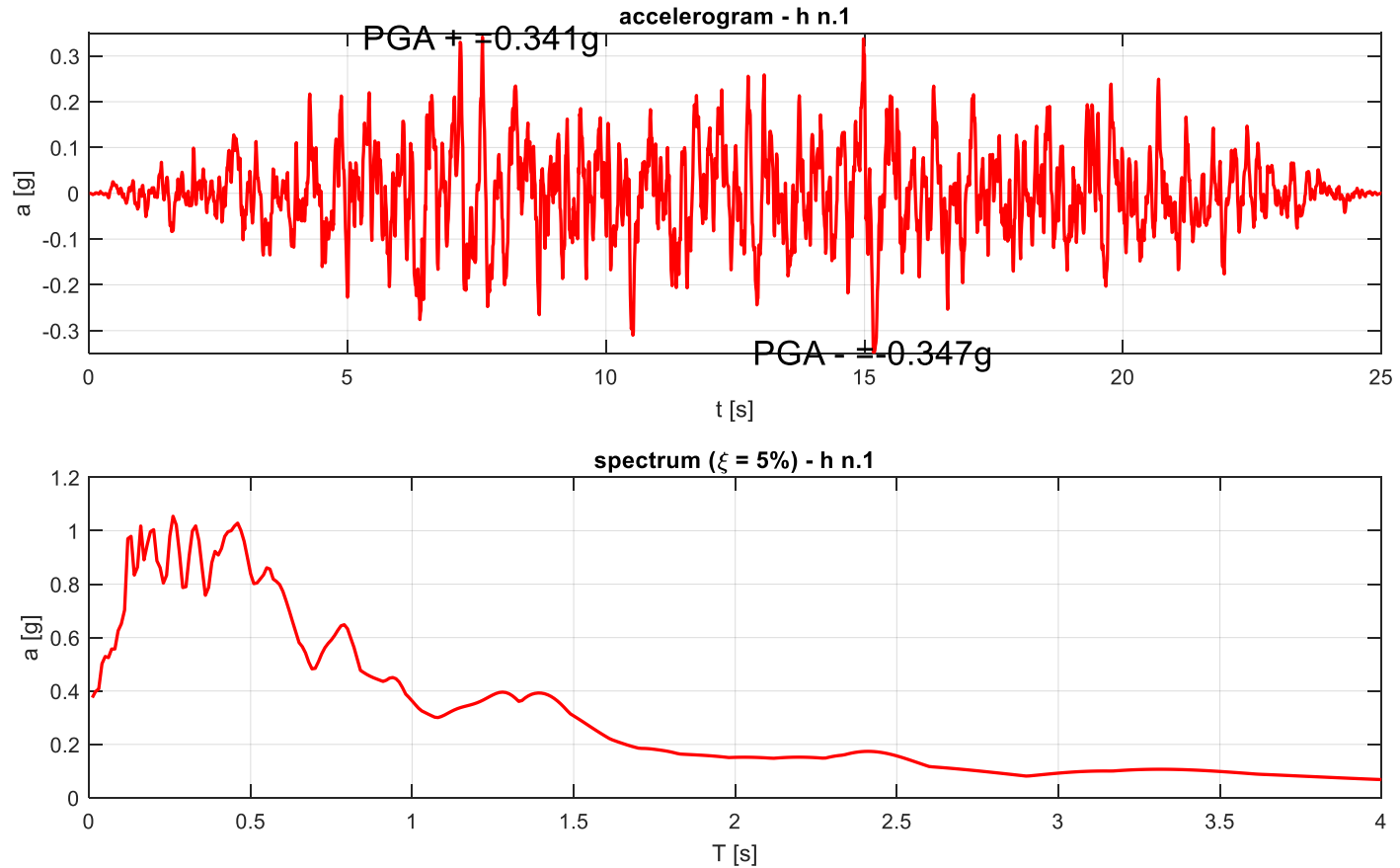


# TH verification



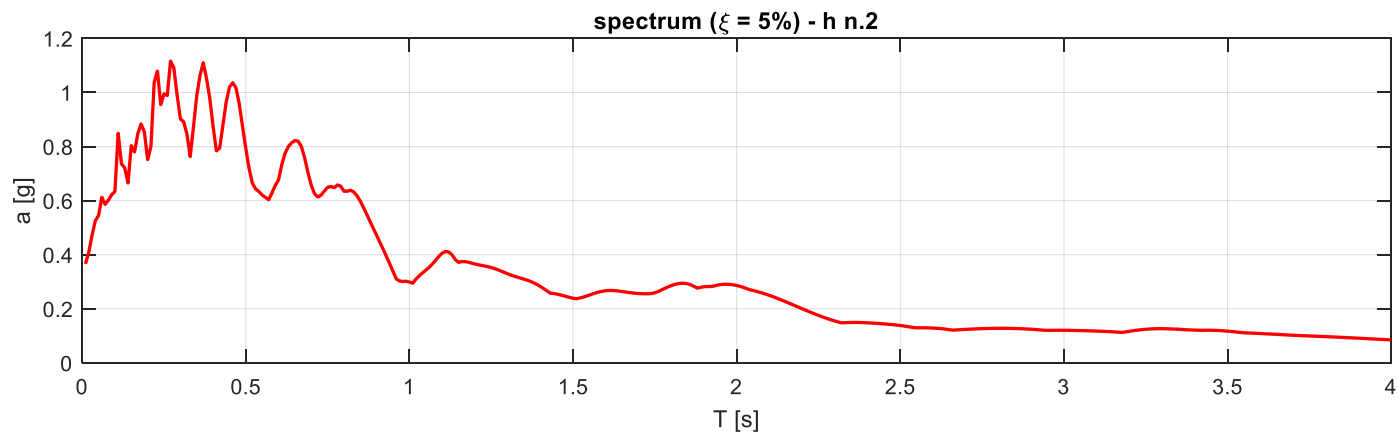
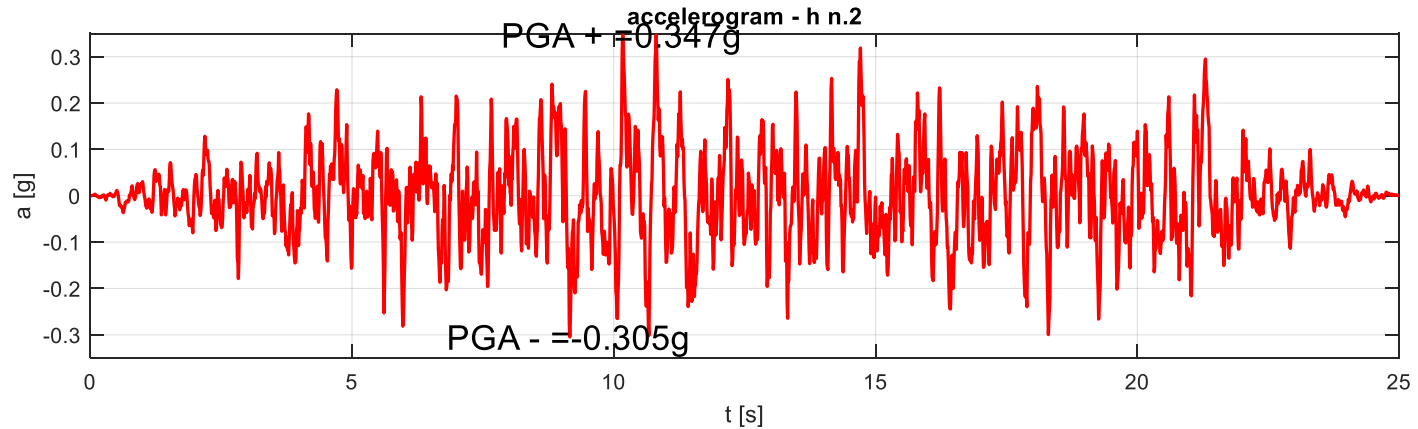
# TH verification

Ex: ground motion n.1

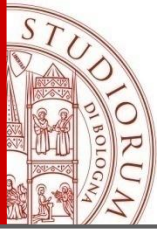


# TH verification

Ex: ground motion n.2

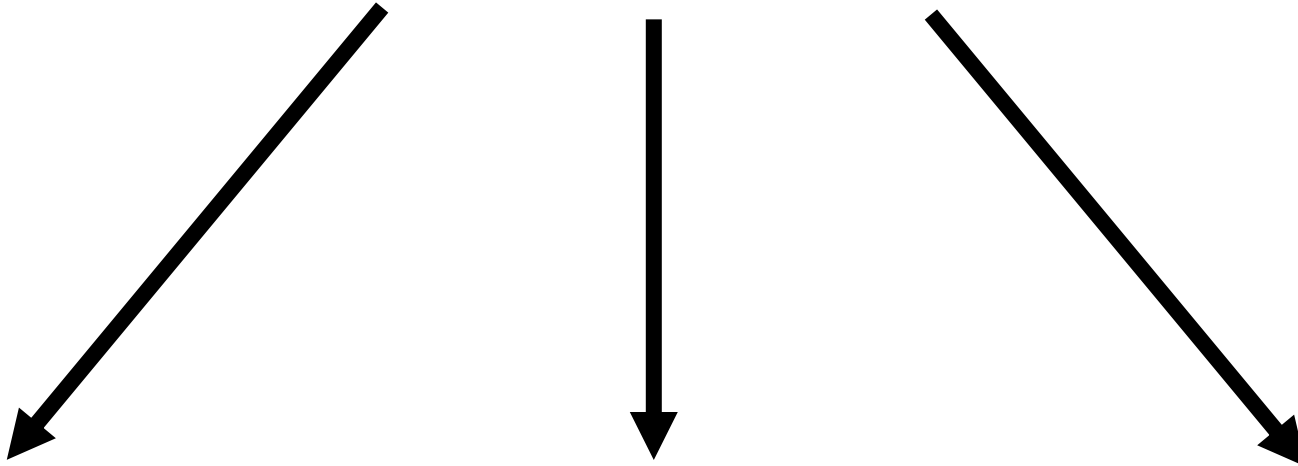






# TH verification

(comparison between models)



## Model DL

$$c_L = 5384 \frac{\text{kN} \cdot \text{s}}{\text{m}}$$

$$\alpha = 1$$

$$K = \infty$$

## Model DNL kinf

(with stiffness of dampers equal to infinity)

$$c_{NL} = 544 \frac{\text{kN} \cdot \text{s}^\alpha}{\text{m}^\alpha}$$

$$\alpha = 0.15$$

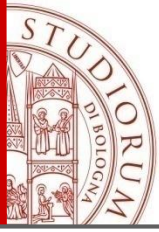
$$K = \infty$$

## Model DNL

$$c_{NL} = 544 \frac{\text{kN} \cdot \text{s}^\alpha}{\text{m}^\alpha}$$

$$\alpha = 0.15$$

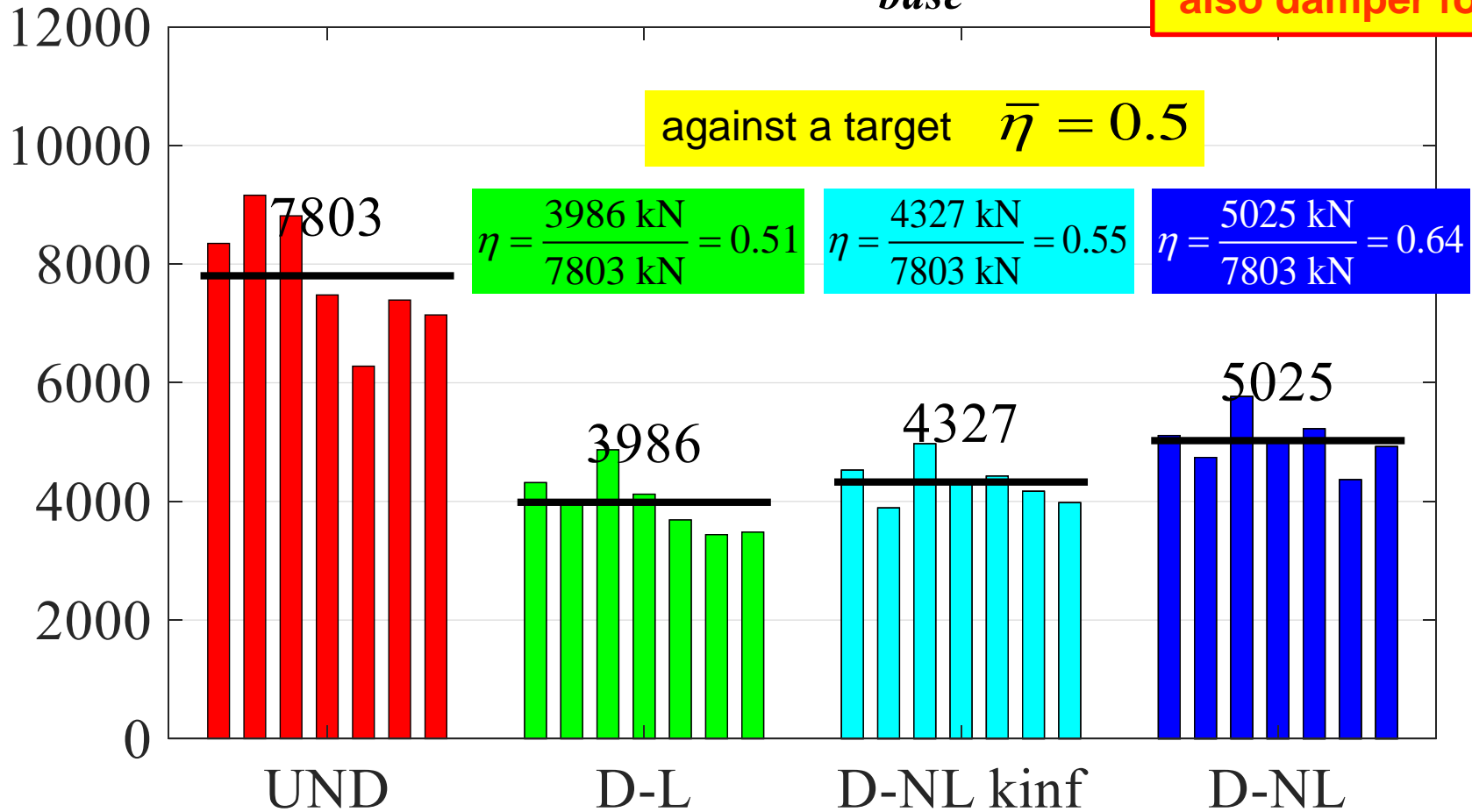
$$K = 4.5 \cdot 10^5 \frac{\text{kN}}{\text{m}}$$



# TH verification

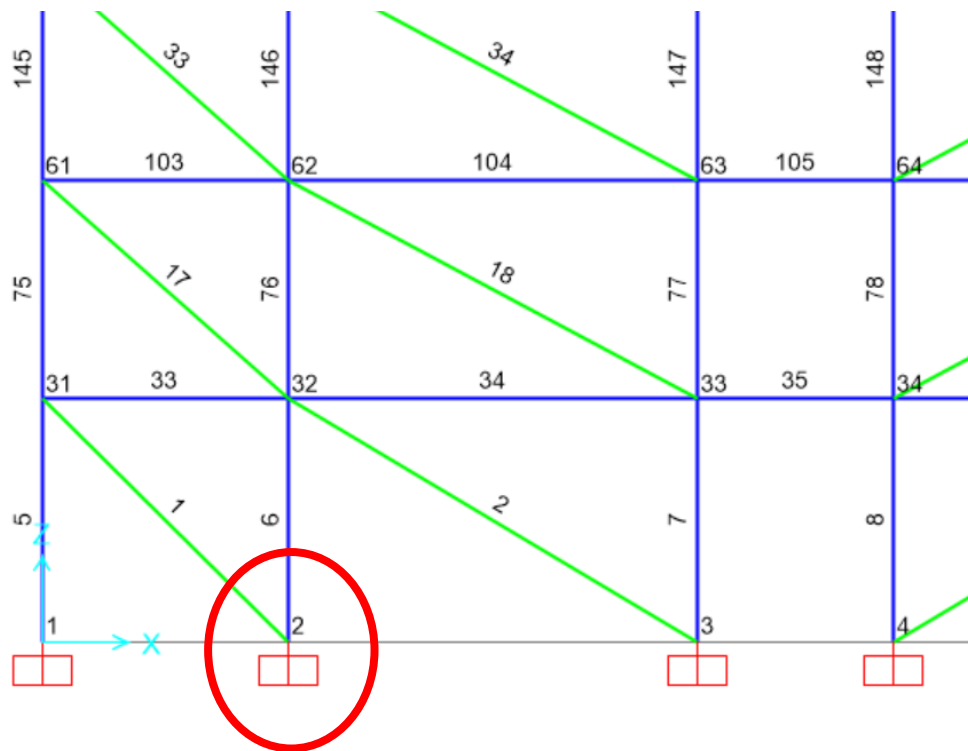
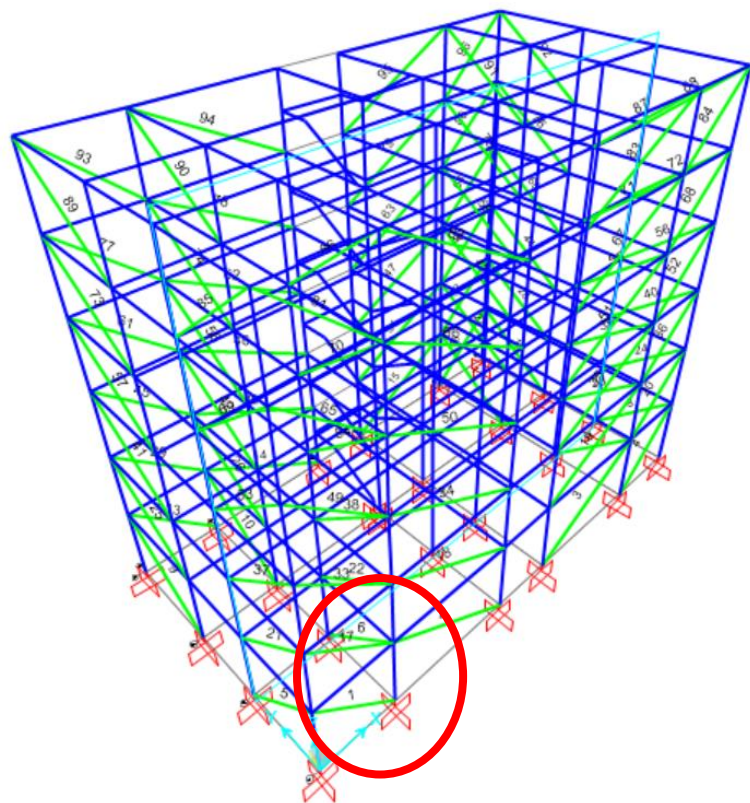
!!!  
Total base shear at the foundation level (including column shear forces and also damper forces)

long. dir. X  $V_{base}$  [kN]

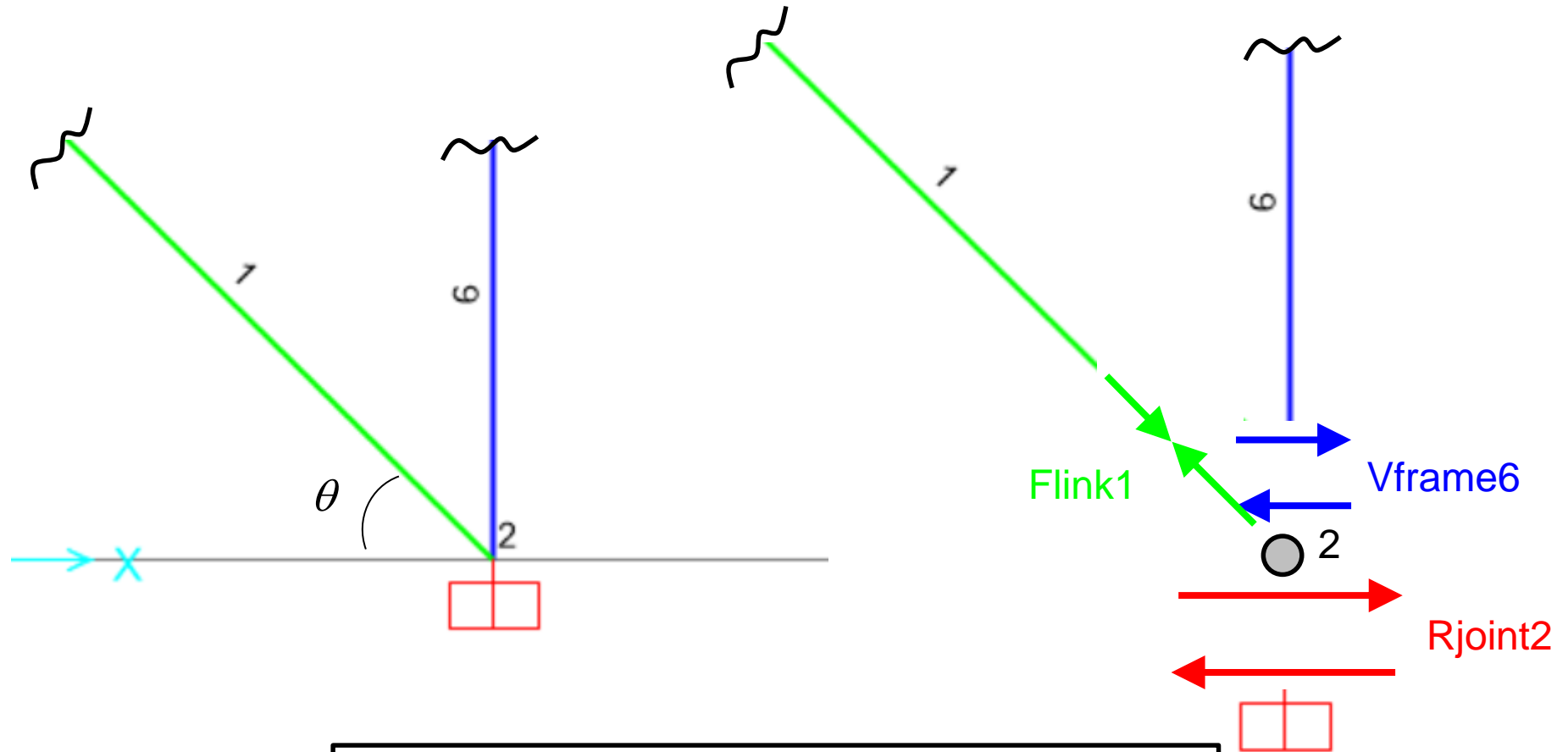


# TH verification

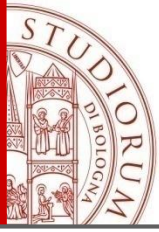
Model D-NL



# TH verification



$$R_{joint2} = V_{frame6} + F_{link1} \cdot \cos \theta$$

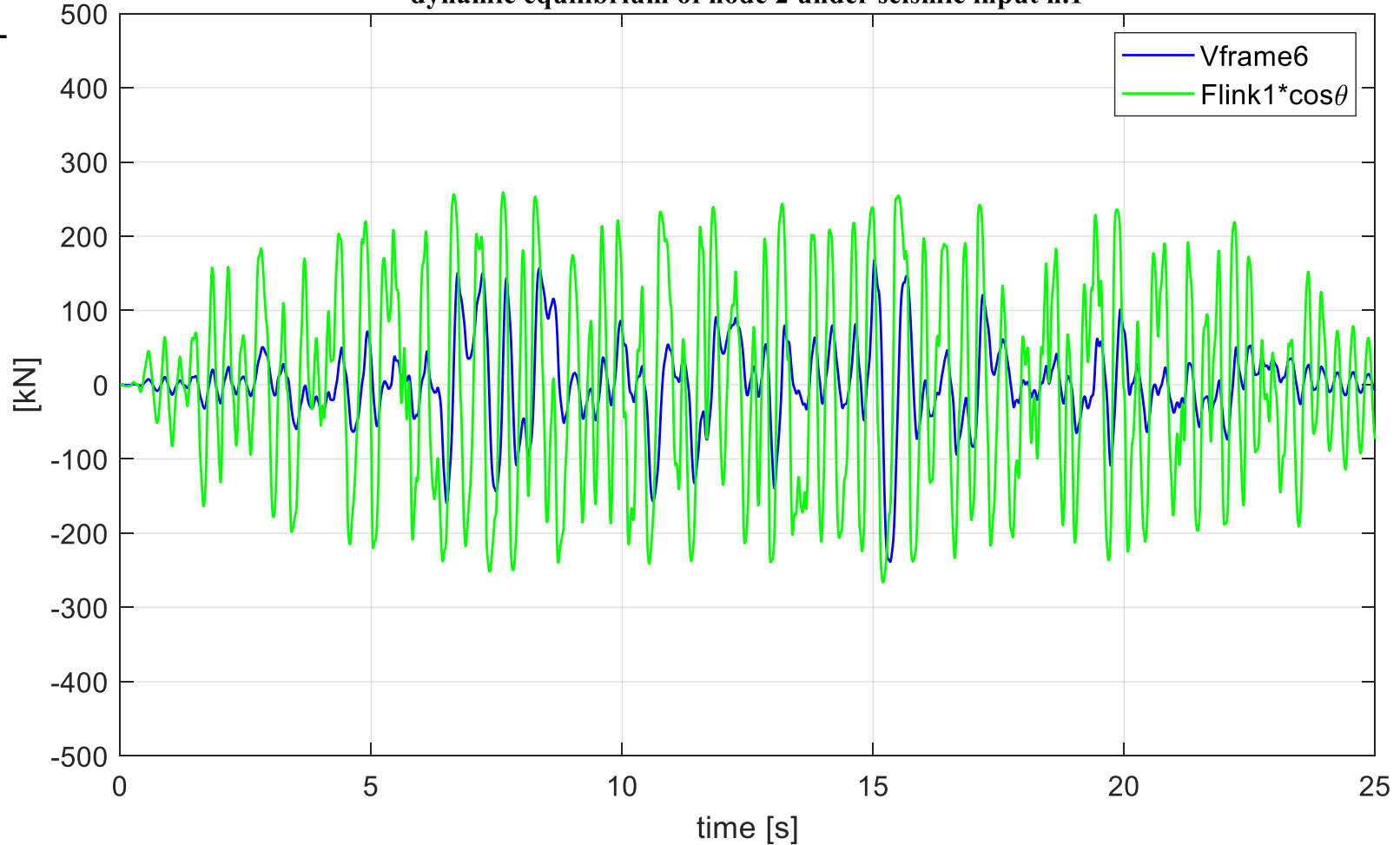


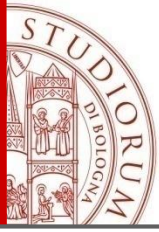
# TH verification

$$R_{\text{joint2}} = V_{\text{frame6}} + F_{\text{link1}} \cdot \cos \theta$$

Model  
D-NL

dynamic equilibrium of node 2 under seismic input n.1



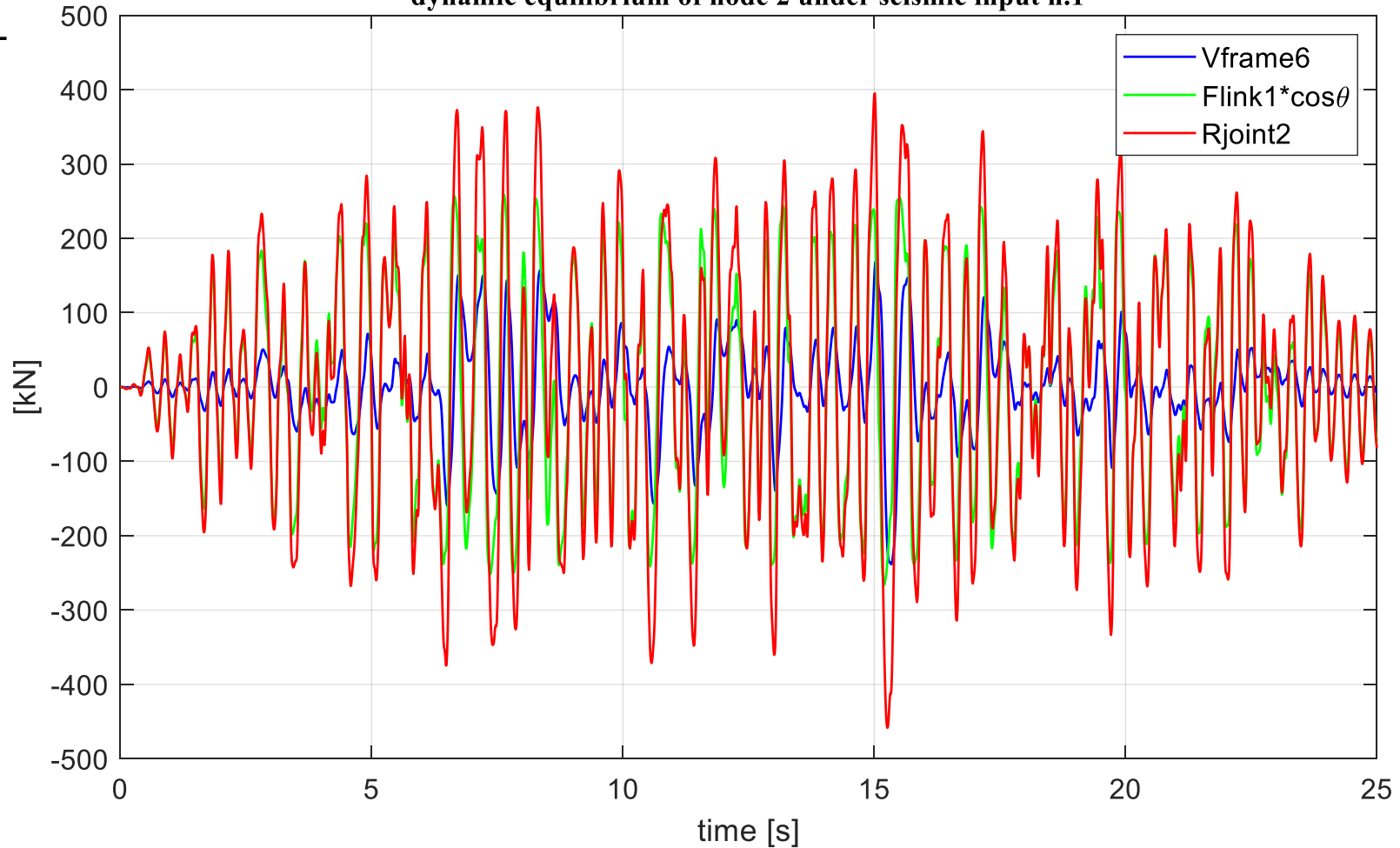


# TH verification

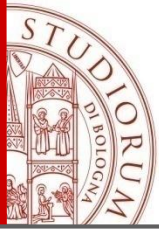
$$R_{\text{joint2}} = V_{\text{frame6}} + F_{\text{link1}} \cdot \cos \theta$$

Model  
D-NL

dynamic equilibrium of node 2 under seismic input n.1





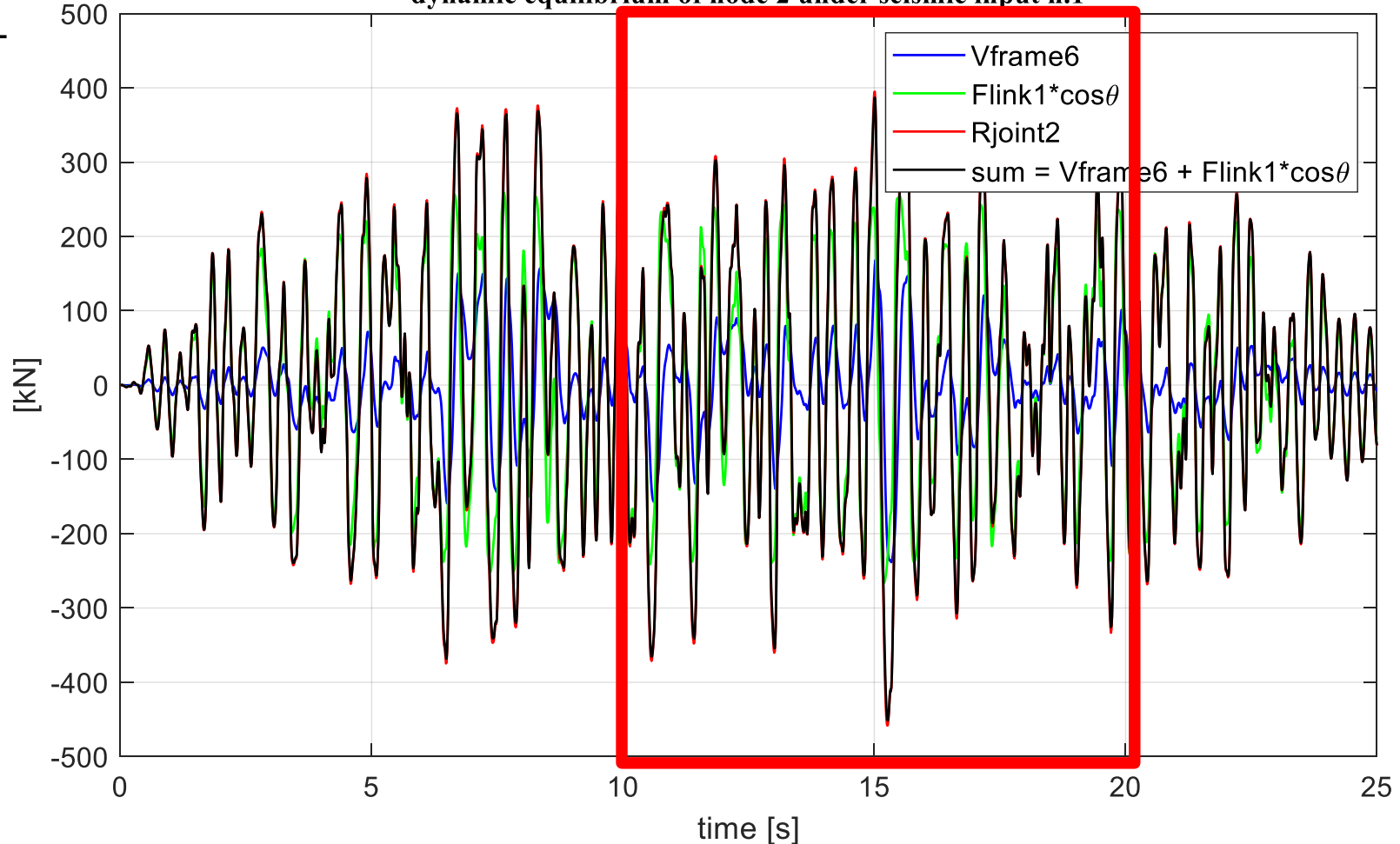


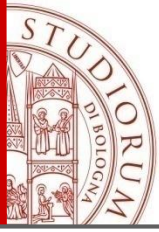
# TH verification

$$R_{\text{joint2}} = V_{\text{frame6}} + F_{\text{link1}} \cdot \cos \theta$$

Model  
D-NL

dynamic equilibrium of node 2 under seismic input n.1



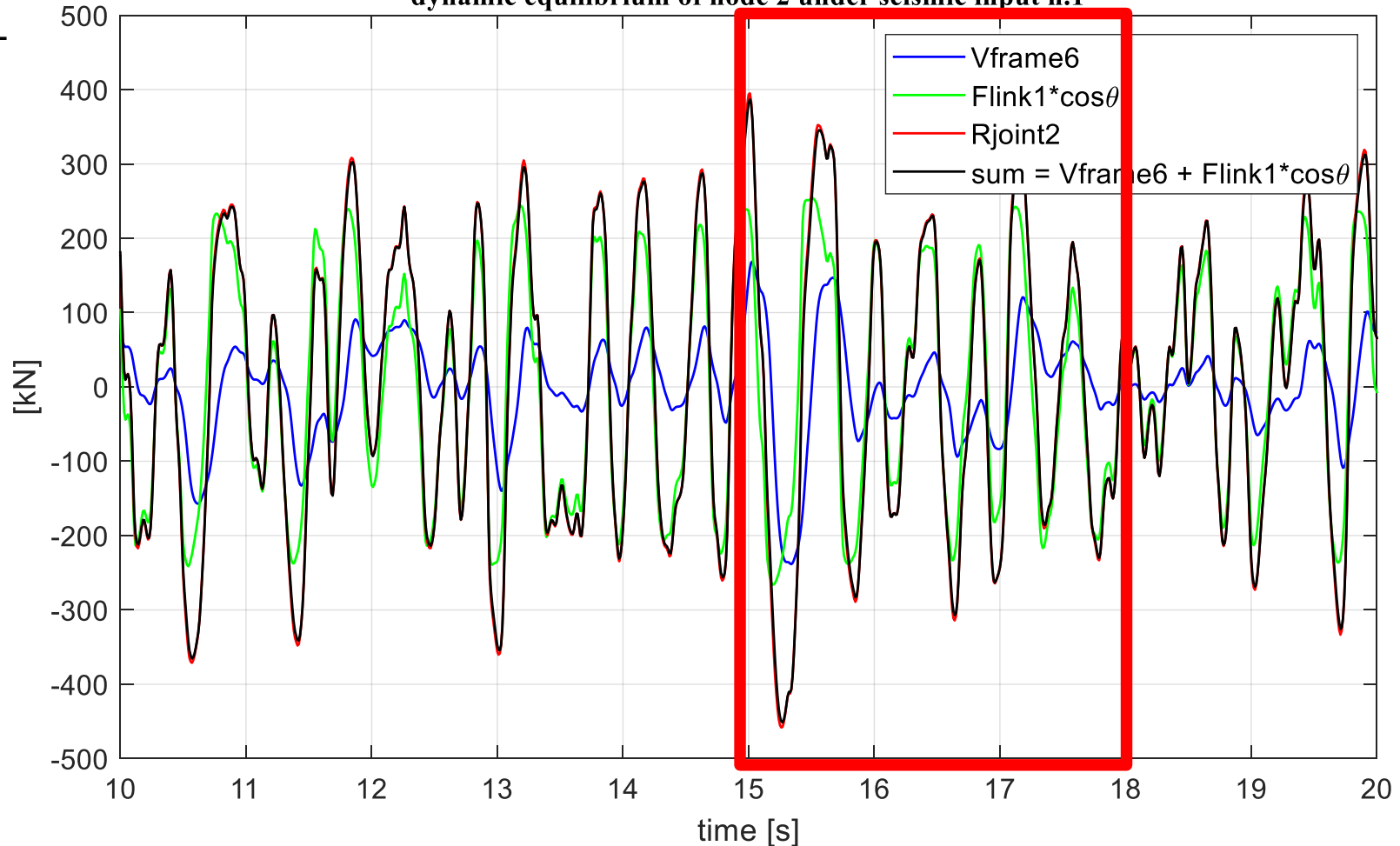


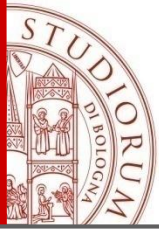
# TH verification

$$R_{\text{joint2}} = V_{\text{frame6}} + F_{\text{link1}} \cdot \cos \theta$$

Model  
D-NL

dynamic equilibrium of node 2 under seismic input n.1



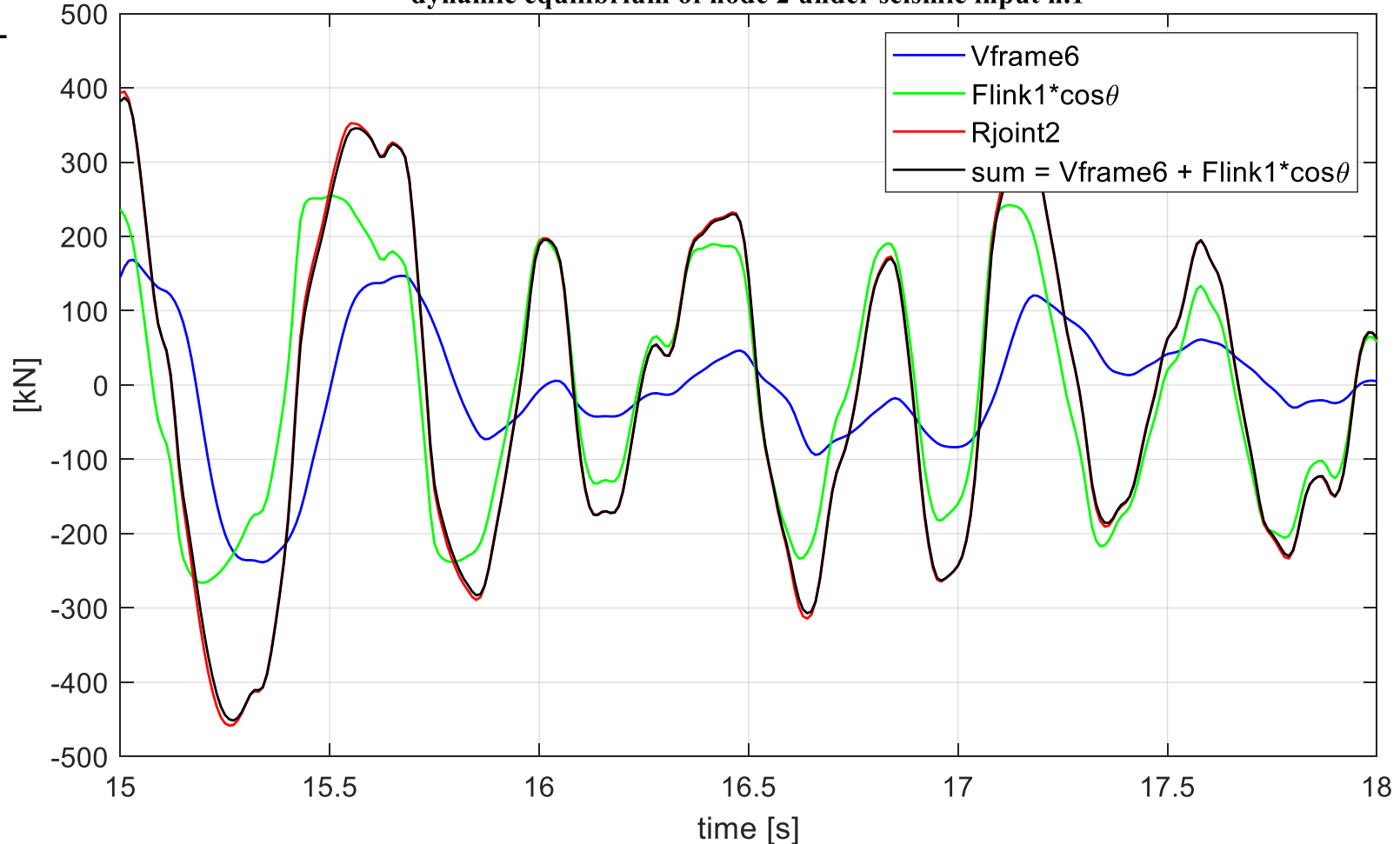


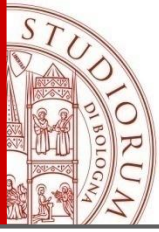
# TH verification

$$R_{\text{joint2}} = V_{\text{frame6}} + F_{\text{link1}} \cdot \cos \theta$$

Model  
D-NL

dynamic equilibrium of node 2 under seismic input n.1



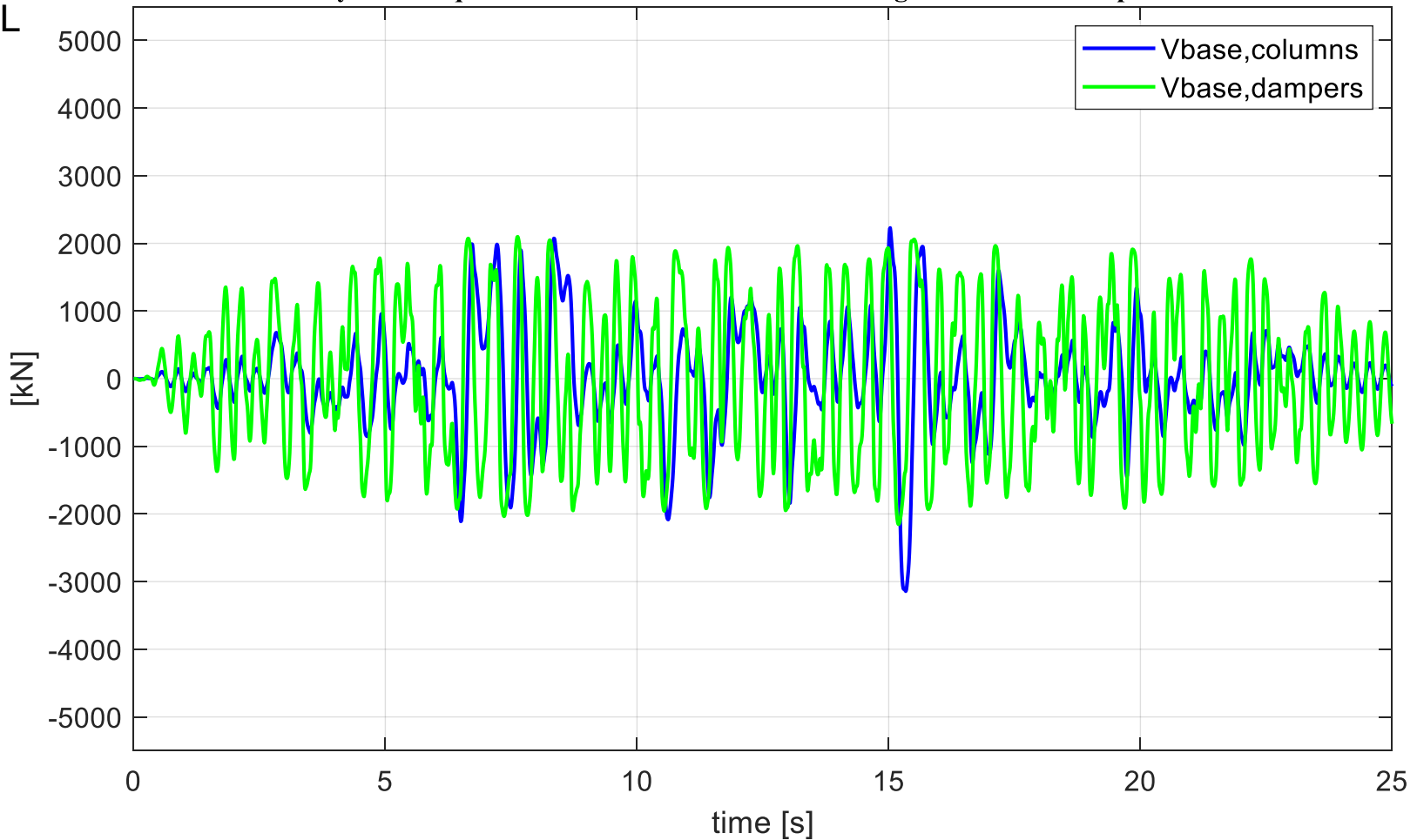


# TH verification

The same occurs  
for all  
ground floor joints

Model  
D-NL

dynamic equilibrium of the base of the building under seismic input n.1

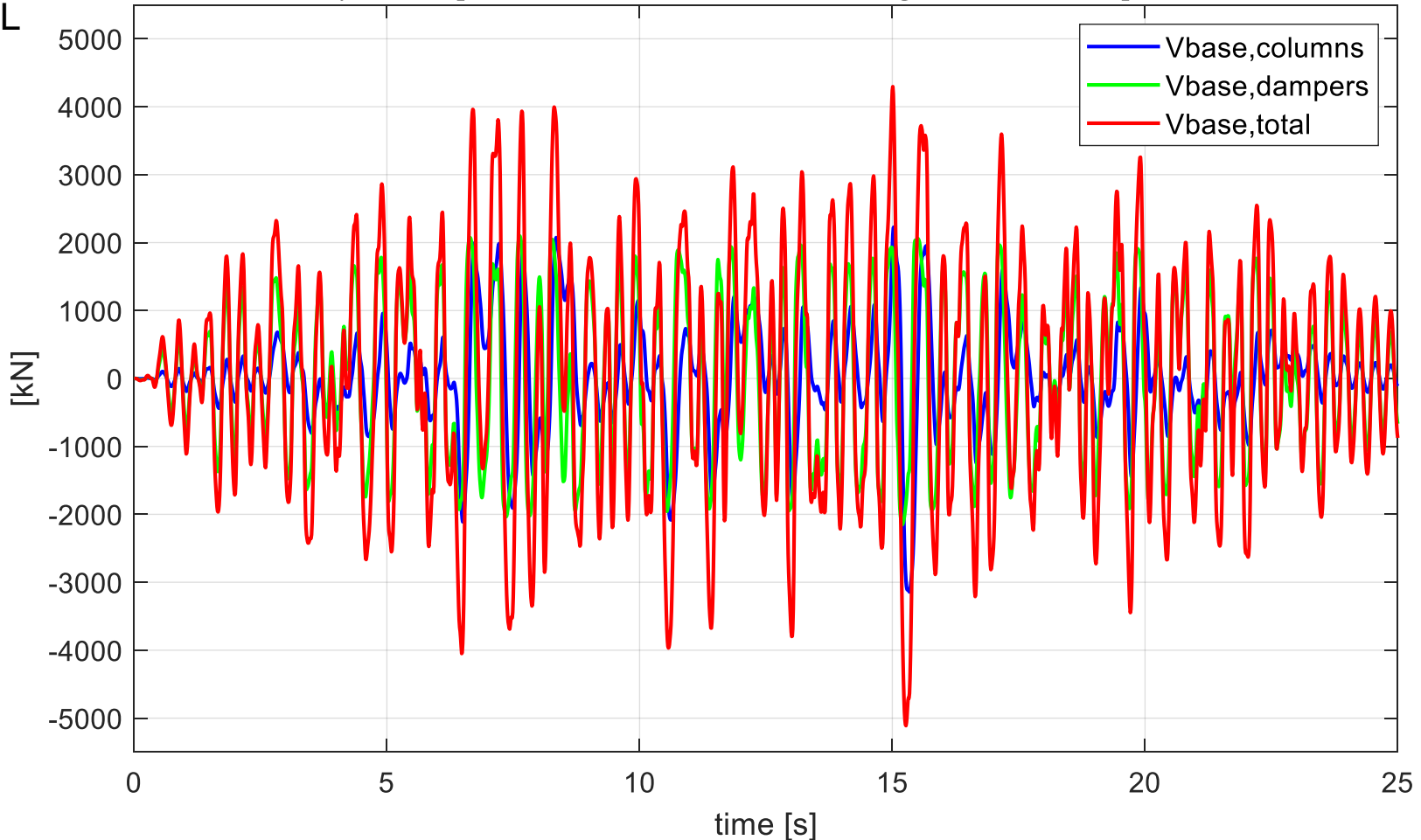


# TH verification

The same occurs  
for all  
ground floor joints

Model  
D-NL

dynamic equilibrium of the base of the building under seismic input n.1

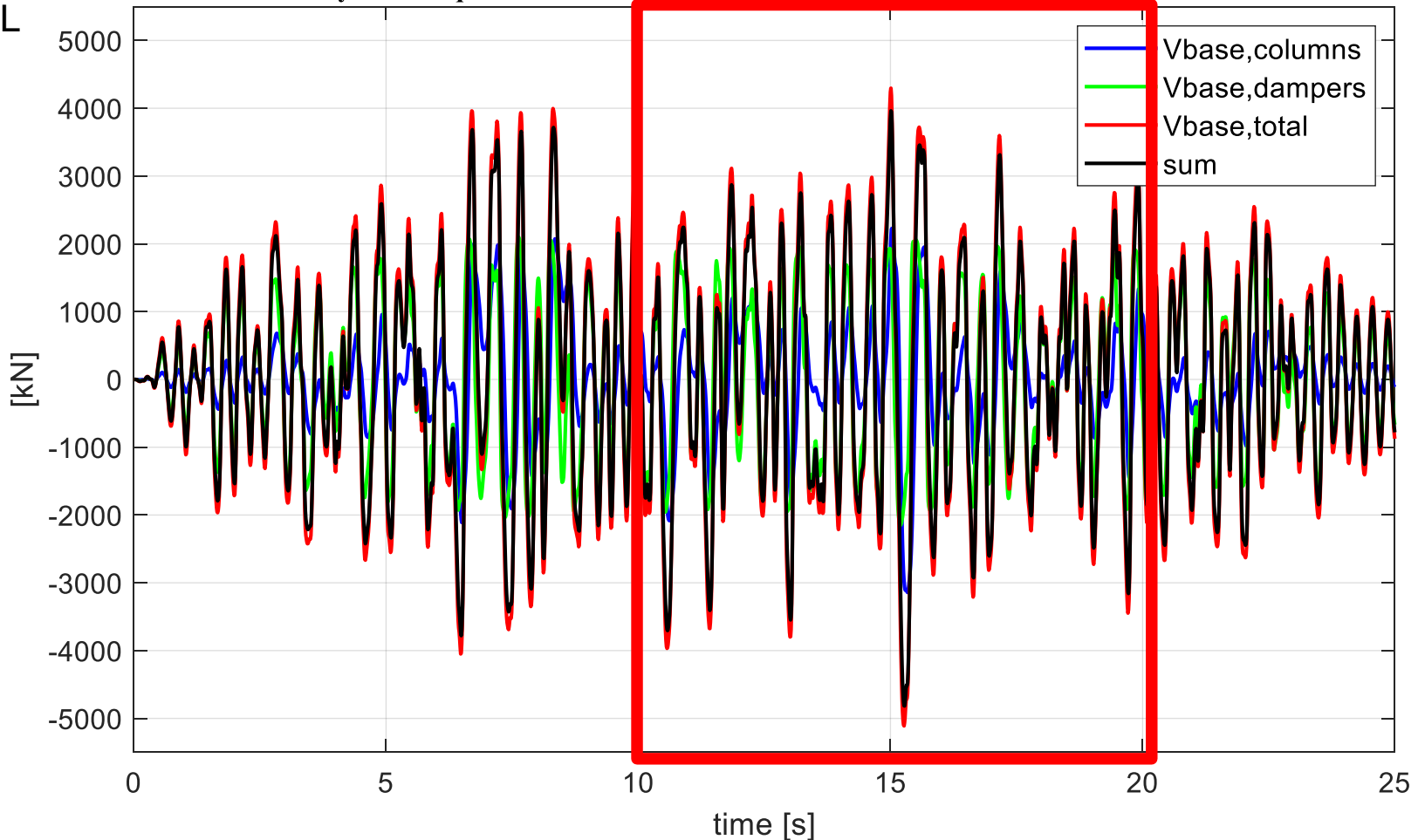


# TH verification

The same occurs  
for all  
ground floor joints

Model  
D-NL

dynamic equilibrium of the base of the building under seismic input n.1



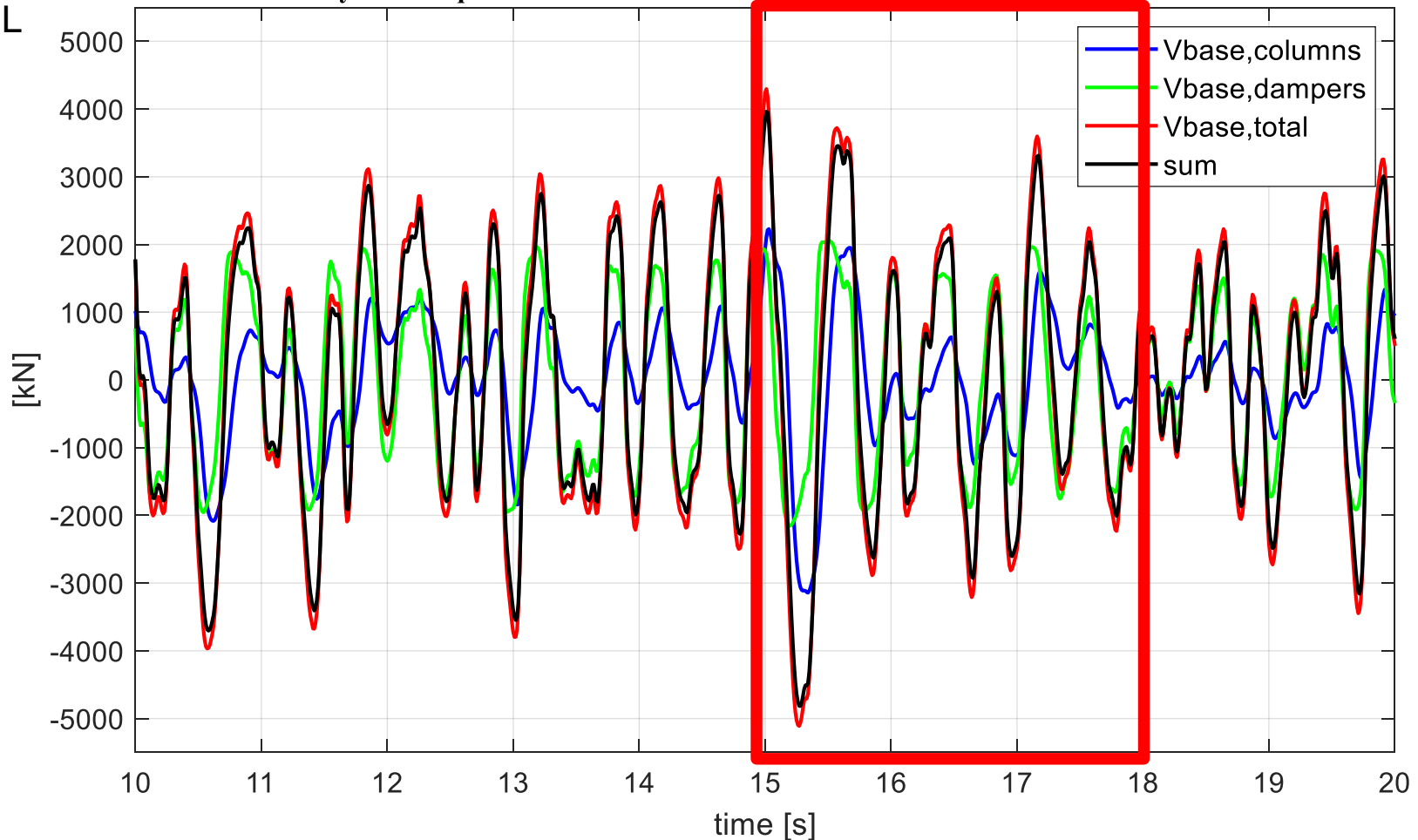


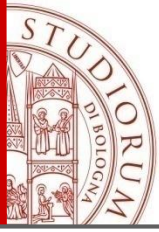
# TH verification

The same occurs  
for all  
ground floor joints

Model  
D-NL

dynamic equilibrium of the base of the building under seismic input n.1



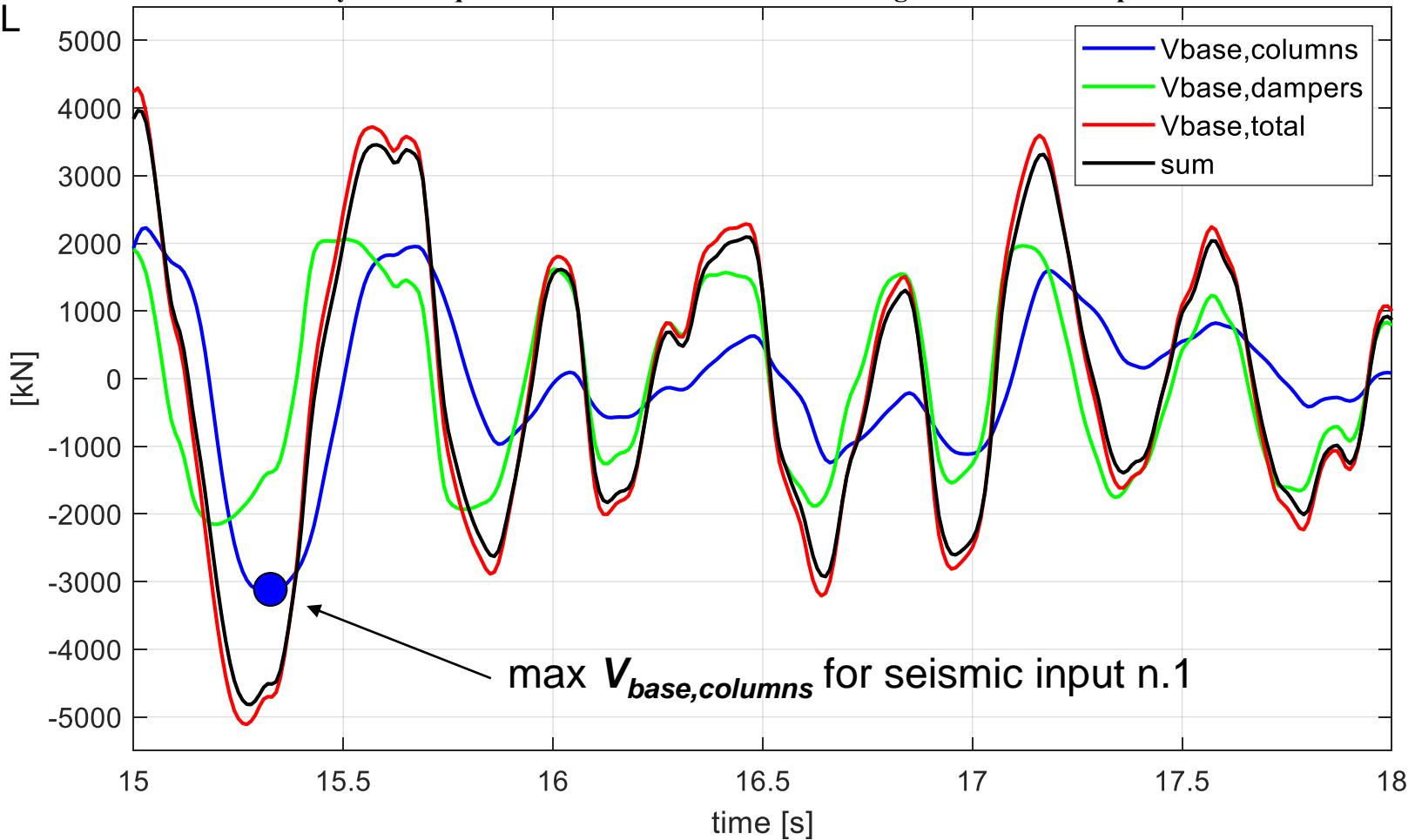


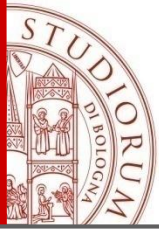
# TH verification

The same occurs for all ground floor joints

Model D-NL

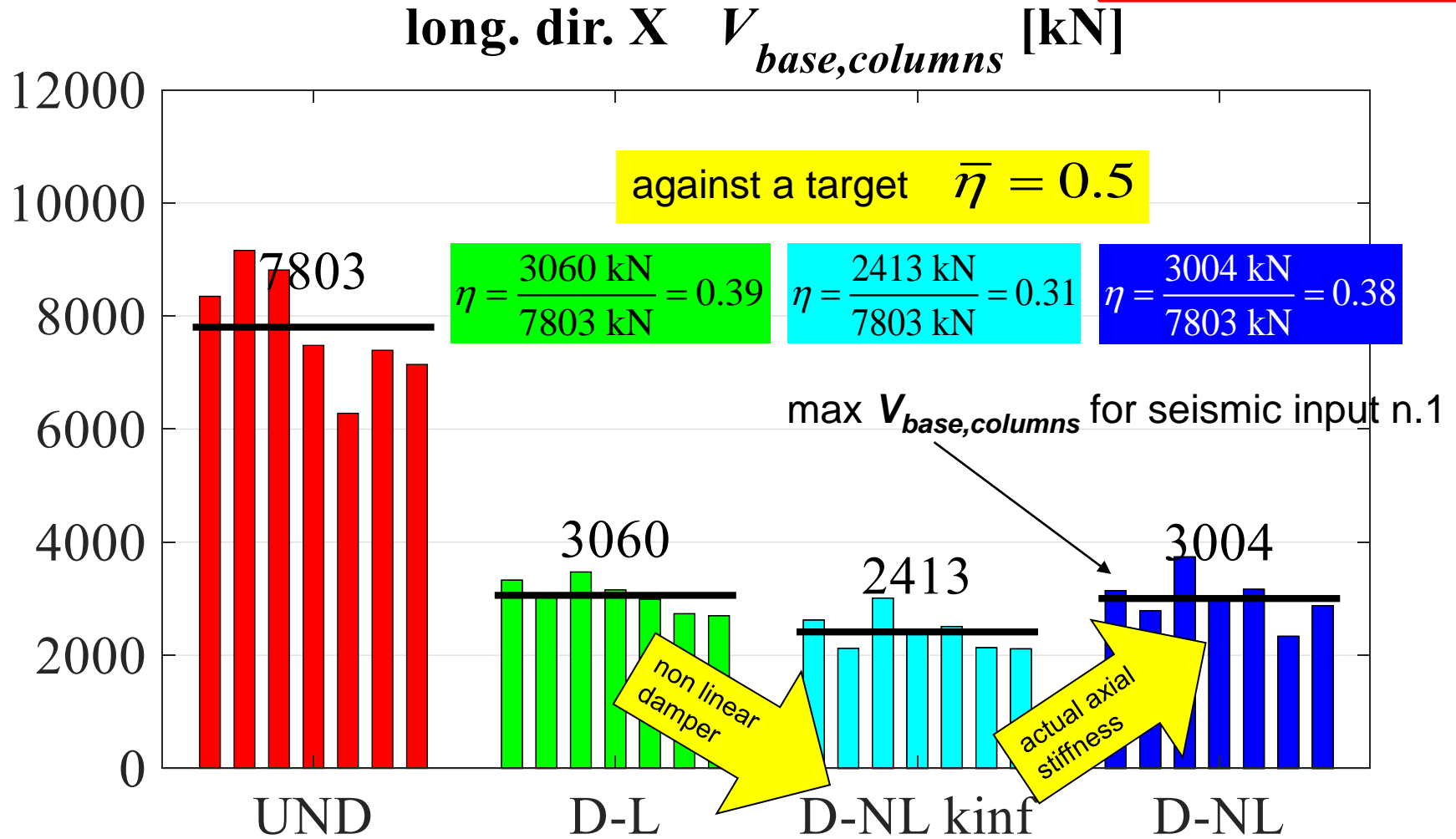
dynamic equilibrium of the base of the building under seismic input n.1





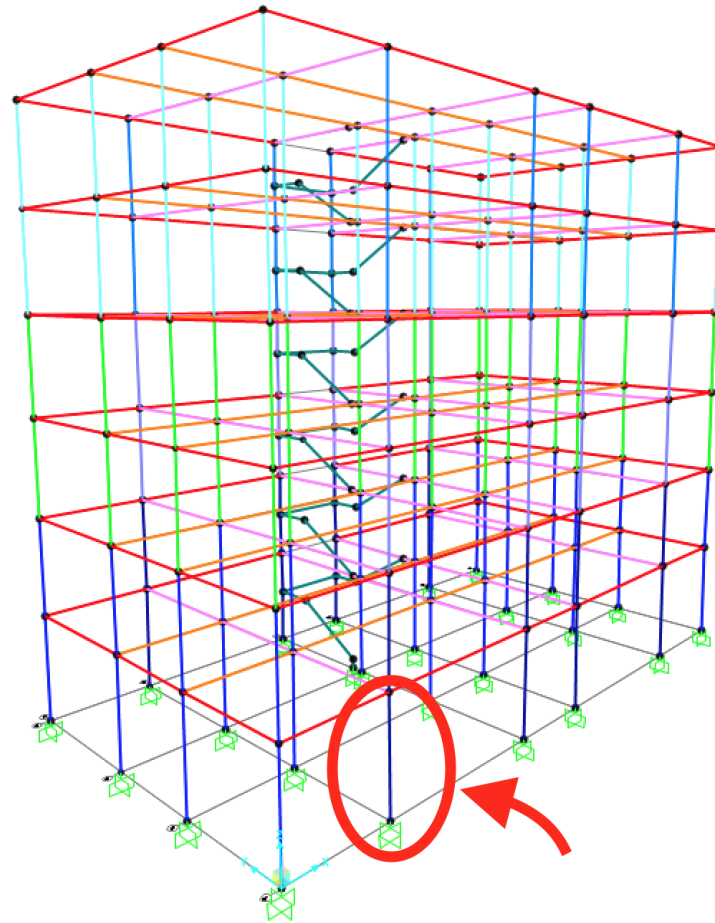
# TH verification

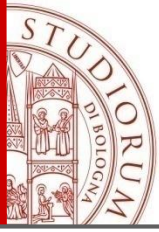
!!!  
Sum of base shear forces in the columns



# TH verification

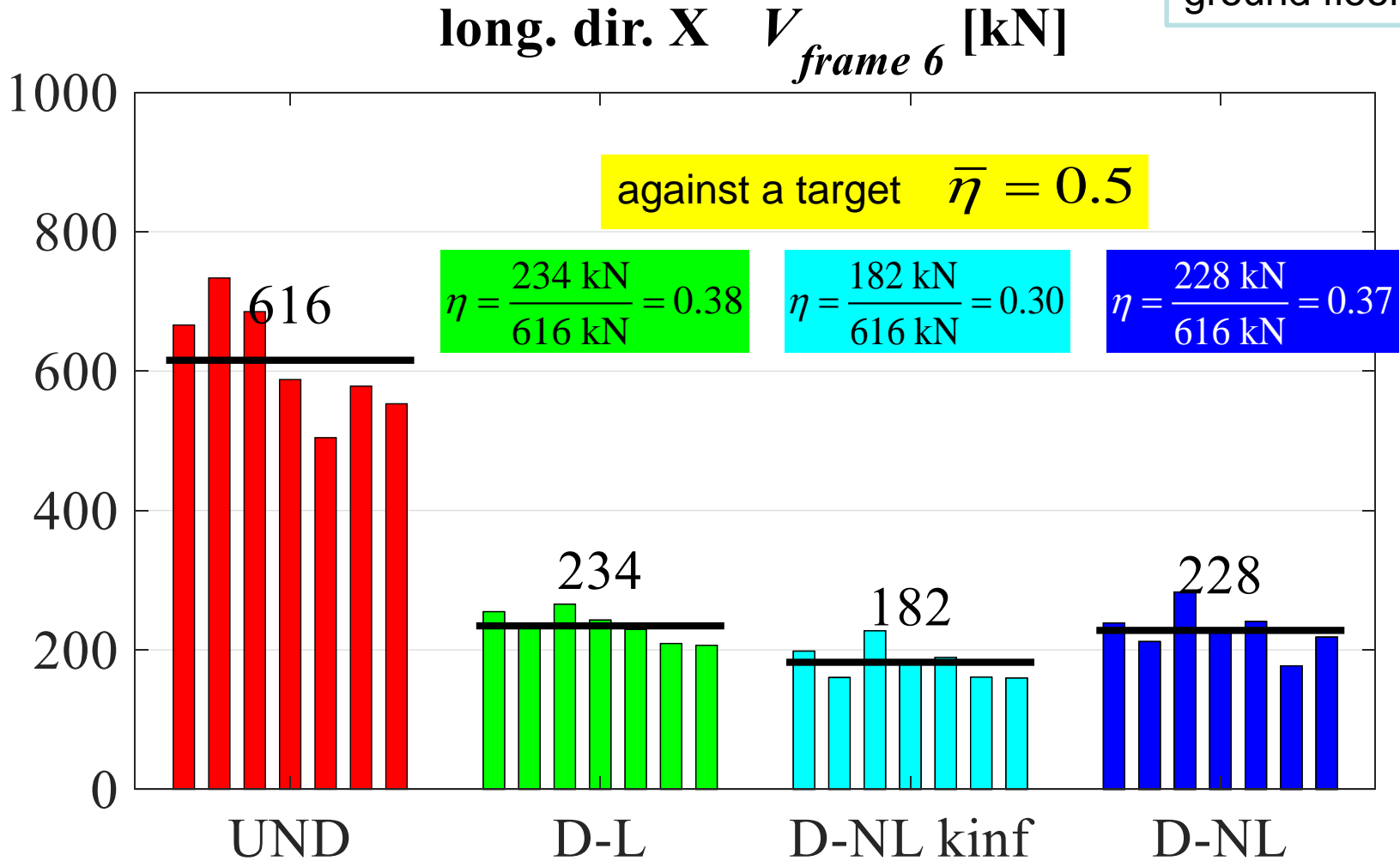
FOCUS on the most stressed column at the ground floor

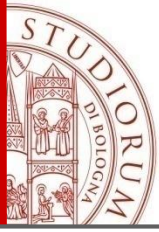




# TH verification

FOCUS on the most stressed column at the ground floor

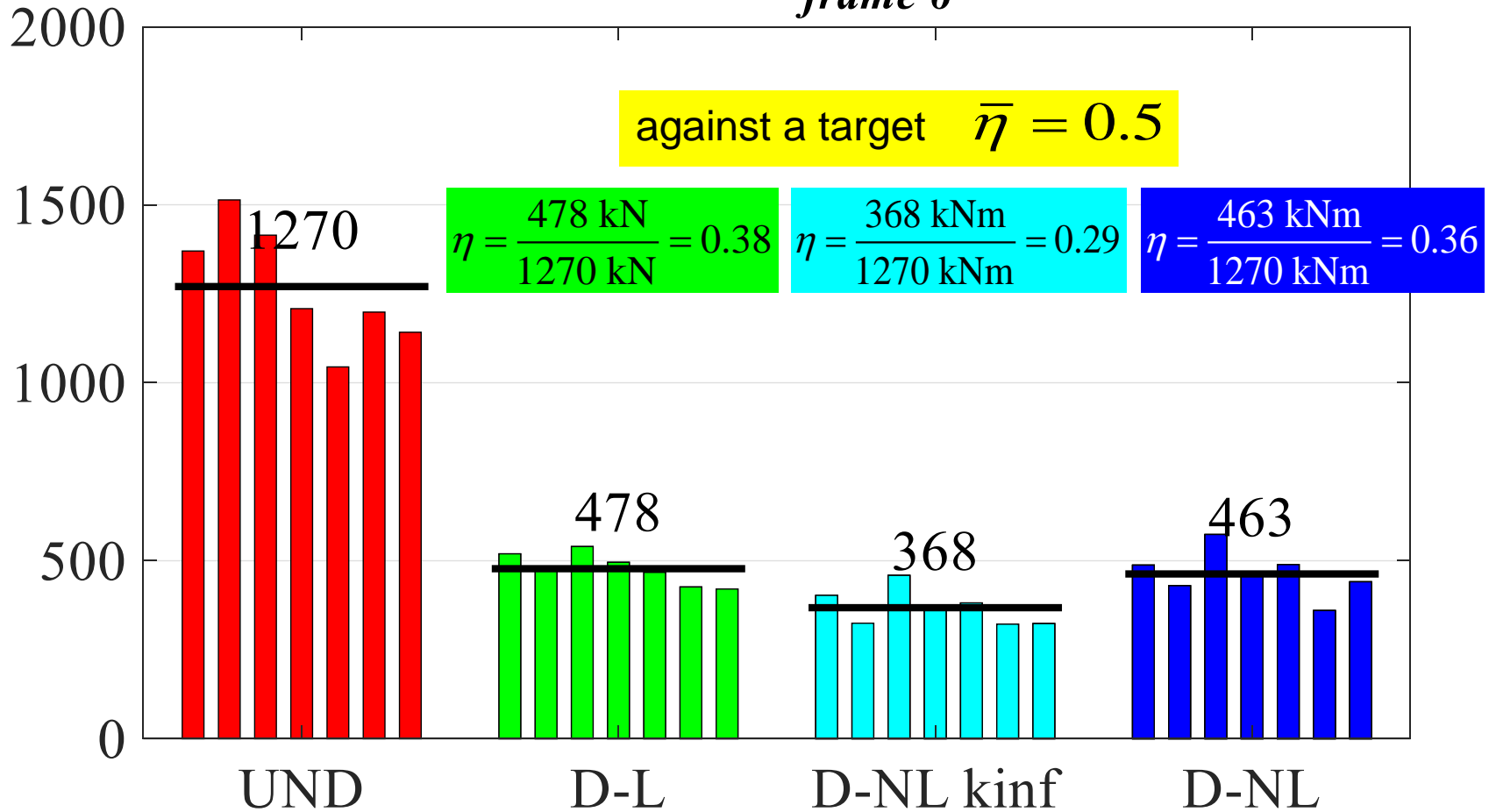




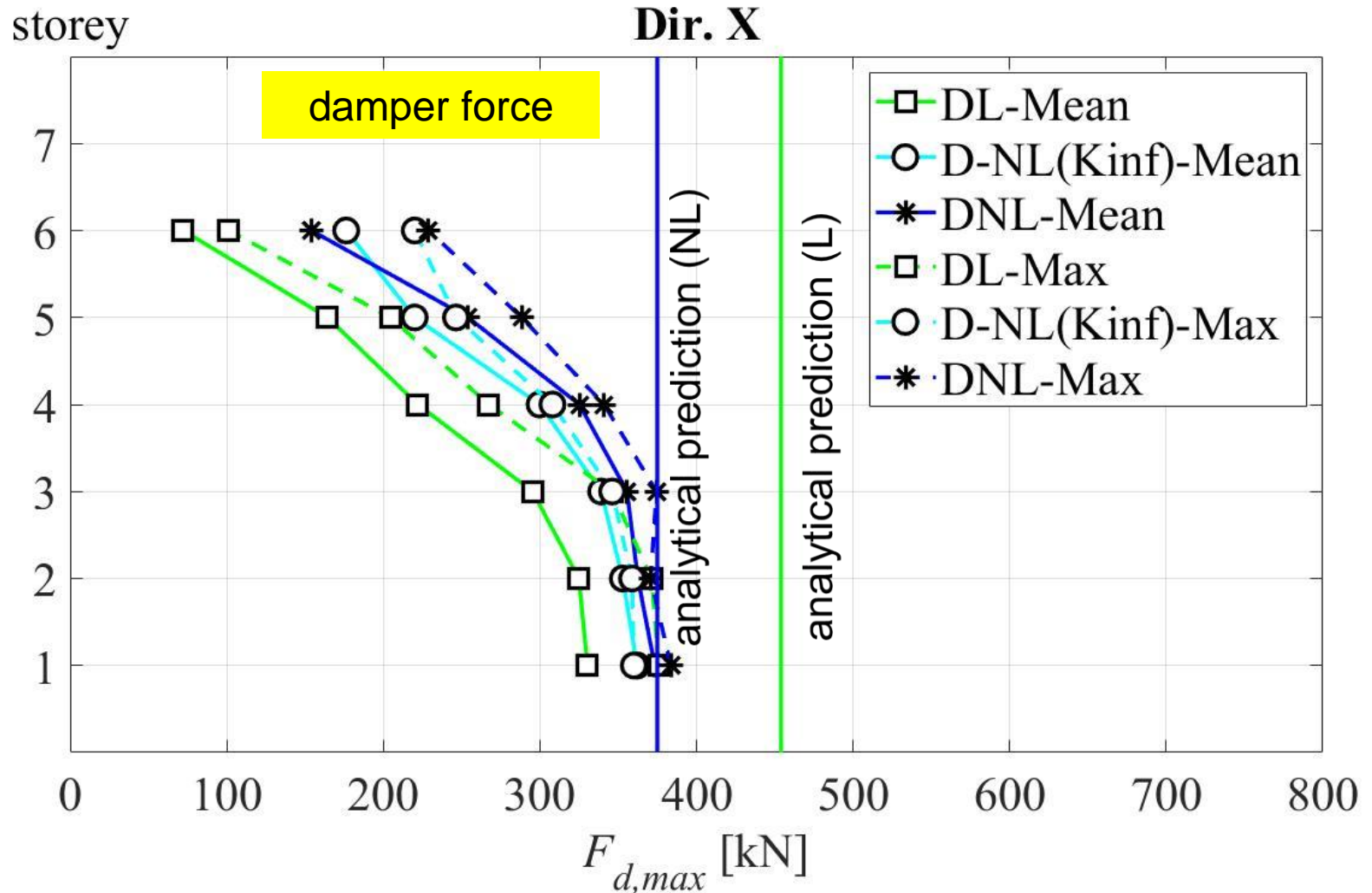
# TH verification

FOCUS on the most stressed column at the ground floor

long. dir. X  $M_{frame\ 6}$  [kNm]

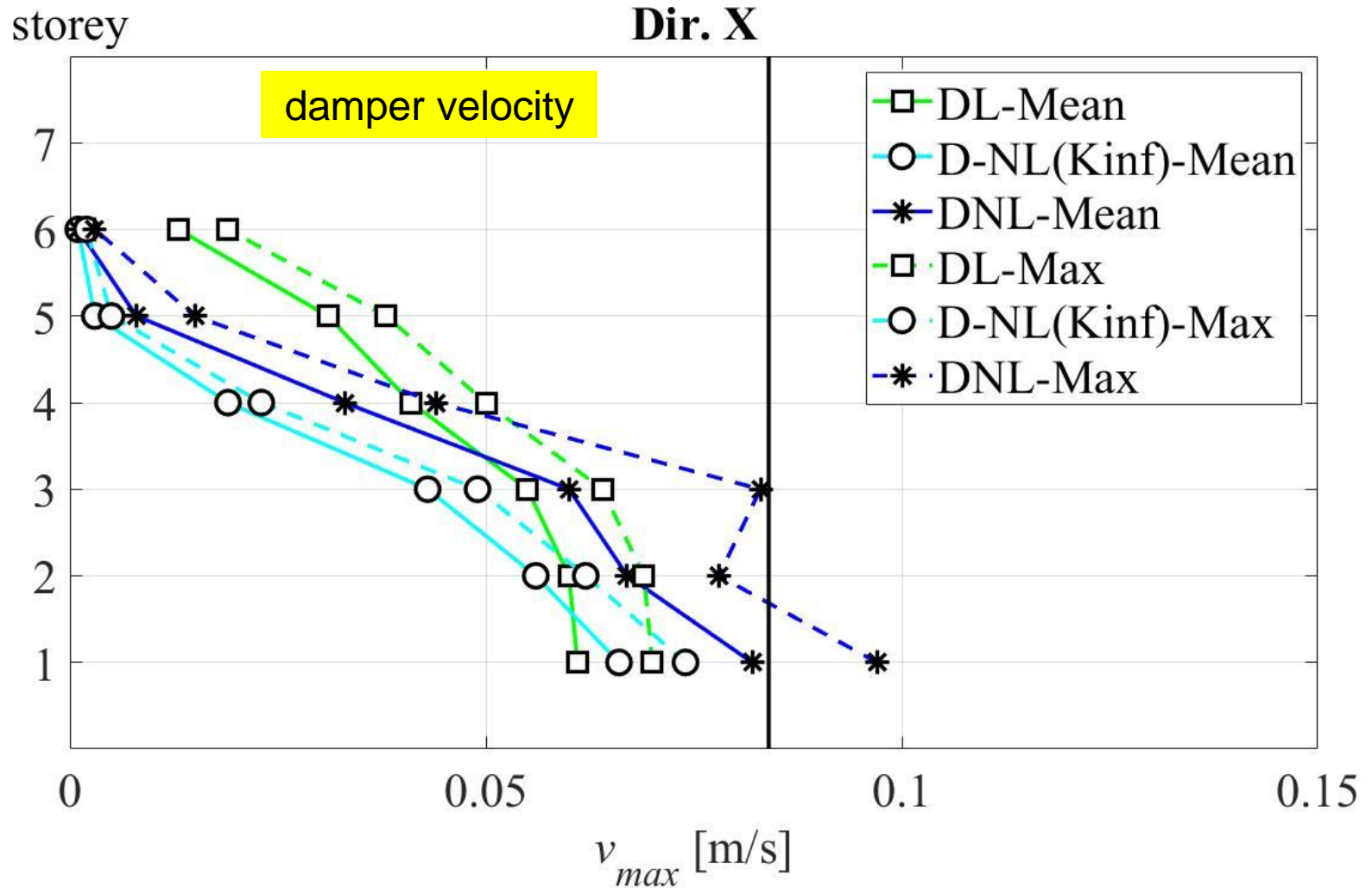


# TH verification

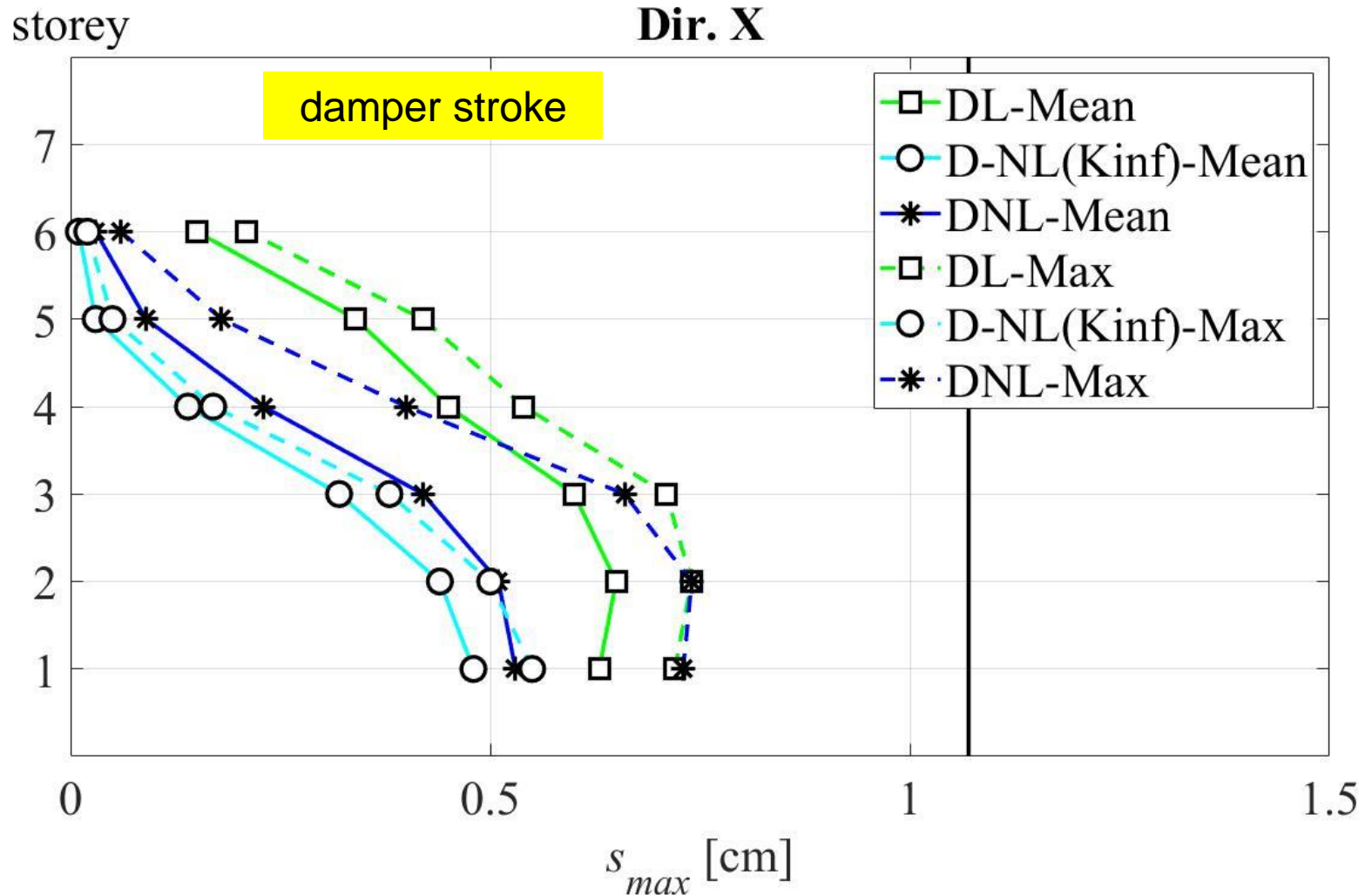


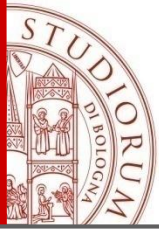


# TH verification

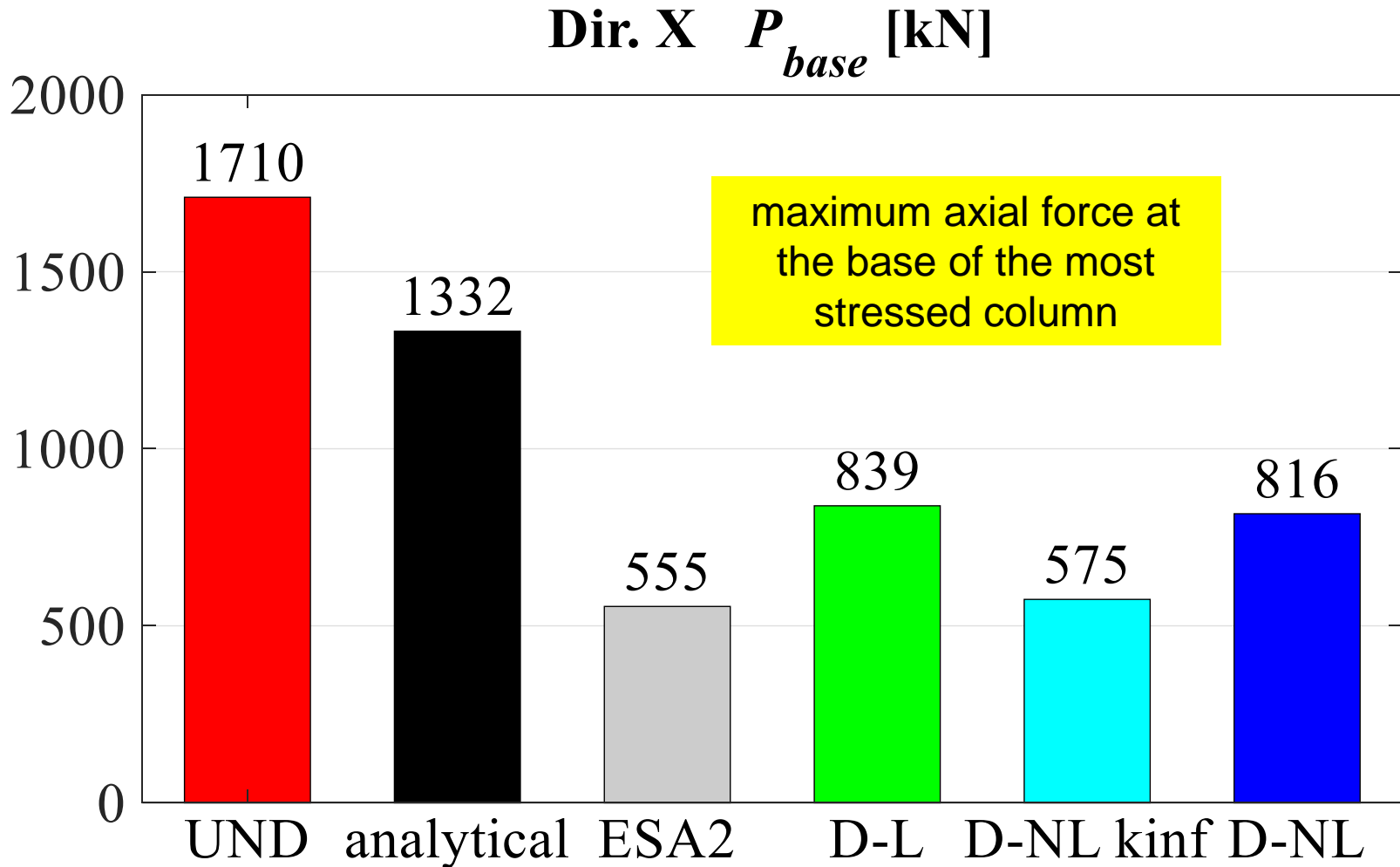


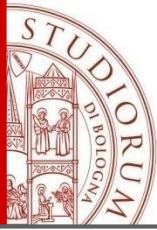
# TH verification





# TH verification





# “Italian” reference paper

Progettazione Sismica – Vol. 8, N.3, Anno 2017  
DOI 10.7414/PS.8.3.9-24 - <http://dx.medra.org/10.7414/PS.8.3.9-24>

## Ricerca

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Un metodo semplificato per il dimensionamento e l'analisi di strutture equipaggiate con smorzatori viscosi

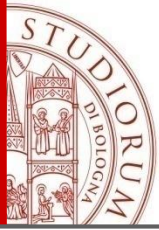
A simplified method for dimensioning and analyzing equipped structures with viscous dampers

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Michele Palermo<sup>1</sup>, Stefano Silvestri<sup>1</sup>, Giada Gasparini<sup>1</sup>, Tomaso Trombetti<sup>1</sup> ■

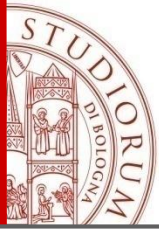
### Sommario

La presente memoria presenta un metodo diretto per il dimensionamento di strutture a telaio dotate di smorzatori viscosi che permette: (1) di dimensionare la taglia degli smorzatori viscosi da inserire nella struttura in modo da soddisfare un determinato obiettivo prestazionale; (2) di stimare le massime sollecitazioni negli elementi strutturali attraverso l'involuppo di due analisi statiche equivalenti.



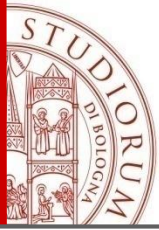
# General Conclusions

- MPD vs SPD systems
- A direct (fully analytical) procedure for the seismic design of building structures with added viscous dampers is presented.
- It represents the **step forward** of the “five-step procedure” (2010).
- It aims at providing **practical tools** for a direct identification of the mechanical characteristics of the manufactured viscous dampers which **allow to achieve target levels of performances**.
- The procedure seems to be **conservative**.
- **In any case, a numerical verification of the final behaviour** of the system by means of non-linear time-history analyses **is recommended**.



# Future developments

- In its current version, the procedure is applicable to **regular multi-storey frame structures** which are characterized by a period of vibration lower than 1.5 s.
- At this stage of the research, the procedure is suitable:
  - for the **preliminary design phase**
  - for the **control of the order of magnitude of FEM results**, since correction factors for the higher modes contributions are necessary to improve its accuracy, especially for high-rise buildings.
- **Extension to existing buildings** to account for the hysteretic dissipation / ductility capacity of the structural elements



**Thank you for your kind attention!**



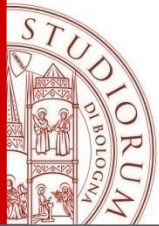
## Thanks to :

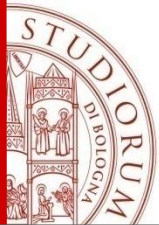
- DPC-RELUIS 2014–2018 Grant - Research line 6:  
“Seismic isolation and dissipation”
- DPC-RELUIS 2019-2021 Grant - WP15:  
“Contribution to codes for isolated and dissipative structures”
- DPC-RELUIS 2022-2024 Grant - WP15:  
“Contributi normativi relativi a Isolamento e Dissipazione”
  
- Ing. Franco Baroni (Studio Ceccoli, Bologna)  
Ing. Gilberto Dallavalle (Studio Ceccoli, Bologna)  
Ing. Friedrich Drollmann (Studio Ceccoli, Bologna)
  
- My colleagues/friends at UNIBO:
  - Tomaso Trombetti, Giada Gasparini
  - Michele Palermo, Luca Landi
  - Matteo Marra, Emma Ghini, Lidiana Arrè
  
- My past and current Graduation Thesis students at UNIBO:
  - Antonio Grana
  - Simone Bernardelli
  - Paolo Catti
  - Luca D’Alonzo
  - Camilla Rita Valente

# Questions?

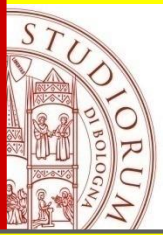


**Stefano Silvestri**  
*stefano.silvestri@unibo.it*





# Extra slides



# Direct-five step procedure for existing buildings



# “Direct five-step procedure” per edifici esistenti

- Per gli edifici esistenti progettati per soli carichi verticali (spesso caratterizzati da indici di sicurezza sismica C/D attorno a 0.20-0.30), in generale, l'introduzione di un sistema di smorzatori viscosi di interpiano (tipo **SPD**) potrebbe essere non sufficiente per un “*adeguamento*” sismico completo in grado di mantenere gli elementi strutturali in campo elastico (visto che la riduzione max della domanda è attorno al 50%)
- Per arrivare ad un “*adeguamento*” e per non fermarsi solo ad un “*miglioramento*”, potrebbe risultare utile affidarsi quindi in parte alla duttilità disponibile (dissipazioni isteretiche associate a danneggiamento elementi strutturali)
- Ma la normativa consente di accoppiare le due dissipazioni solo con Analisi Non Lineari Dinamiche ed impone il confronto con Analisi Modale con Spettro di Risposta:

## 7.3.4.1 ANALISI NON LINEARE DINAMICA

L'analisi non lineare dinamica consiste nel calcolo della risposta sismica della struttura mediante integrazione delle equazioni del moto, utilizzando un modello non lineare della struttura e le storie temporali del moto del terreno definite al § 3.2.3.6. Essa ha lo scopo di valutare il comportamento dinamico della struttura in campo non lineare, consentendo il confronto tra duttilità richiesta e duttilità disponibile allo SLC e le relative verifiche, nonché di verificare l'integrità degli elementi strutturali nei confronti di possibili comportamenti fragili.

L'analisi non lineare dinamica deve essere confrontata con un'analisi modale con spettro di risposta di progetto, al fine di controllare le differenze in termini di sollecitazioni globali alla base della struttura.

Nel caso delle costruzioni con isolamento alla base l'analisi dinamica non lineare è obbligatoria quando il sistema d'isolamento non può essere rappresentato da un modello lineare equivalente, come stabilito nel § 7.10.5.2. Gli effetti torsionali sul sistema d'isolamento sono valutati come precisato nel § 7.10.5.3.1, adottando valori delle rigidezze equivalenti coerenti con gli spostamenti risultanti dall'analisi. In proposito si può fare riferimento a documenti di comprovata validità.

# “Direct five-step procedure” per edifici esistenti

$$\eta = \frac{\text{risp. plast. smorz.}}{\text{risp. elast. non smorz.}} = \left( \frac{\text{risp. plast. smorz.}}{\text{risp. elast. smorz.}} \right) \cdot \left( \frac{\text{risp. elast. smorz.}}{\text{risp. elast. non smorz.}} \right) =$$

HP)  $\frac{\text{risp. plast. smorz.}}{\text{risp. elast. smorz.}} = \frac{\text{risp. plast. non smorz.}}{\text{risp. elast. non smorz.}} = \eta_q = \frac{1}{q}$

$$\eta_q$$

$$\eta_\xi = \sqrt{\frac{10}{5+\xi}}$$

PROPOSTA:

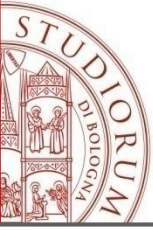
$$\eta = \eta_\xi \cdot \eta_q$$

Fattore di riduzione totale (da applicare allo spettro elastico ( $\xi=5\%$  e  $q=1$ )) = Livello di progetto per gli elementi strutturali

Aliquota del fattore di riduzione dovuta agli effetti dissipativi degli smorzatori viscosi

Aliquota del fattore di riduzione dovuta alla duttilità disponibile

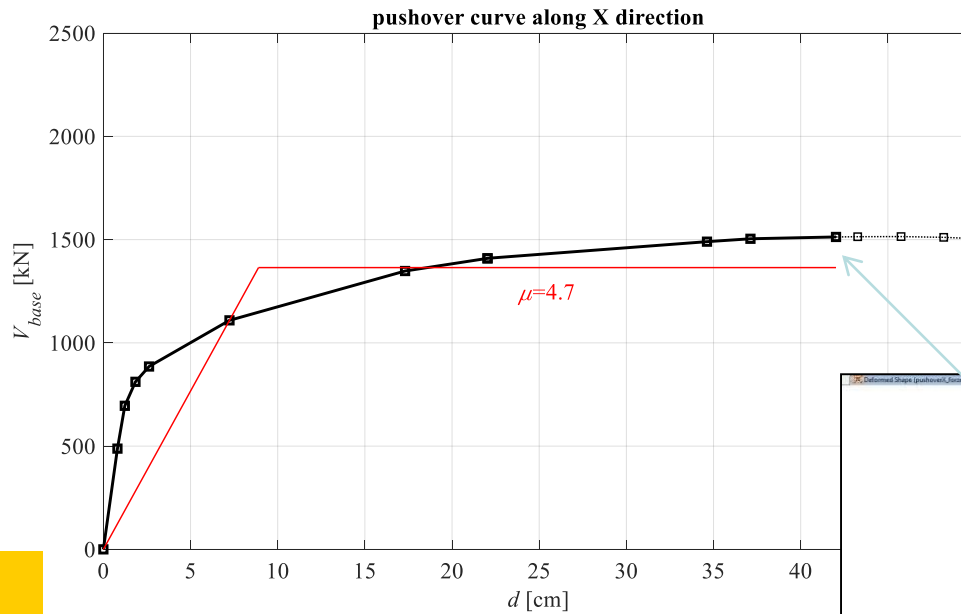
	Edifici Nuovi	Edifici Esistenti
$\eta$	<b>Da definire</b> sulla base dei dati di progetto e del tasso di lavoro che si vuole attribuire agli elementi strutturali.	<b>Definito</b> sulla base delle <b>armature</b> e delle <b>dimensioni geometriche</b> degli elementi strutturali (es. $M_{Rd}$ ) e l'azione sismica di progetto (es. $M_{Ed}$ ).
$\eta_q$	<b>Da definire</b> sulla base della tipologia di struttura e i valori del fattore di comportamento $q$ dati nella Norma.	<b>Definito</b> sulla base della reale duttilità della struttura, identificabile mediante la sua <b>curva di capacità</b> .
$\eta_\xi$	<b>Da definire</b> per progettare il sistema di dissipazione.	<b>Da definire</b> per progettare il sistema di dissipazione.



# “Direct five-step procedure” per edifici esistenti

ad esempio: flessione nei pilastri o taglio alla base

$$\bar{\eta} = \frac{\text{target seismic demand (i.e. capacity/strength)}}{\text{actual seismic (elastic) demand with no dampers}} = \frac{M_{Ed,\xi} (= M_{Rd})}{M_{Ed,\xi=5\%}} = 0.25$$



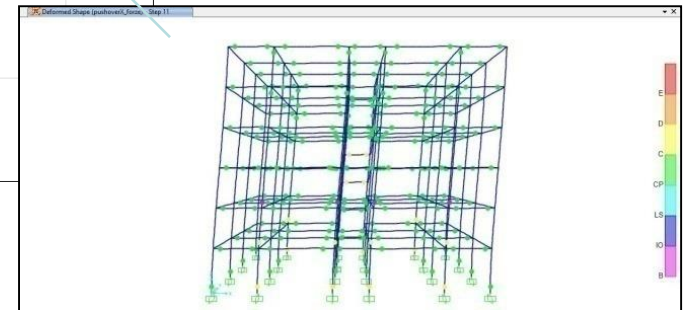
$$\bar{\eta} = \zeta_E = \frac{C}{D}$$

$$\mu_{disp} = 4.7$$

$$HP) \quad q = \mu$$

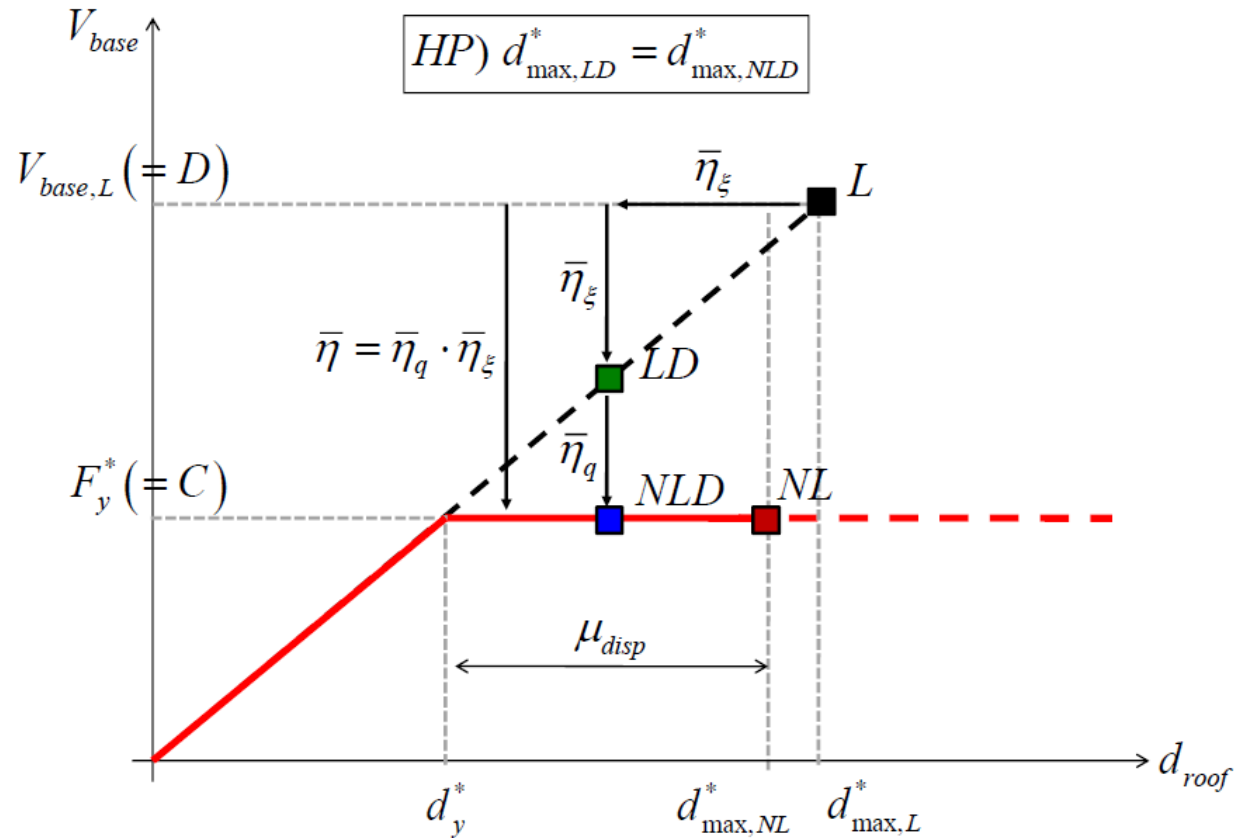
$$q_{max,disp} > q_{NTC,esistenti}$$

$$q_{NTC,esistenti} = 1.5 \div 3.0$$



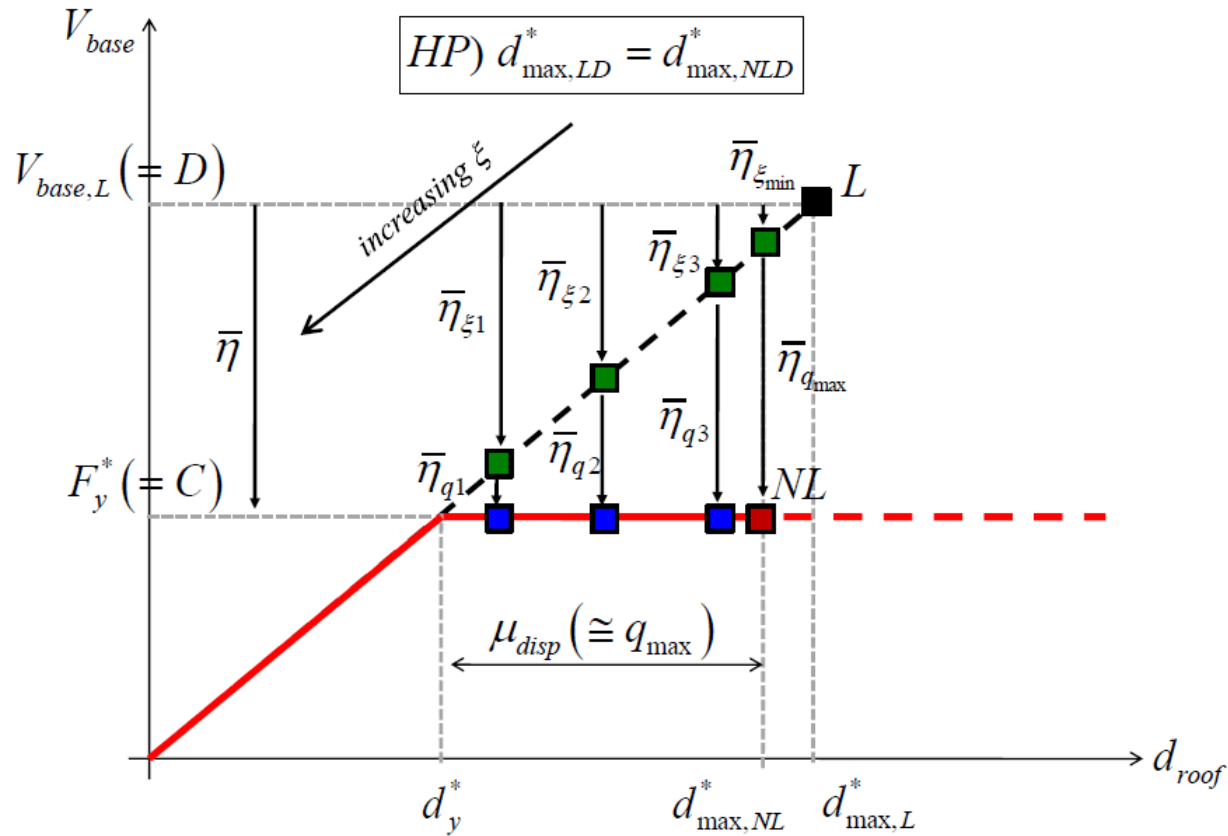


# “Direct five-step procedure” per edifici esistenti



**Figura I** – Illustrazione dell'obiettivo prestazionale, rappresentato dal punto di performance identificato dal quadratino blu (NLD). NL = risposta non-lineare della struttura esistente allo stato di fatto. NLD = risposta non-lineare della struttura esistente con smorzatori. L = risposta della struttura lineare equivalente. LD = risposta della struttura lineare equivalente con smorzatori.

# “Direct five-step procedure” per edifici esistenti



**Figura II** – Illustrazione delle strategie progettuali, basate su una ponderata ripartizione del fattore di riduzione della risposta sismica tra quota parte dovuta a dissipazione viscosa e quota parte dovuta a dissipazione isteretica.

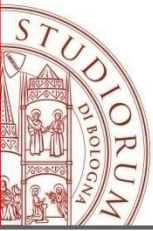
# “Direct five-step procedure” per edifici esistenti

Possibilità a disposizione del progettista:

$$\eta = \eta_q \cdot \eta_\xi$$

$$\eta = \frac{1}{q} \cdot \sqrt{\frac{10}{5 + \xi}}$$

	$\eta$	=	$\eta_q$	·	$\eta_\xi$
$\xi = 15\% \rightarrow q = 2.9$	0.25	=	0.35	·	0.71
$\xi = 25\% \rightarrow q = 2.3$	0.25	=	0.43	·	0.58
$< q_{\max, disp}$	0.25	=	...	·	...



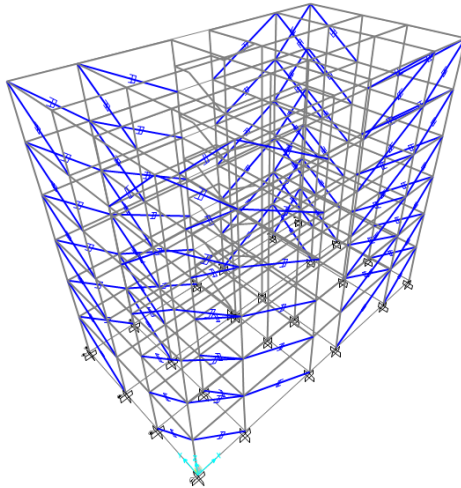
# “Direct five-step procedure” per edifici esistenti

$$q = 2.3 + \xi = 25\%$$

$$\xi = \xi_{intr} + \xi_{visc}$$

$$= 5\% + 20\%$$

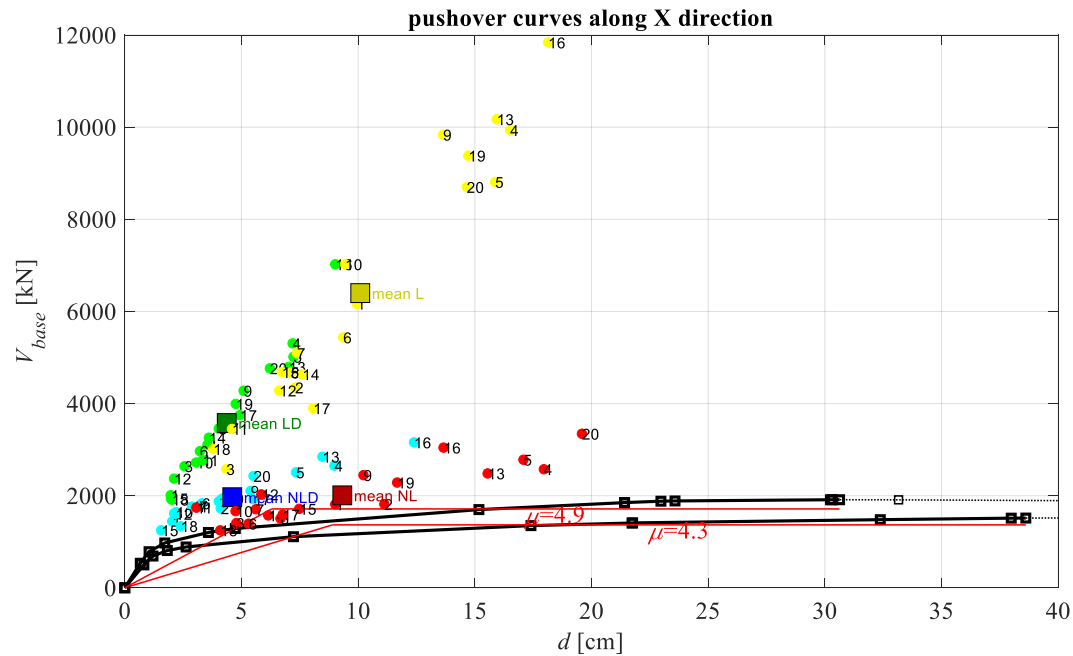
progettazione smorzatori  
viscosi con Direct Five-Step  
Procedure

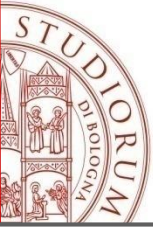


		dir. long. (x)	dir. trasv. (y)	unità di misura
<b>STEP 1</b>				
smorzamento intrinseco	$\xi_{intr} =$	0.05	0.05	
smorzamento viscoso	$\xi_{visc} =$	0.20	0.20	
smorzamento totale	$\xi_{tot} =$	0.25	0.25	
fattore riduzione risposta	$\eta =$	0.577	0.577	
<b>STEP 2</b>				
numero totale piani	N =	6	6	
peso totale struttura	Wtot =	16006	16006	kN
periodo fondamentale struttura	T1 =	0.795	0.693	s
pulsazione fondamentale struttura	$\omega 1 =$	7.90	9.06	rad/s
numero di smorzatori per piano	n =	8	8	
inclinazione smorzatori	$\theta =$	43	39	°
coefficiente smorzamento lineare	cL =	4218	4284	kNs/m
rigidezza assiale	kaxial =	infinita	infinita	
<b>STEP 3</b>				
accelerazione spettrale	Sa(T1) =	0.244	0.280	g
coefficiente correttivo	M =	1.00	1.00	
velocità massima smorzatori lineari	vmax =	0.063	0.067	m/s
forza massima smorzatori lineari	FLmax =	267	288	kN
corsa massima pistone	smax =	0.80	0.74	cm
<b>STEP 4</b>				
esponente	$\alpha =$	0.15	0.15	
coefficiente smorzamento non-lineare	cNL =	334	357	kN (s/m) <sup><math>\alpha</math></sup>
forza massima smorzatori non-lineari	FNLmax =	221	238	kN
rigidezza assiale minima	kaxial >	333216	388233	kN/m
<b>STEP 5</b>				
<b>ESA1</b>				
forza totale	Fh =	3904	4478	kN
<b>ESA2</b>				
forza struttura	Fstructure =	1292	1482	kN
numero telai con smorzatori	n frames =	2	4	
forza telaio	Fframe =	646	370	kN
numero specchiature con smorzatori nel telaio	n bays =	4	2	
forza specchiatura (singola reticolare)	Fbay =	161	185	kN
<b>sforzo normale max nelle colonne</b>				
	P1,max =	903	900	kN
	P2,max =	753	750	kN
	P3,max =	602	600	kN
<b>sforzo normale max alla base singola colonna</b>				
	Fbase =	903	900	kN

# “Direct five-step procedure” per edifici esistenti

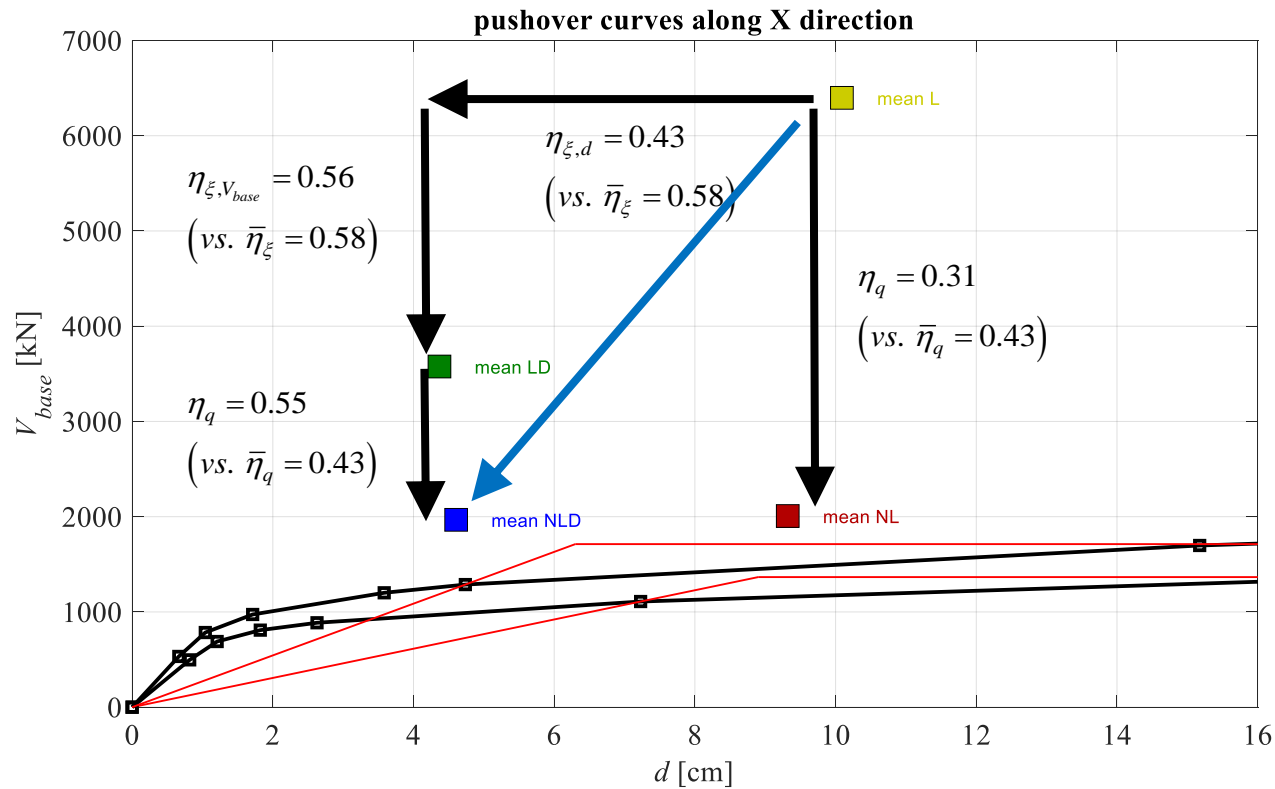
Verifica dell'efficacia della procedura:

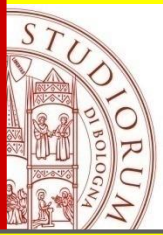




# “Direct five-step procedure” per edifici esistenti

Verifica dell'efficacia della procedura:





# Other applications MPD and SPD

(RELUIS project 2022-2023)

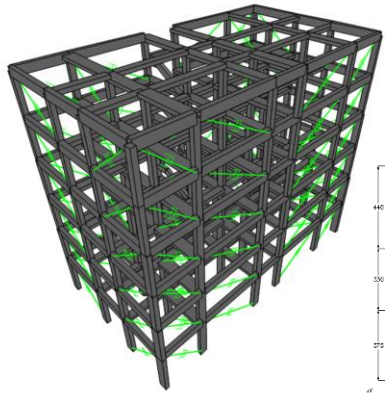


# CASE-STUDIES

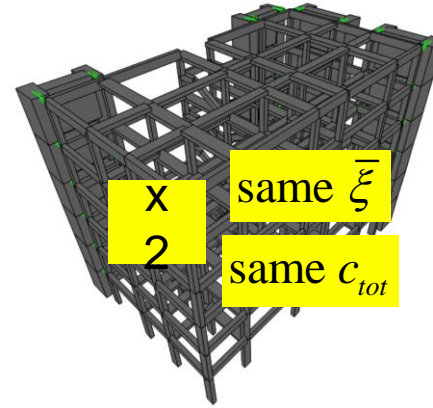
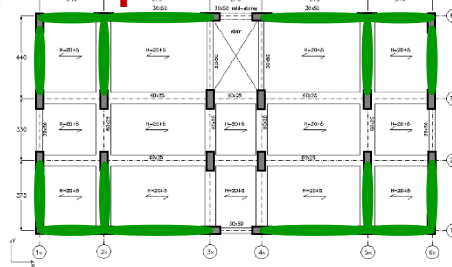
## Interstorey viscous dampers

## Dissipative links connected to external stiff towers

6-storey new building

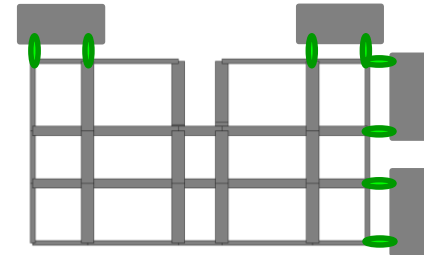


**SPD  
placement**

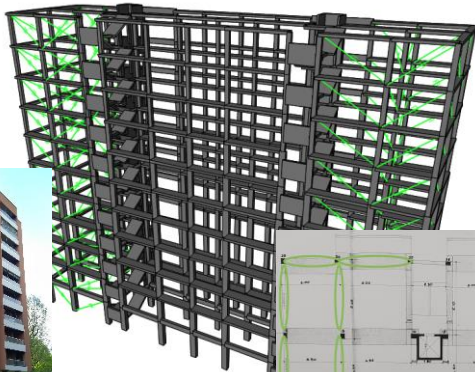


$\times 2$  same  $\xi$   
 $\times 2$  same  $c_{tot}$

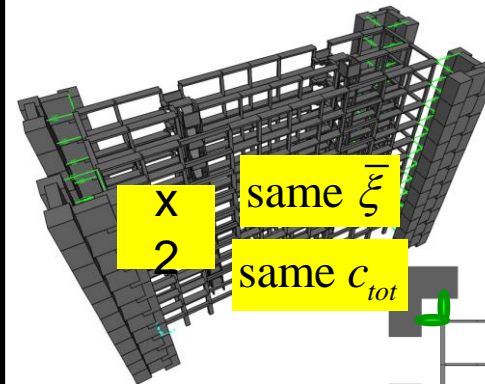
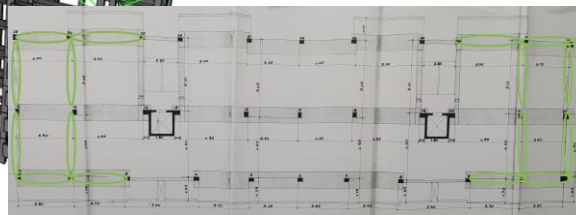
**MPD tower**



11-storey existing building

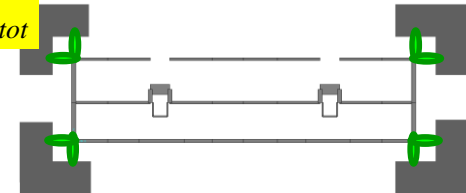


**SPD  
placement**



$\times 2$  same  $\xi$   
 $\times 2$  same  $c_{tot}$

**MPD tower**



# THE «DIRECT FIVE-STEP PROCEDURE» (2018)

STEP 1: performance



$$\bar{\eta} \rightarrow \bar{\xi}$$

$$\bar{\eta} = \sqrt{\frac{10}{5 + \bar{\xi}}}$$

$$c_{NL} = \zeta_{visc} \cdot \frac{2\pi}{T_1} \cdot \frac{W}{g} \cdot \left(\frac{N+1}{n}\right) \cdot \frac{1}{\cos^2 \theta} \cdot \left(0.8 \cdot \frac{S_e(T_1, \bar{\eta}_{\xi})}{2\pi/T_1} \cdot \frac{2}{N+1} \cdot \cos \theta\right)^{1-\alpha}$$

$$k_{axial} \geq 10 \cdot \bar{\xi} \cdot \zeta_{visc} \cdot \left(\frac{2\pi}{T_1}\right)^2 \cdot \frac{W}{g} \cdot \left(\frac{N+1}{n}\right) \cdot \frac{1}{\cos^2 \theta}$$

VERIFICA  
N

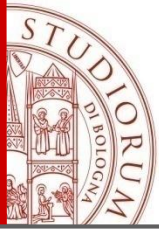
STEP 5: non-linear TH analyses



structural  
response



**2. Equivalent Static Analysis (ESA)**



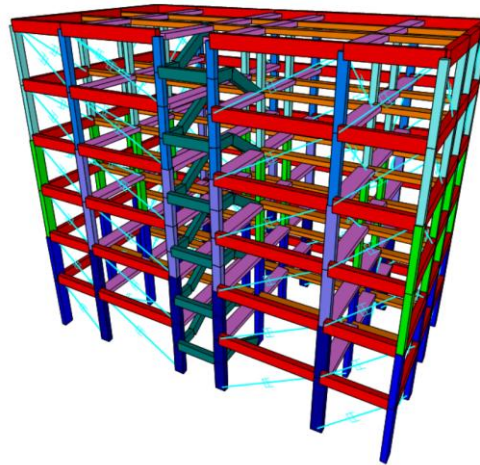
## **CASE 1A**

6-storey new RC frame building + interstorey viscous dampers

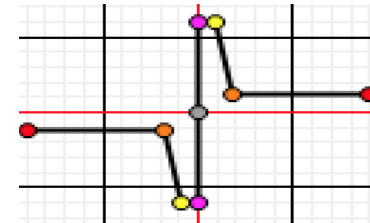
# THE 6-STOREY STRUCTURE

**bars in the columns** → guarantee at least 1% of the area of the concrete section

**bars in the beams** → guarantee at least 0.15% of the area of the concrete section, both in the tension area and in the compressed area, and in any case able to carry the maximum bending moments induced by a distribution of static vertical loads corresponding to the rare SLS combination

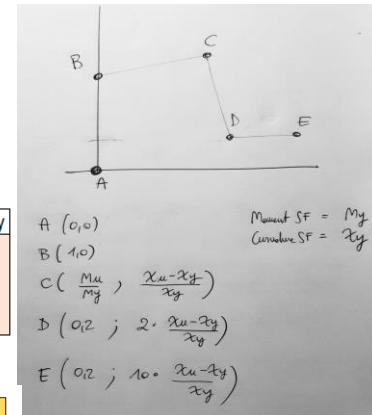


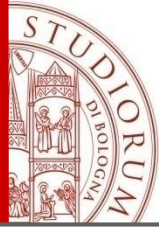
Flexural Plastic Hinges



	Cerniere Platiche Trave					
	My	Xy	Mu	Xu	Mu/My	(Xu-Xy)/Xy
Trave a Ginocchio	133,82	0,00519	138,25	0,0671	1,03	11,9
Trave Perimetrale	253,96	0,00437	267,78	0,0597	1,05	12,7
Trave in spessore X	74,60	0,01201	73,92	0,0773	1	5,4
Trave in spessore Y	180,95	0,01310	178,76	0,0642	1	3,9

		Cerniere Plastiche Pilastri M3														
Telaio 1		My	Xy	Mu	Xu	Ned	Mu/My	(Xu-Xy)/Xy	Telaio 2	My	Xy	Mu	Xu	Ned	Mu/My	(Xu-Xy)/Xy
P1		399,2	0,006231	426,1	0,016863	428,73	1,1	1,7	P1	423,2	0,005244	448,5	0,013086	552,4	1,1	1,5
P2		448,1	0,004176	468,6	0,010536	686,05	1,0	1,5	P2	442,5	0,004437	487,5	0,008487	851,55	1,1	0,9
P3		444,6	0,004146	465,9	0,010842	666,68	1,0	1,6	P3	446,5	0,004375	483,6	0,008891	812,9	1,1	1,0
P4		444,6	0,004146	465,9	0,010842	666,52	1,0	1,6	P4	446,5	0,004375	483,6	0,008891	812,13	1,1	1,0
P5		448,1	0,004176	468,6	0,010536	686,47	1,0	1,5	P5	442,5	0,004437	487,5	0,008487	851,6	1,1	0,9
P6		399,2	0,006231	426,1	0,016863	429,74	1,1	1,7	P6	423,2	0,005244	448,5	0,013086	552,65	1,1	1,5
P7		384,2	0,006994	410,6	0,020458	353,47	1,1	1,9	P7	403,9	0,006016	430,7	0,015959	452,99	1,1	1,7
P8		424,3	0,005202	449,5	0,01294	558,6	1,1	1,5	P8	451,1	0,004201	470,7	0,010294	702,15	1,0	1,5
P9		422,2	0,005277	447,7	0,0132	547,63	1,1	1,5	P9	445,5	0,004154	466,6	0,010763	671,58	1,0	1,6
P10		422,2	0,005277	447,7	0,0132	547,59	1,1	1,5	P10	445,5	0,004154	466,6	0,010763	671,79	1,0	1,6
P11		424,3	0,005202	449,5	0,01294	558,9	1,1	1,5	P11	451,1	0,004201	470,7	0,010294	702,16	1,0	1,5



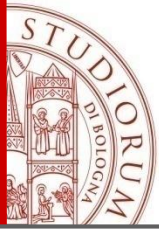


## CAUTIONARY NOTE ABOUT SHEAR BEHAVIOUR

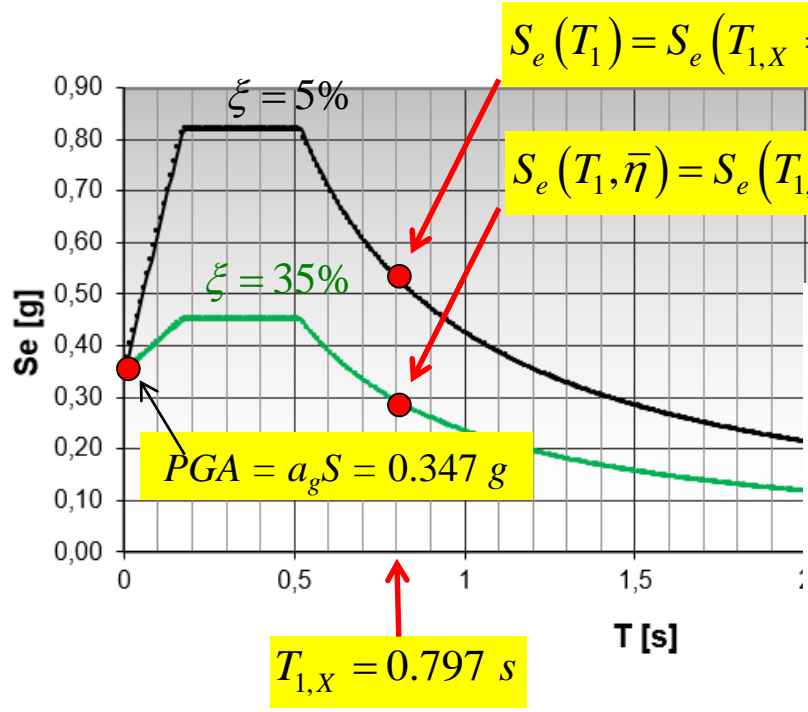
The non-linear (elasto-brittle) **shear behaviour** of the structural elements is **not modelled**.

It is therefore implicitly **assumed that the shear strength of all the structural elements has been adequately increased by means of structural reinforcement interventions** (e.g. bands with fibre-reinforced polymeric materials) aimed at:

- (i) guaranteeing a shear strength higher than the shear force corresponding to the formation of bending plastic hinges (bending capacity suitably increased with overstrength factors), according to the hierarchy of resistances
- (ii) increasing the ductile capacity of the cross-section

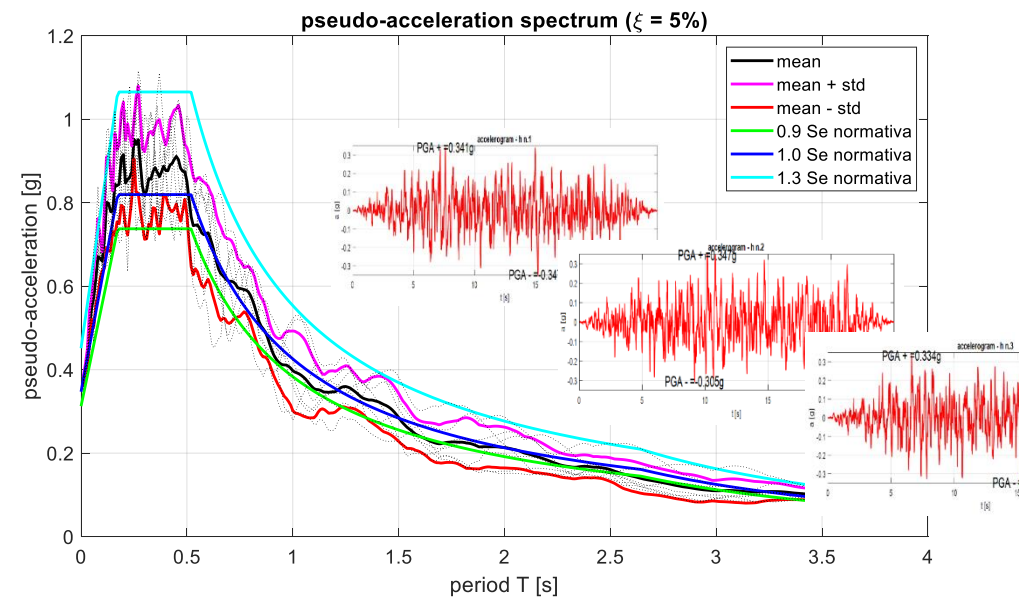


# SEISMIC INPUT



$$S_e(T_1) = S_e(T_{1,X} = 0.797s, \xi = 5\%) = 0.534 g$$

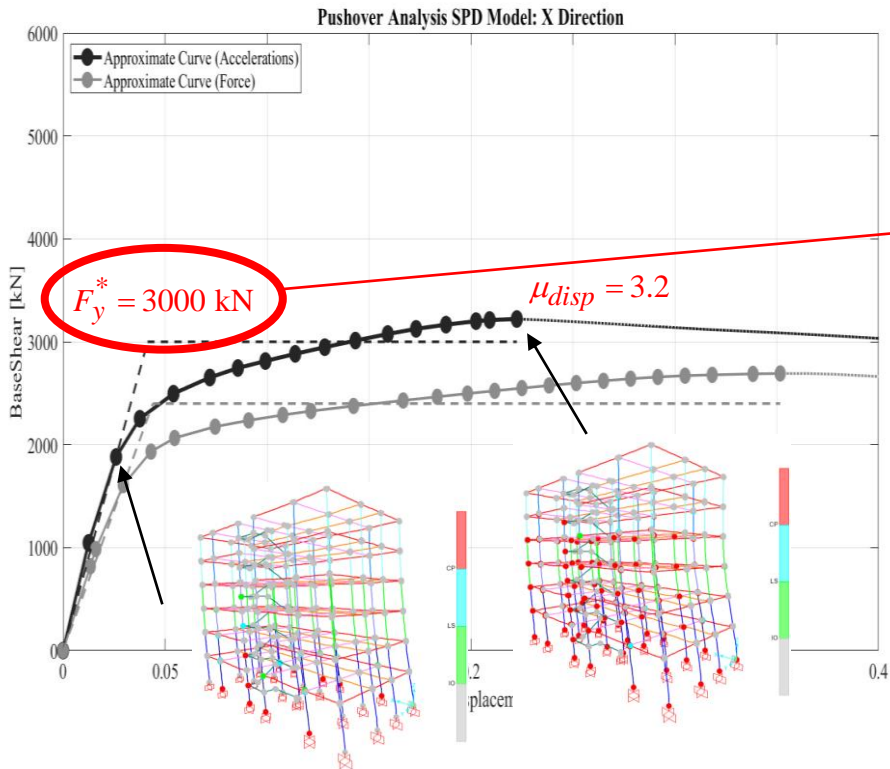
$$S_e(T_1, \bar{\eta}) = S_e(T_{1,X} = 0.797s, \bar{\xi}_{tot} = 35\%) = 0.294 g$$





# STARTING POINT: CAPACITY-DEMAND RATIO (X Direction)

- at the global response level of the entire structure in terms of base shear - top displacement curve

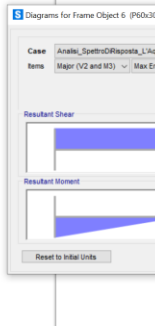
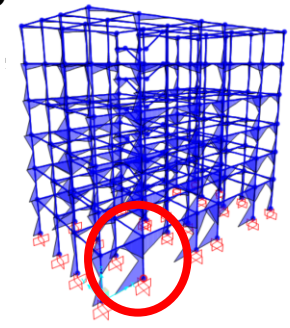


$$V_{base} \cong \lambda \cdot \frac{W_{tot}}{g} \cdot S_a(T_1) = 0.85 \cdot \frac{16600 \text{ kN}}{g} \cdot 0.534g \cong 7500 \text{ kN}$$

$$\left. \frac{C}{D} \right|_{global} \cong \frac{3000}{7500} \cong 0.4$$

- at the local response level (e.g., bending moment, shear force) of the most stressed structural element (e.g. beam).

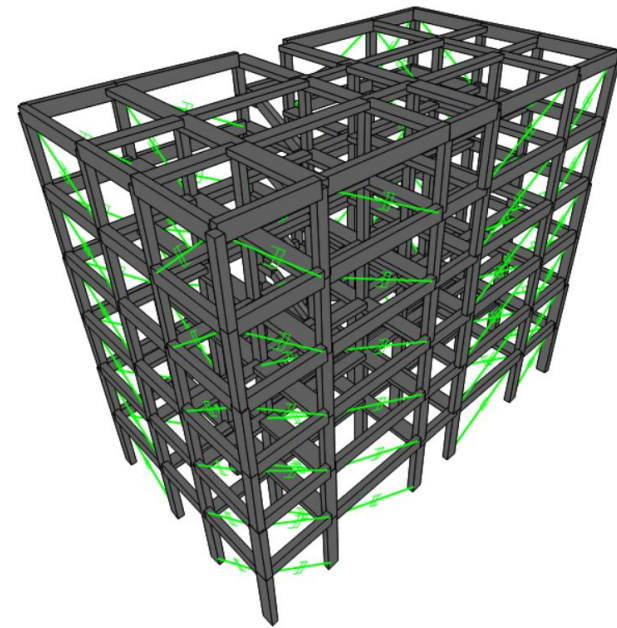
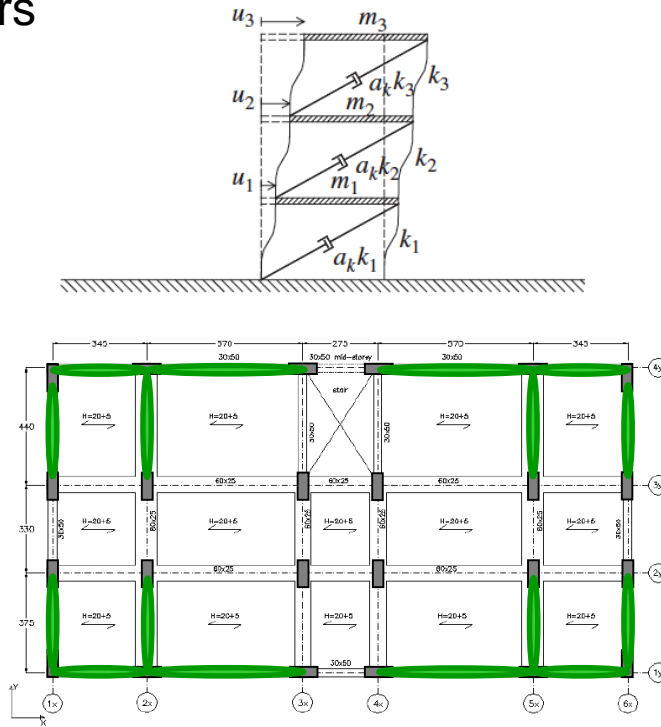
$$\left. \frac{C}{D} \right|_{local} = \frac{M_{Rd}}{M_{Ed}} \cong 0.25$$



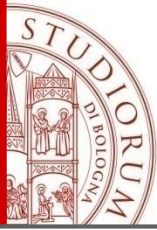


## CASE 1A

6-storey new RC frame building + interstorey viscous dampers



18.65 m



## DESIGN STRATEGIES

The design strategy is based on the dimensioning of our dampers in order to achieve the target. Moreover, is also possible to taking into account the weighted coupling of hysteretic dissipation (ductility available in the structural elements). The starting point is represented by:

$$\left. \begin{array}{l} \frac{C}{D}_{global} \cong \frac{3000}{7500} \cong 0.4 \\ \frac{C}{D}_{local} = \frac{M_{Rd}}{M_{Ed}} \cong 0.25 \end{array} \right\} \bar{\eta} = \zeta_E = \frac{C}{D} = 0.5$$

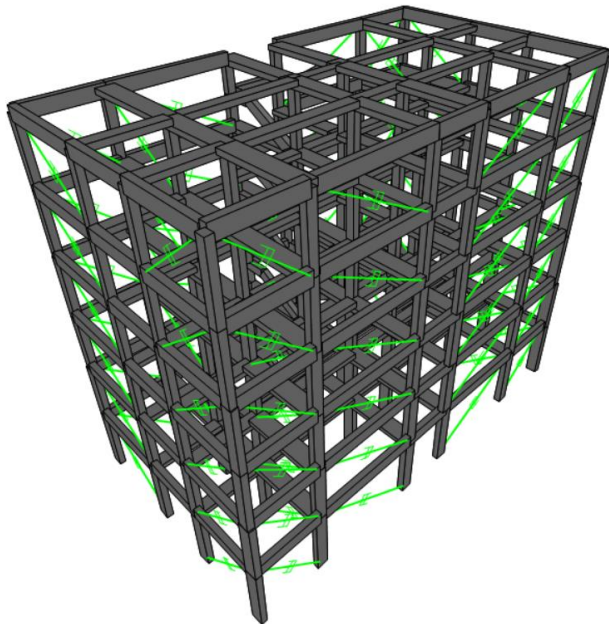
Assuming three different target demands, the reduction factors and the target damping ratios are evaluated, and three viscous dampers systems are obtained:

$$\xi_{tot} = 35\% \rightarrow \bar{\xi}_{visc} = 30\% \rightarrow c_{NL} = 544 \text{ kN} \cdot (\text{s/m})^{0.15}$$

$$\xi_{tot} = 25\% \rightarrow \bar{\xi}_{visc} = 20\% \rightarrow c_{NL} = 378 \text{ kN} \cdot (\text{s/m})^{0.15}$$

$$\xi_{tot} = 15\% \rightarrow \bar{\xi}_{visc} = 10\% \rightarrow c_{NL} = 224 \text{ kN} \cdot (\text{s/m})^{0.15}$$

# DESIGN OF FLUID VISCOUS DAMPERS: APPLICATION OF DIRECT FIVE STEP PROCEDURE FOR $\xi_{visc} = 30\%$



$$\xi_{tot} = \xi_{intr} + \xi_{visc}$$

$$= 5\% + 30\%$$

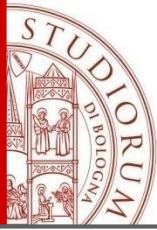
		dir. long. (x)	dir. trasv. (y)	unità di misura
<b>STEP 1</b>				
smorzamento intrinseco	$\xi_{intr} =$	0,05	0,05	
smorzamento viscoso	$\xi_{visc} =$	0,30	0,30	
smorzamento totale di target	$\xi_{tot} =$	0,35	0,35	
fattore riduzione risposta di target	$\eta =$	0,500	0,500	

<b>STEP 2</b>				
numero totale piani	N =	6	6	
peso totale struttura	Wtot =	16600	16600	kN
periodo fondamentale struttura	T1 =	0,797	0,704	s
pulsazione fondamentale struttura	$\omega_1 =$	7,88	8,93	rad/s
numero di smorzatori per piano	n =	8	8	
inclinazione smorzatori	$\theta =$	36	38	°
coefficiente smorzamento lineare	cL =	5384	6461	kNs/m
rigidezza assiale	kaxial =	infinita	infinita	

<b>STEP 3</b>				
accelerazione spettrale	Sa(T1) =	0,294	0,333	g
coefficiente correttivo	M =	1,00	1,00	
velocità massima smorzatori lineari	vmax =	0,084	0,082	m/s
forza massima smorzatori lineari	FLmax =	454	529	kN
corsa massima pistone	smax =	1,07	0,92	cm

<b>STEP 4</b>				
esponente	$\alpha =$	0,15	0,15	
coefficiente smorzamento non-lineare	cNL =	544	637	kN (s/m) <sup>2</sup> a
forza massima smorzatori non-lineari	FNLmax =	375	437	kN
rigidezza assiale minima	kaxial >	424327	576634	kN/m

<b>STEP 5</b>				
<b>ESA1</b>				
forza totale	Fh =	4877	5523	kN
<b>ESA2</b>				
forza struttura	Fstructure =	2421	2741	kN
numero telai con smorzatori	n frames =	2	4	
forza telaio	Fframe =	1210	685	kN
numero specchiature con smorzatori nel telaio	n bays =	4	2	
forza specchiatura (singola reticolare)	Fbay =	303	343	kN
<b>sfuerzo normale max nelle colonne</b>				
	P1,max =	1332	1631	kN
	P2,max =	1110	1359	kN
	P3,max =	888	1088	kN
sfuerzo normale max alla base singola colonna	Pbase =	1332	1631	kN



## MODELS ANALYZED

**LS** = bare structure (without dampers) modeled as linear

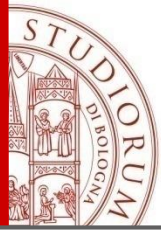
**NLS** = bare structure (without dampers) modeled as non-linear with flexural plastic hinges

**LS\_LD** = linear structure (modeled without the flexural plastic hinges) with linear dampers (designed with the direct five-step procedure)

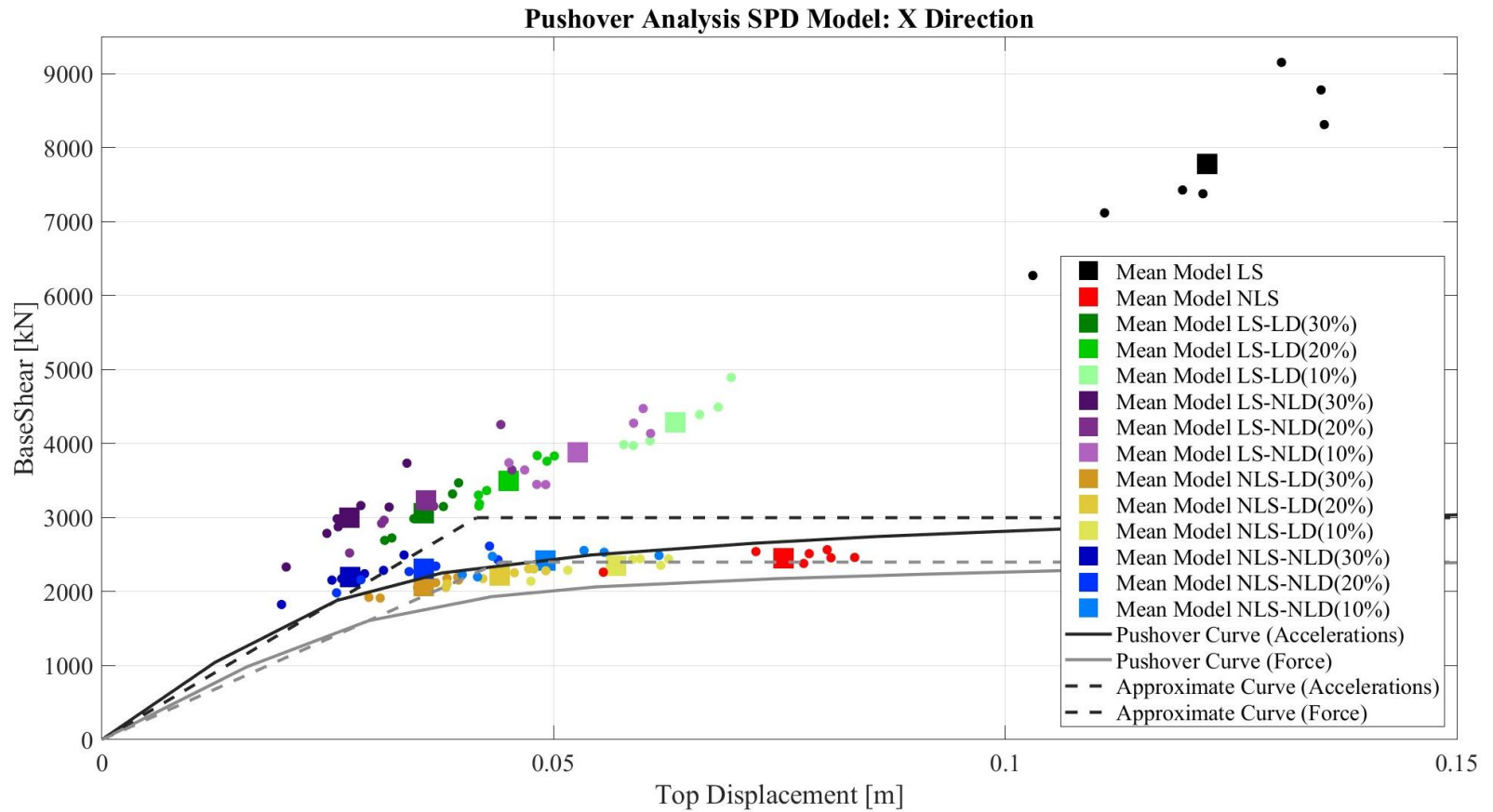
**LS\_NLD** = linear structure (modeled without the flexural plastic hinges) with non-linear viscous dampers (designed with the direct five-step procedure)

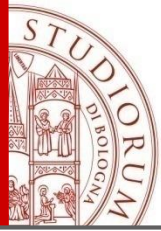
**NLS\_LD** = non linear structure (modeled with the flexural plastic hinges) with linear dampers (designed with the direct five-step procedure)

**NLS\_NLD** = non linear structure (modeled with the flexural plastic hinges) with non-linear viscous dampers (designed with the direct five-step procedure)

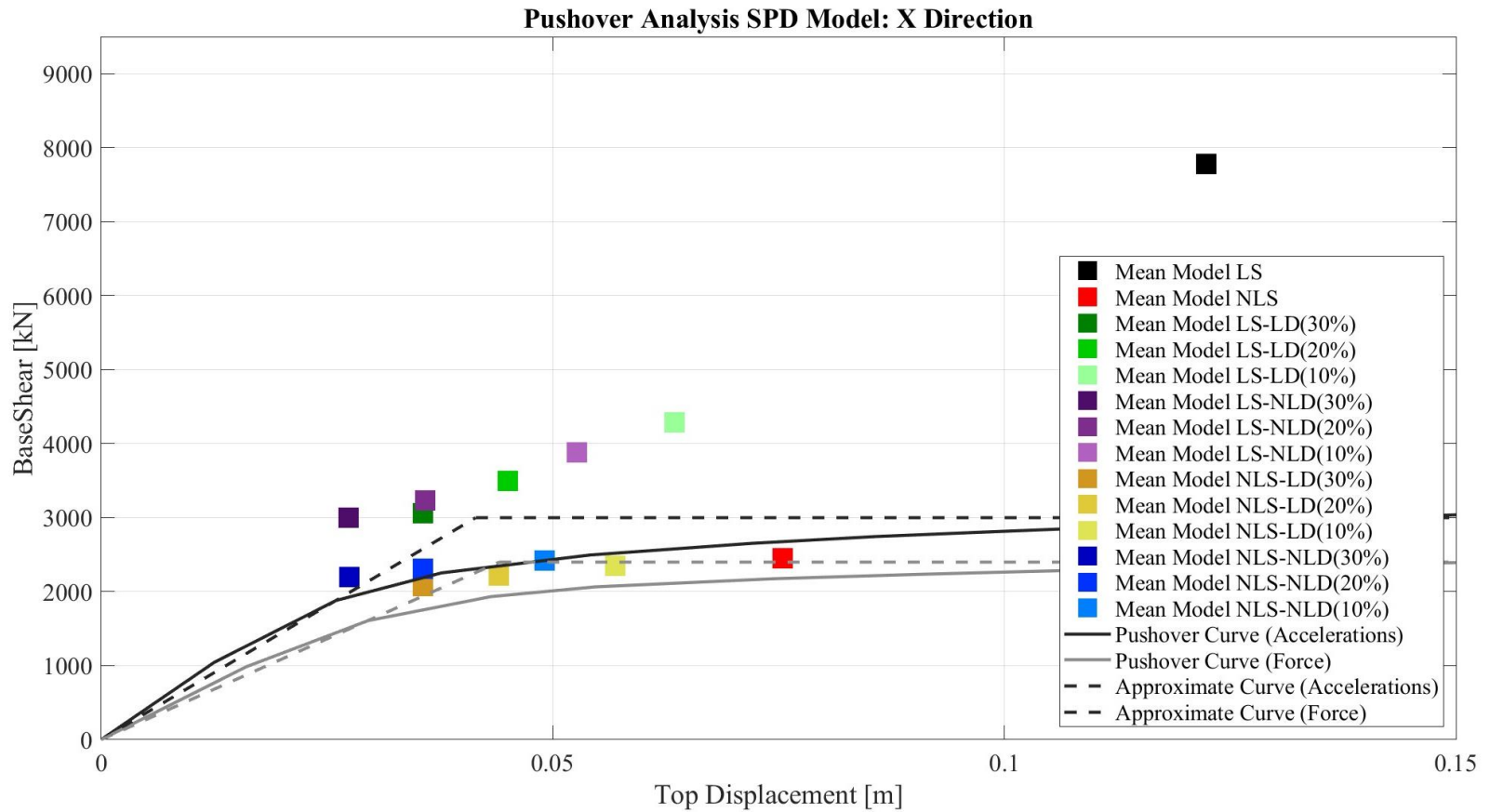


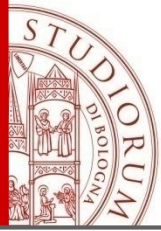
# TIME-HISTORY RESULTS (X Direction)



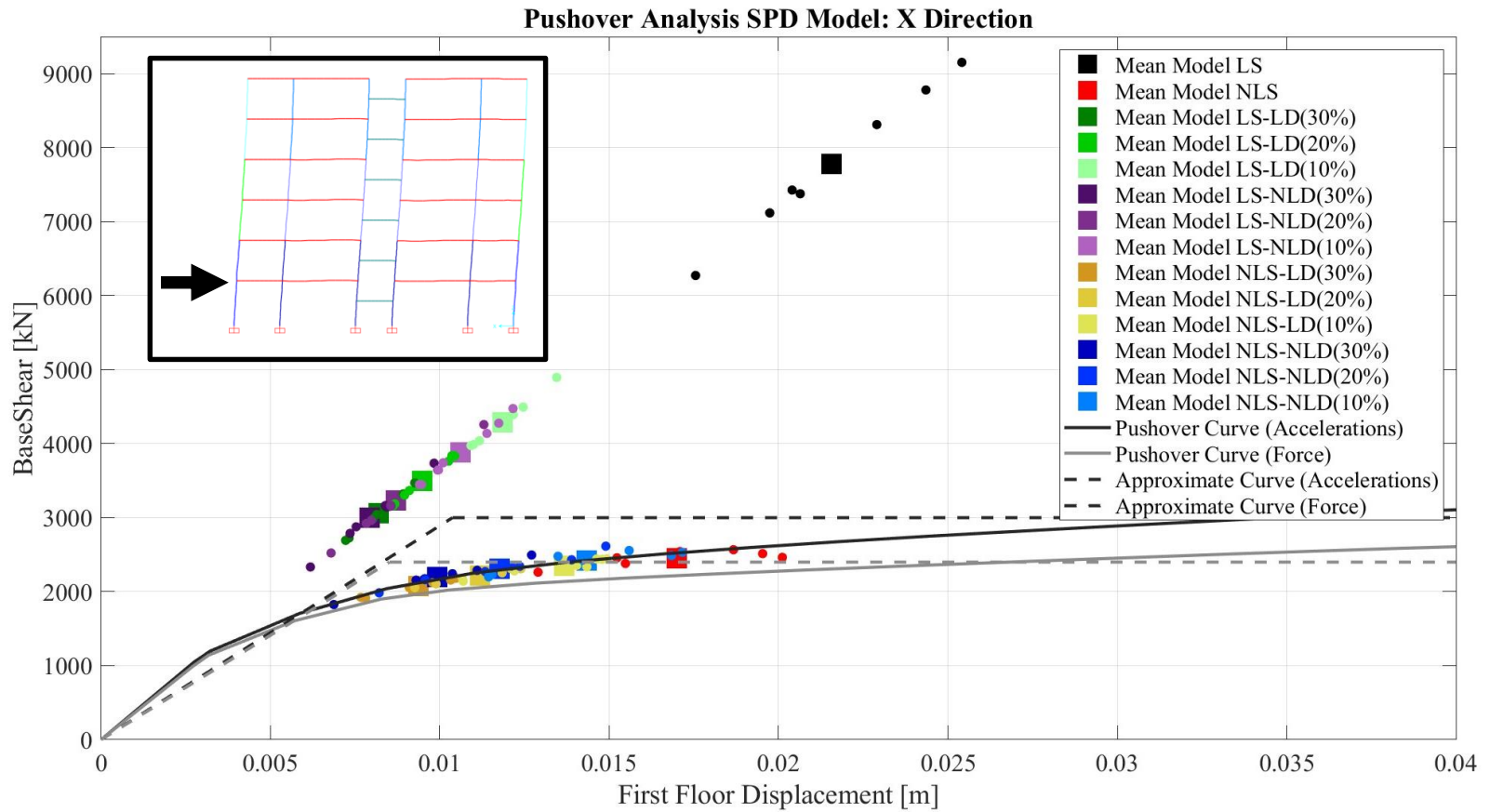


# TIME-HISTORY RESULTS (X Direction)

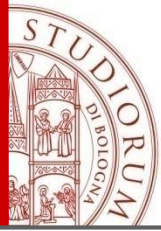




# TIME-HISTORY RESULTS (X Direction)

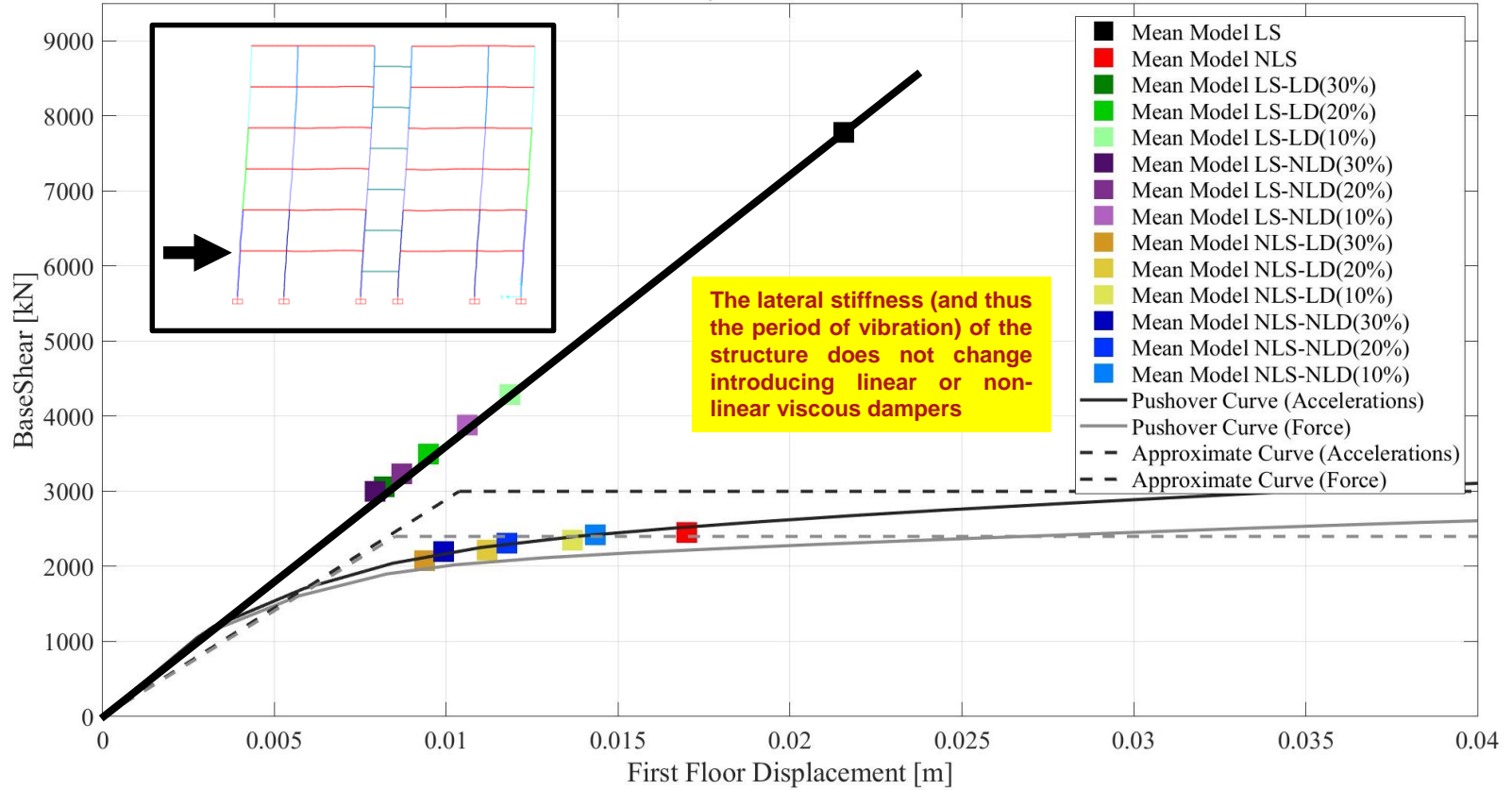






# TIME-HISTORY RESULTS (X Direction)

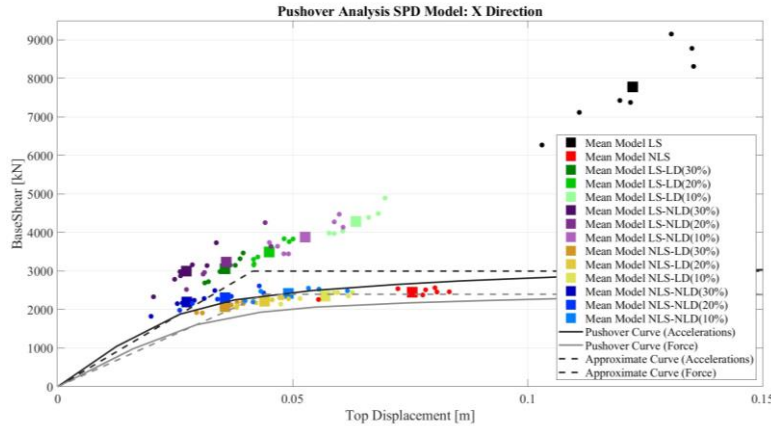
Pushover Analysis SPD Model: X Direction



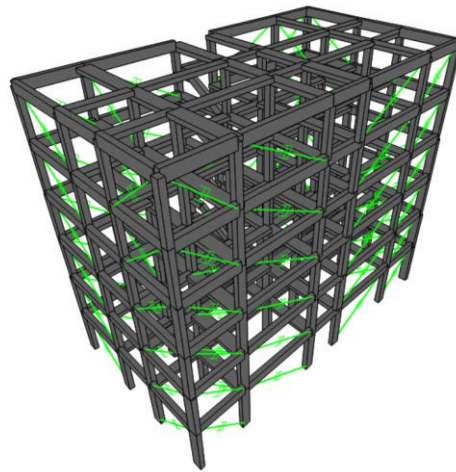
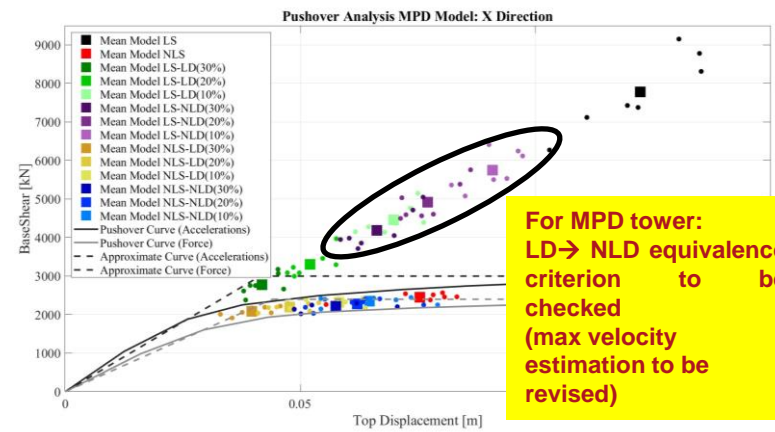
# COMPARISON SPD-MPD with same target damping ratio

6-storey new building

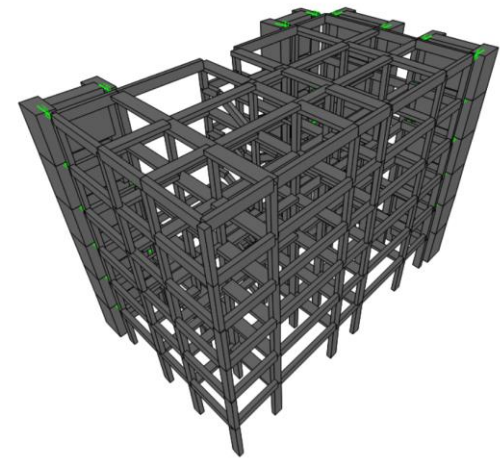
Interstorey viscous dampers



Dissipative links connected to external stiff towers

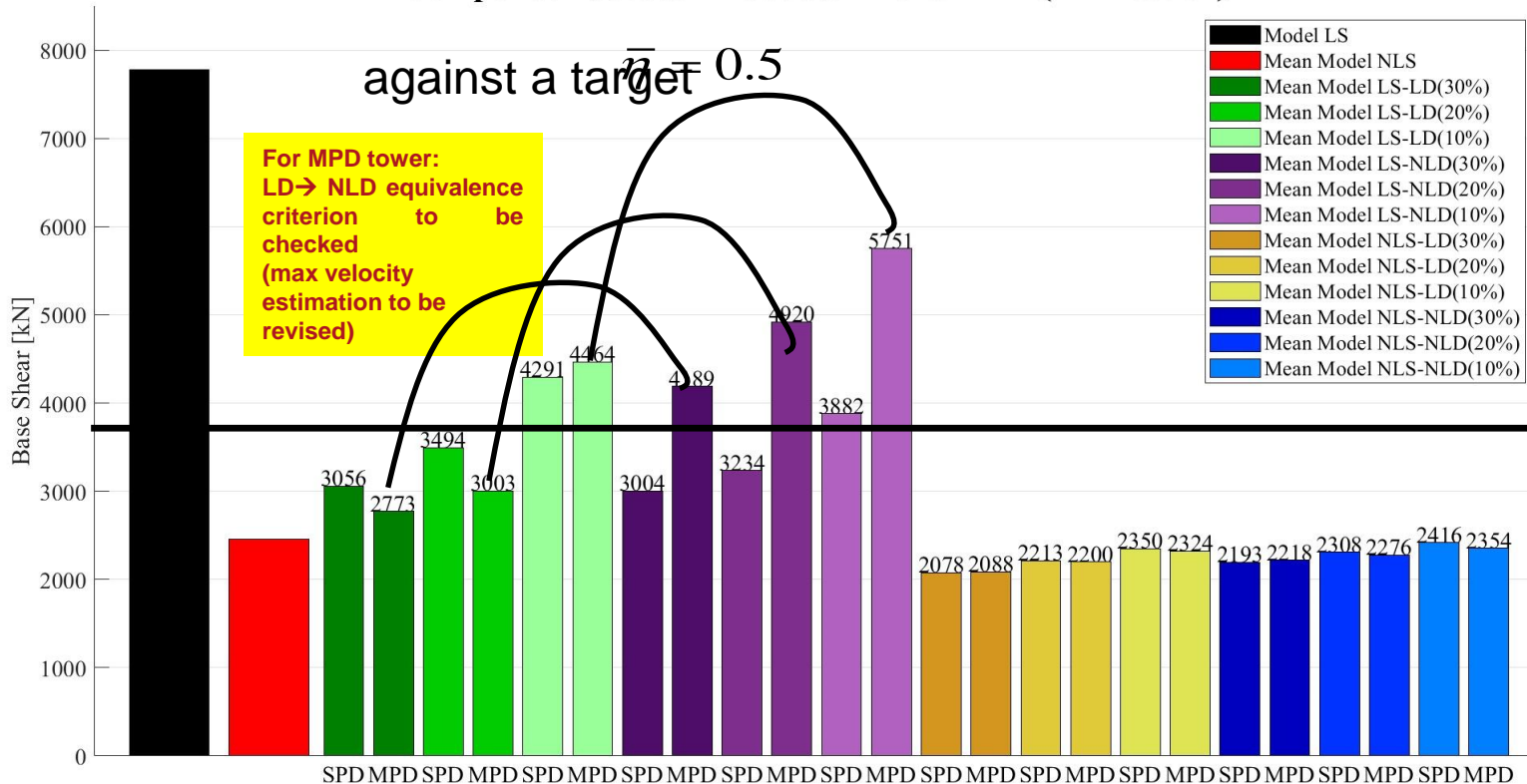


same  $\xi$



# COMPARISON SPD-MPD with same target damping ratio

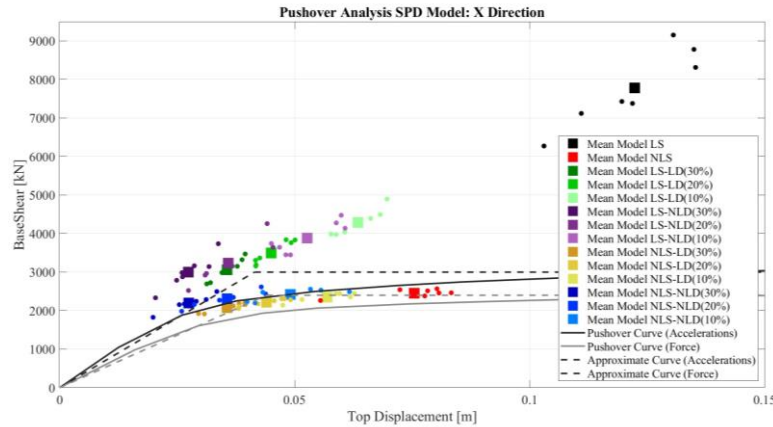
Comparison between models SPD and MPD (X Direction)



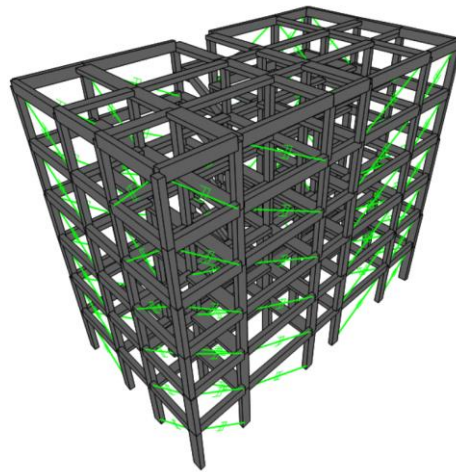
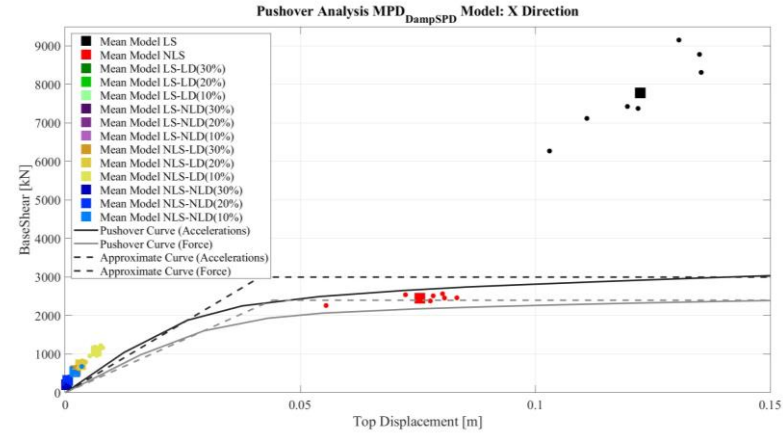
# COMPARISON SPD-MPD with same total c

6-storey new building

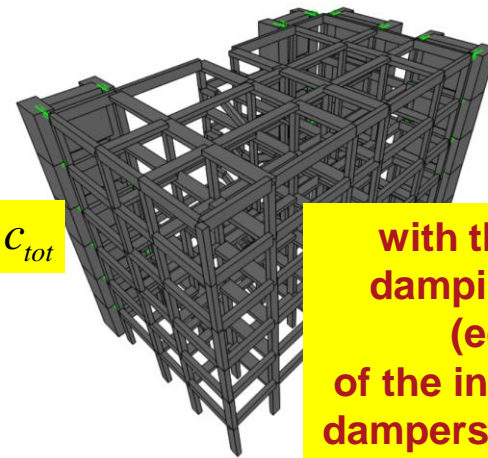
Interstorey viscous dampers



Dissipative links connected to external stiff towers



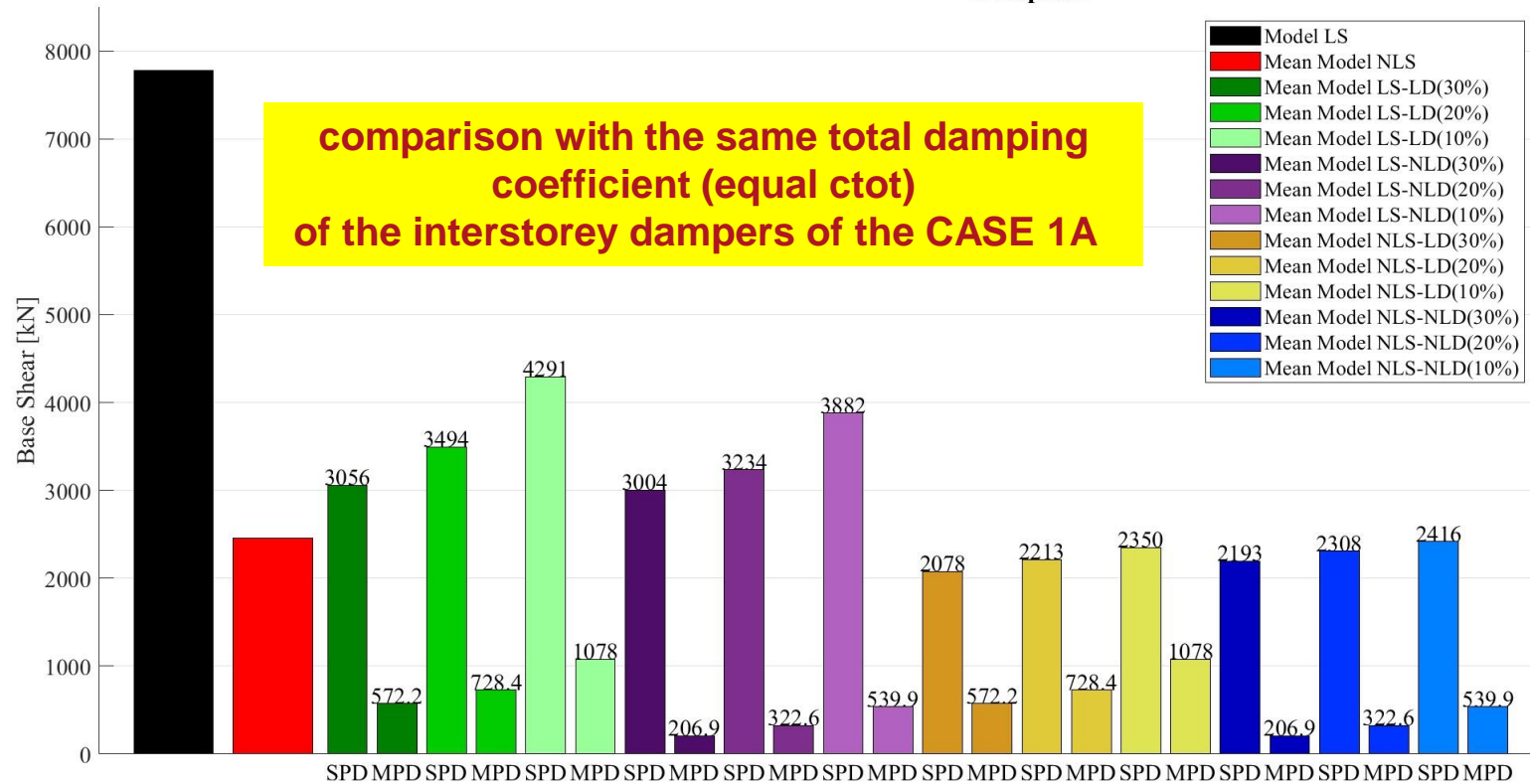
same  $c_{tot}$

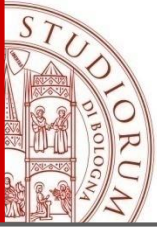


with the same total damping coefficient (equal  $c_{tot}$ ) of the interstorey dampers of the CASE 1A

# COMPARISON SPD-MPD with same total c

Comparison between models SPD and MPD<sub>DampSPD</sub> (X Direction)

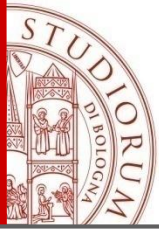




## **CASE 2**

11-storey existing RC frame building





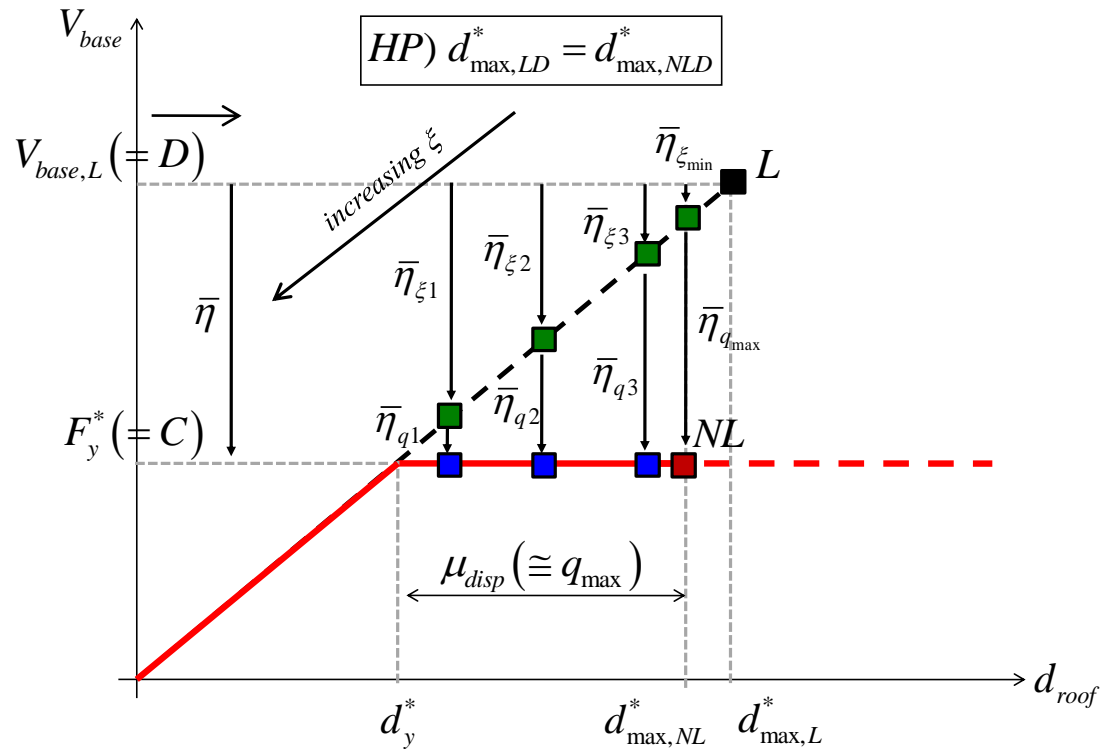
# DIRECT FIVE-STEP PROCEDURE FOR EXISTING BUILDINGS: REVISION OF STEP 1

several strategies:

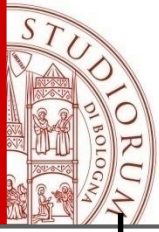
$$\bar{\eta} = \bar{\eta}_{q1} \cdot \bar{\eta}_{\xi1}$$

$$\bar{\eta} = \bar{\eta}_{q2} \cdot \bar{\eta}_{\xi2}$$

$$\bar{\eta} = \bar{\eta}_{q3} \cdot \bar{\eta}_{\xi3}$$



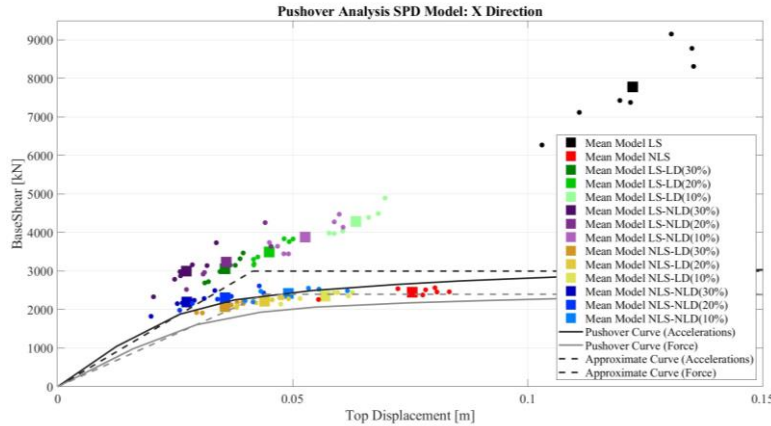




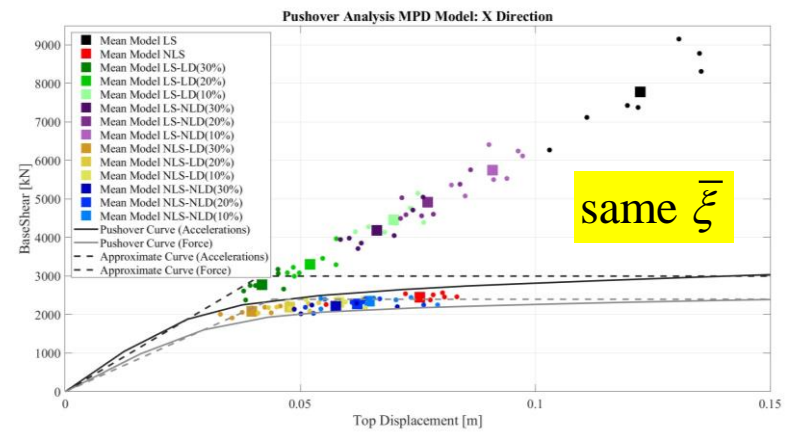
# COMPARISON SPD-MPD with same target damping ratio

6-storey new building

Interstorey viscous dampers



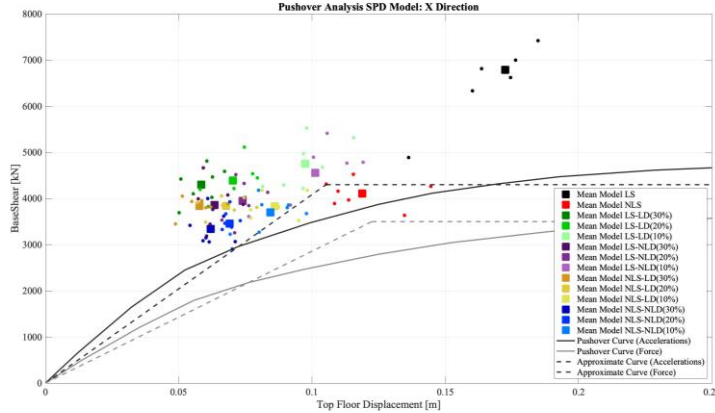
Dissipative links connected to external stiff towers



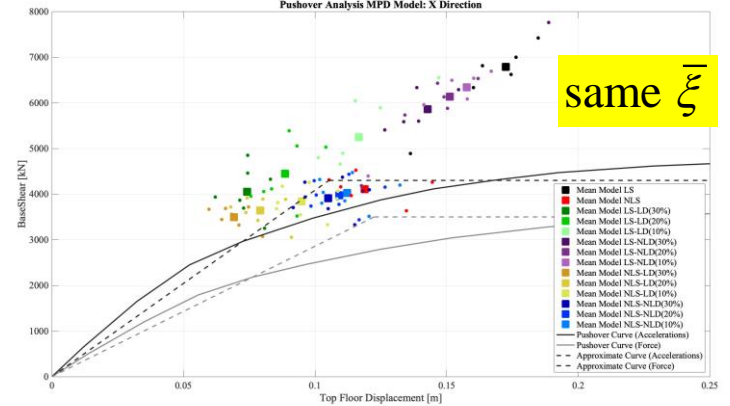
11-storey existing building



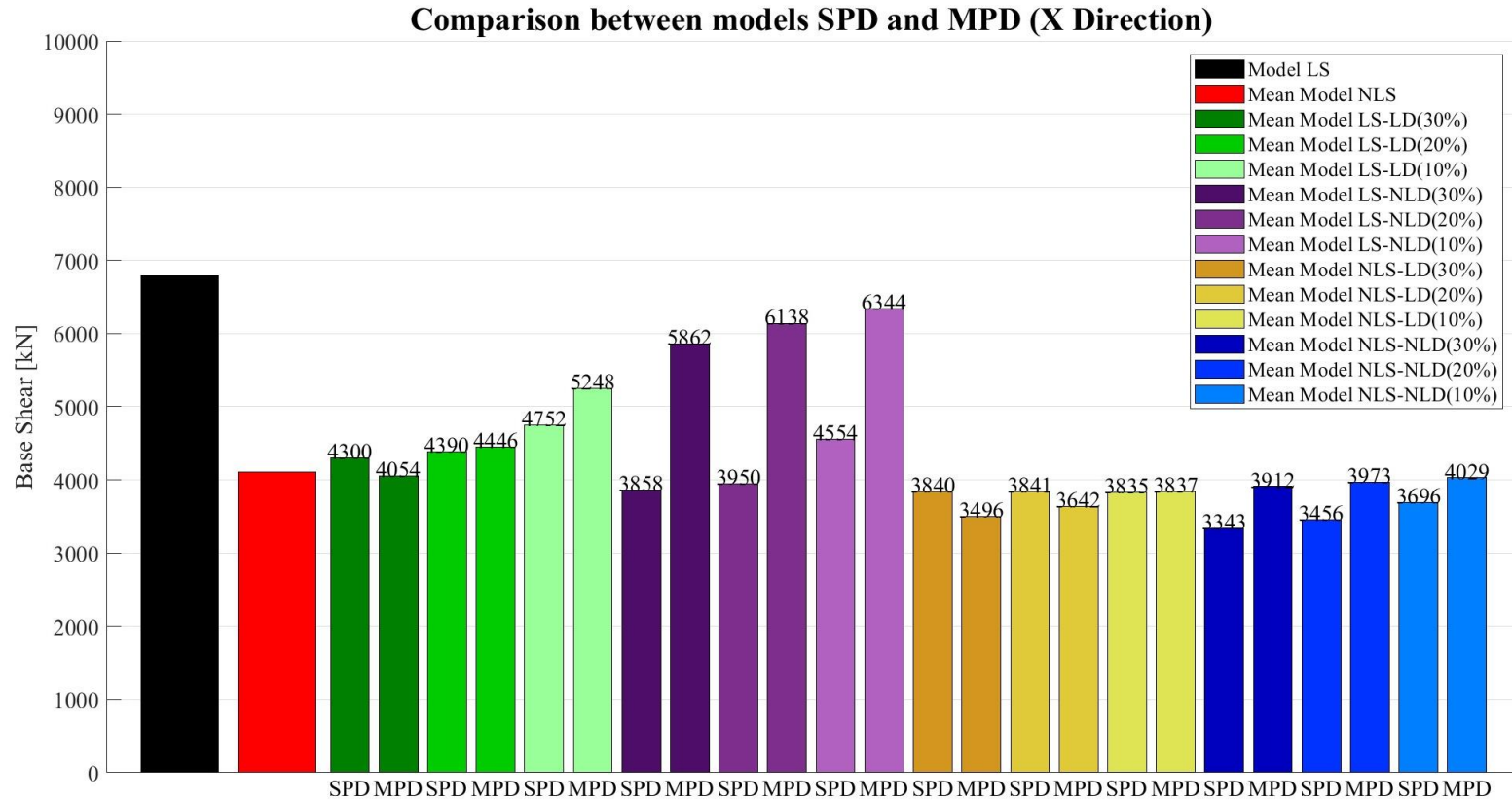
Pushover Analysis SPD Model: X Direction

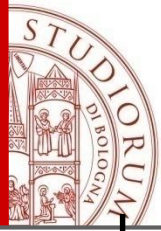


Pushover Analysis MPD Model: X Direction



# COMPARISON SPD-MPD with same target damping ratio

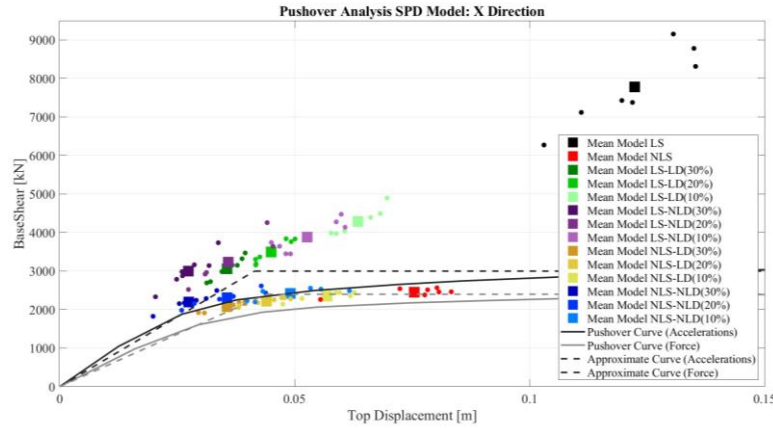




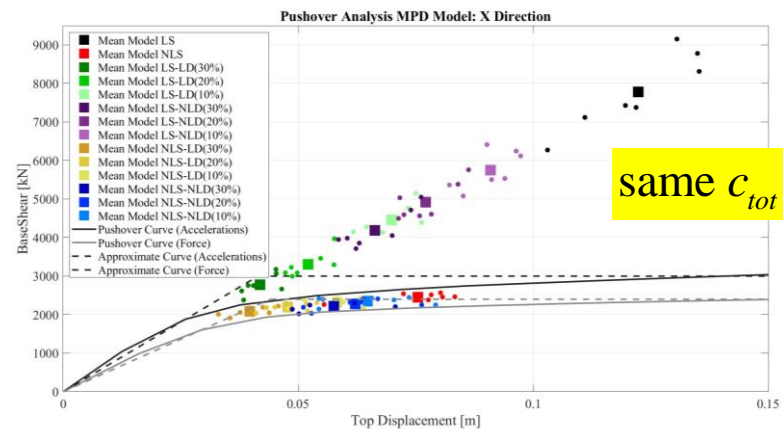
# COMPARISON SPD-MPD with same total c

6-storey new building

Interstorey viscous dampers



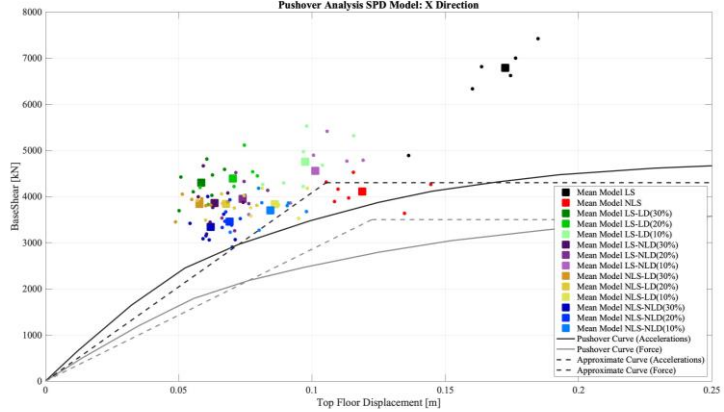
Dissipative links connected to external stiff towers



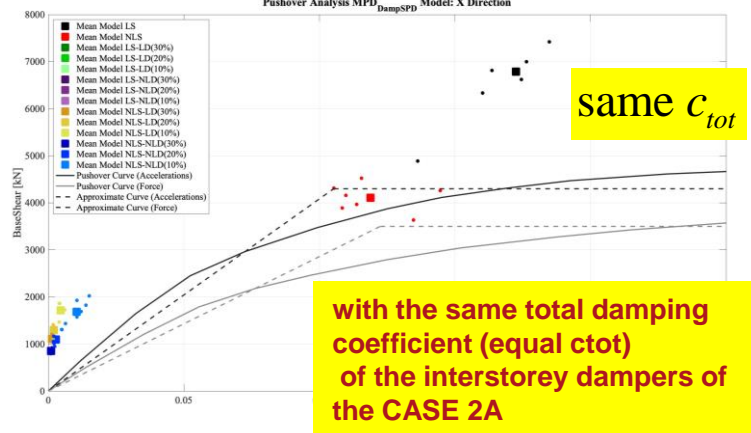
11-storey existing building



Pushover Analysis SPD Model: X Direction

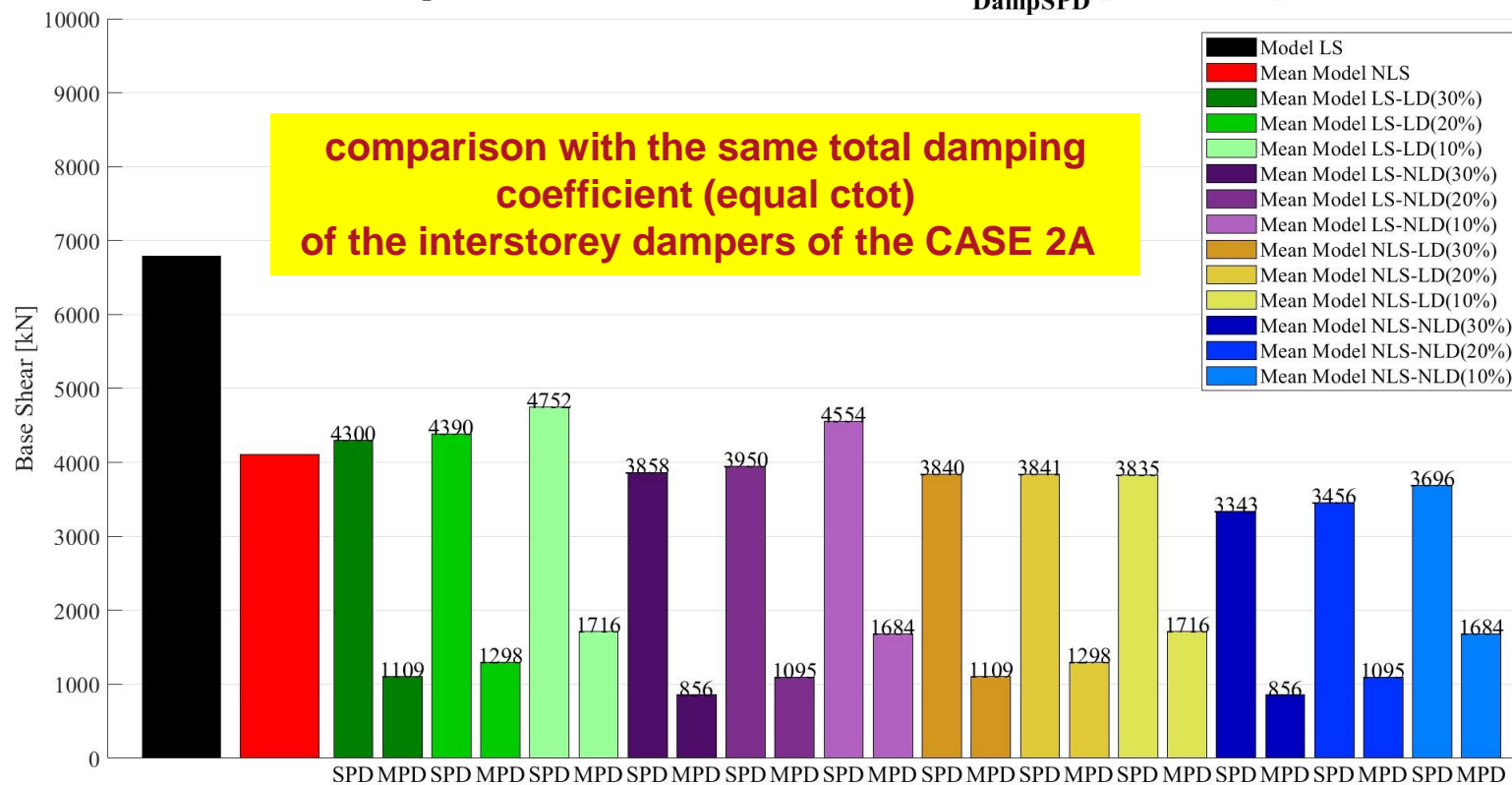


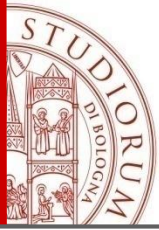
Pushover Analysis MPD<sub>DampSPD</sub> Model: X Direction



# COMPARISON SPD-MPD with same total c

Comparison between models SPD and MPD  $D_{ampSPD}$  (X Direction)





*Thank you!*

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